

# Implementation of lattice $s(x) - \bar{s}(x)$ in CT fits

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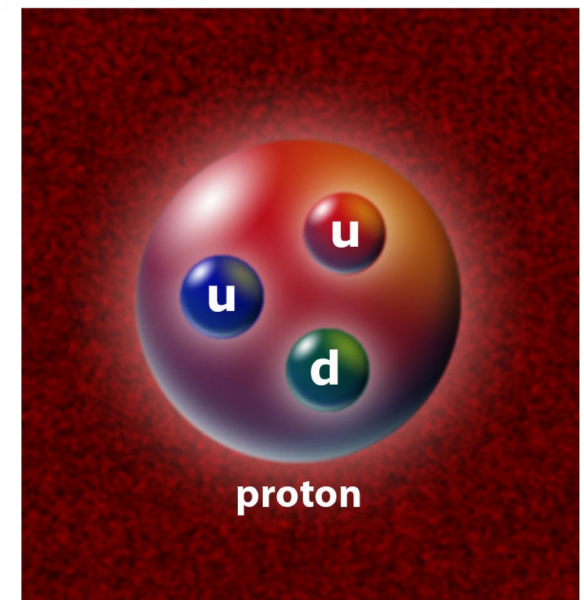
2022.0322  
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- The quark model predicts the content of proton to be uud, which is realized as the valence ingredient of proton. This resulting as the number sum rule:

$$\int_0^1 [u(x) - \bar{u}(x)] dx = 2 \quad \int_0^1 [d(x) - \bar{d}(x)] dx = 1$$

$$\int_0^1 dx [s(x) - \bar{s}(x)] = 0.$$

- The zero-number sum of strange lead to the different feature of  $s_v$  from  $u_v$  and  $d_v$ : half area of the  $s_v$  has to be negative.
- In CT18, we presume  $s = \bar{s}$ .



- People used to parametrize the strange as  $s^+ = (s + \bar{s})$  and  $s^- = (s - \bar{s})$  because the DGLAP equ. preserve the  $\text{Int}[s^-] = 0$ .
- The zero-number sum of strange is controlled by one parameter in  $s^-$  :

For ex. CTEQ 6

$$s^+(x, Q_0) = A_0 x^{A_1} (1 - x)^{A_2} P_+(x; A_3, A_4, \dots)$$

$$s^-(x, Q_0) = s^+(x, Q_0) \tanh[a x^b (1 - x)^c P_-(x; x_0, d, e, \dots)]$$

$$P_-(x) = \left(1 - \frac{x}{x_0}\right) (1 + dx + ex^2 + \dots)$$

MMHT2014/15/16/17/18/19

$$s_-(x, Q_0^2) = A_{s^-} (1 - x)^{\eta_{s^-}} (1 - x_0/x) x^{\delta_{s^-}}$$

- We consider an alternative way on parametrizing the strangeness. Consider both  $s$  and  $s\bar{b}$  contain an overall factor  $A$ :

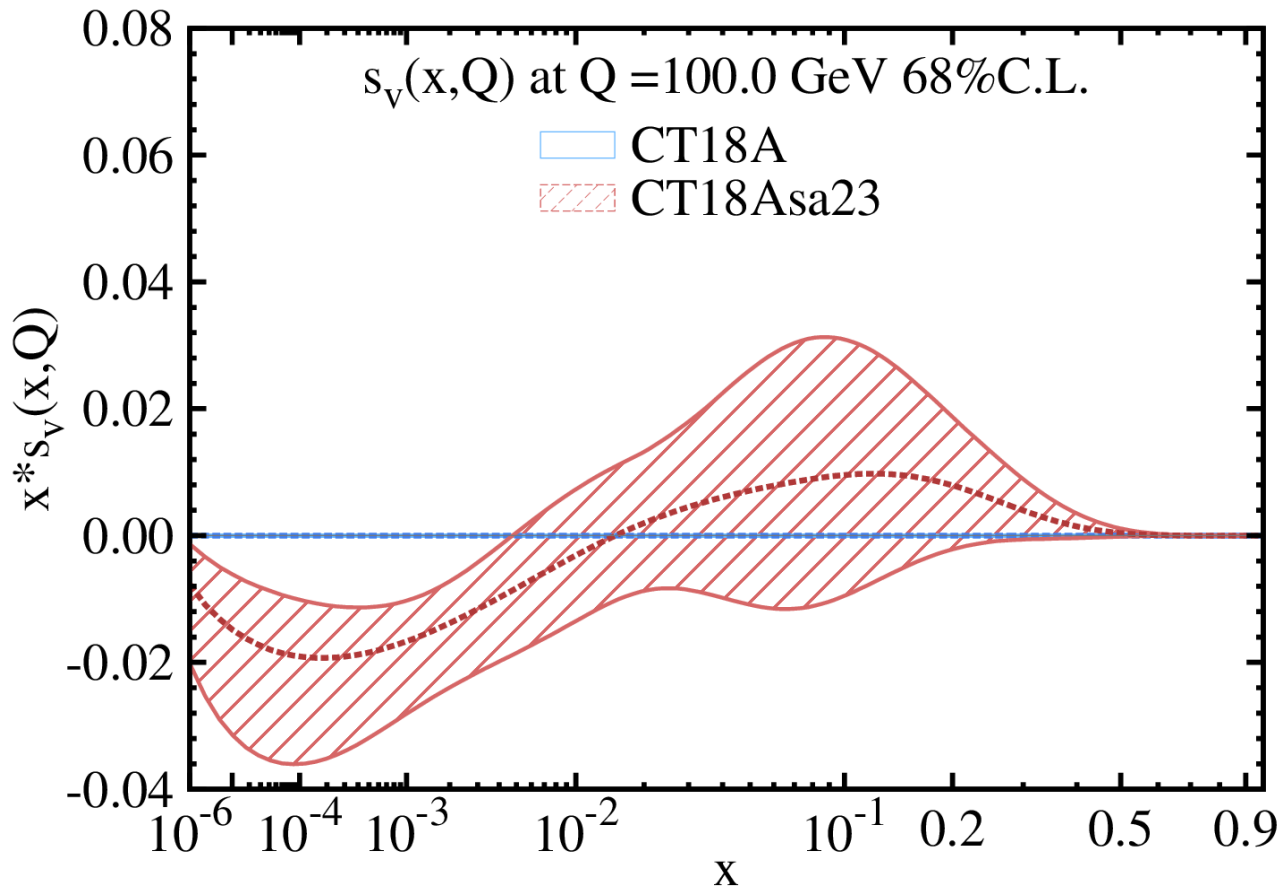
$$\int dx \left( A(s)g(s) - A(\bar{s})g(\bar{s}) \right) = 0$$

- By given  $A(s\bar{b})$  first and,

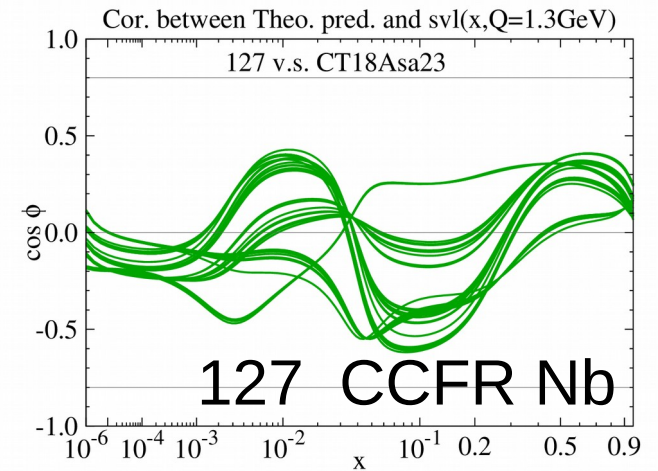
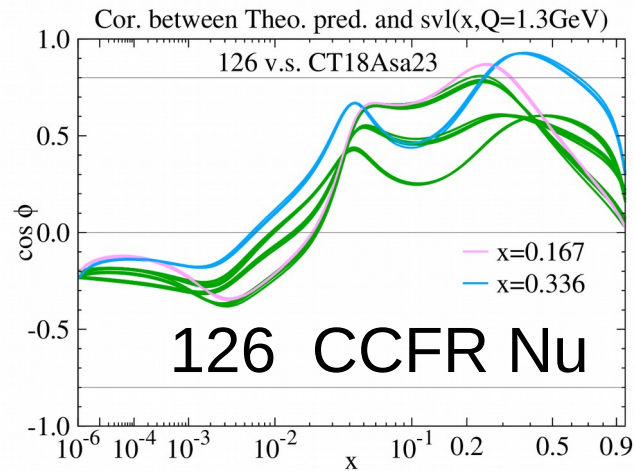
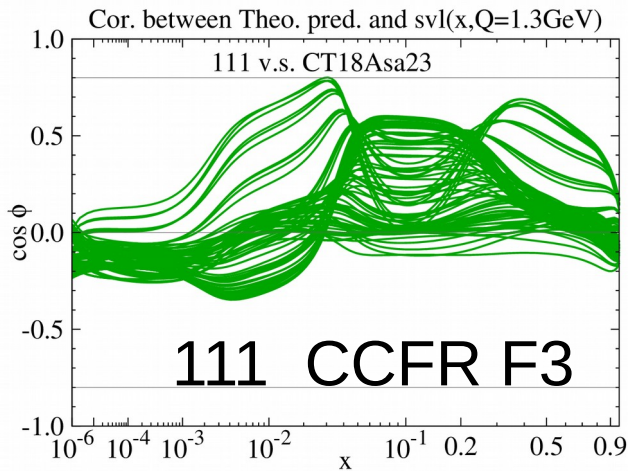
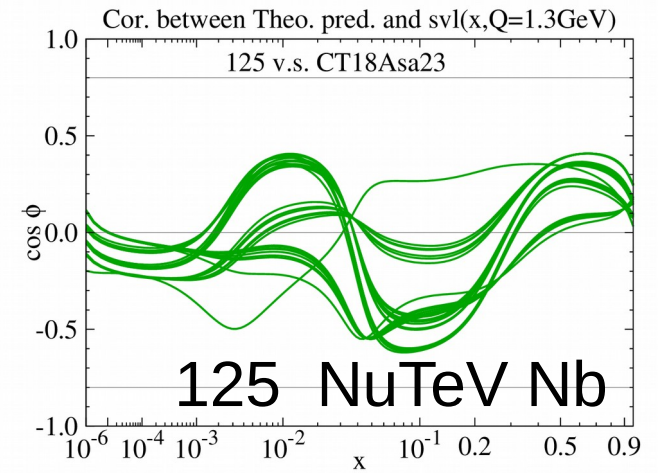
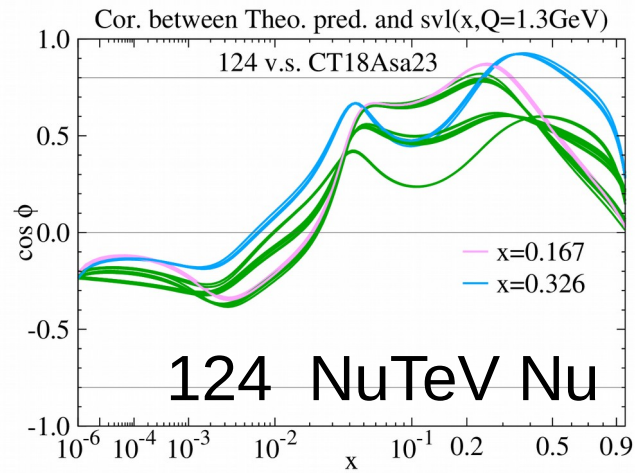
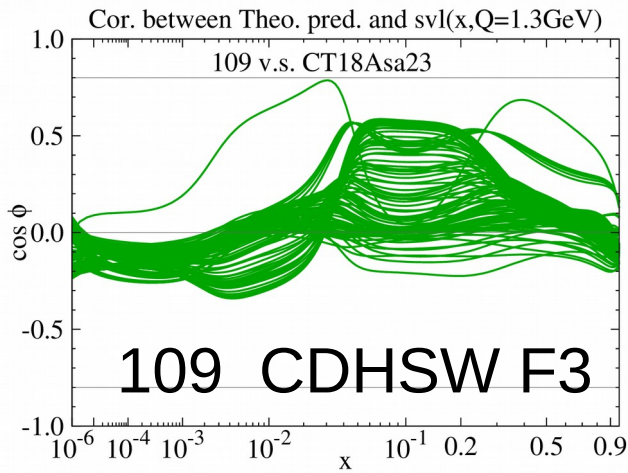
$$A(s) = \frac{\int dx A(\bar{s})g(\bar{s})}{\int dx g(s)}$$

The function of  $g(s)$  and  $g(s\bar{b})$  can be parametrized independently.

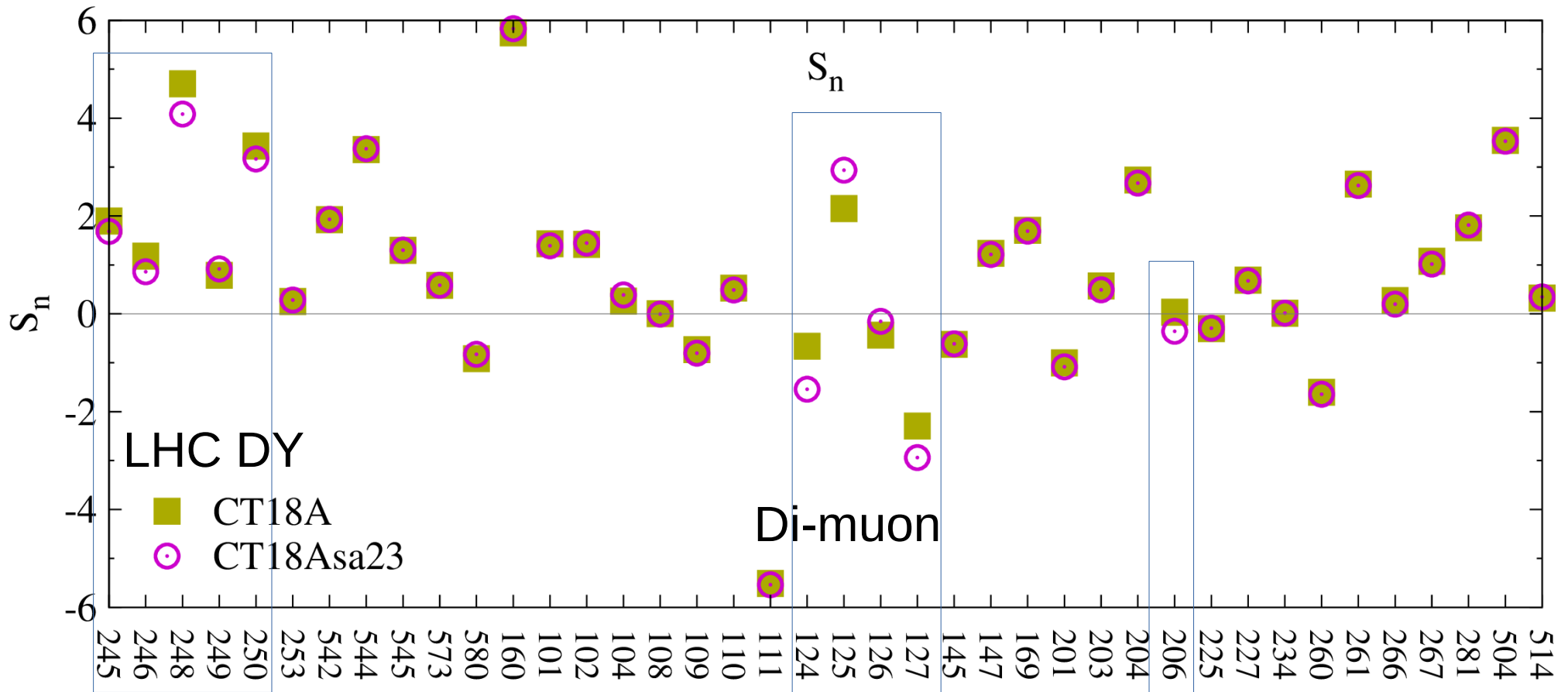
- Different from the root-finding method, there is no presumed requirement on the function of  $g(s)$  and  $g(s\bar{b})$ . But it is relatively hard to control the number of crossing in  $s$ - $s\bar{b}$ .



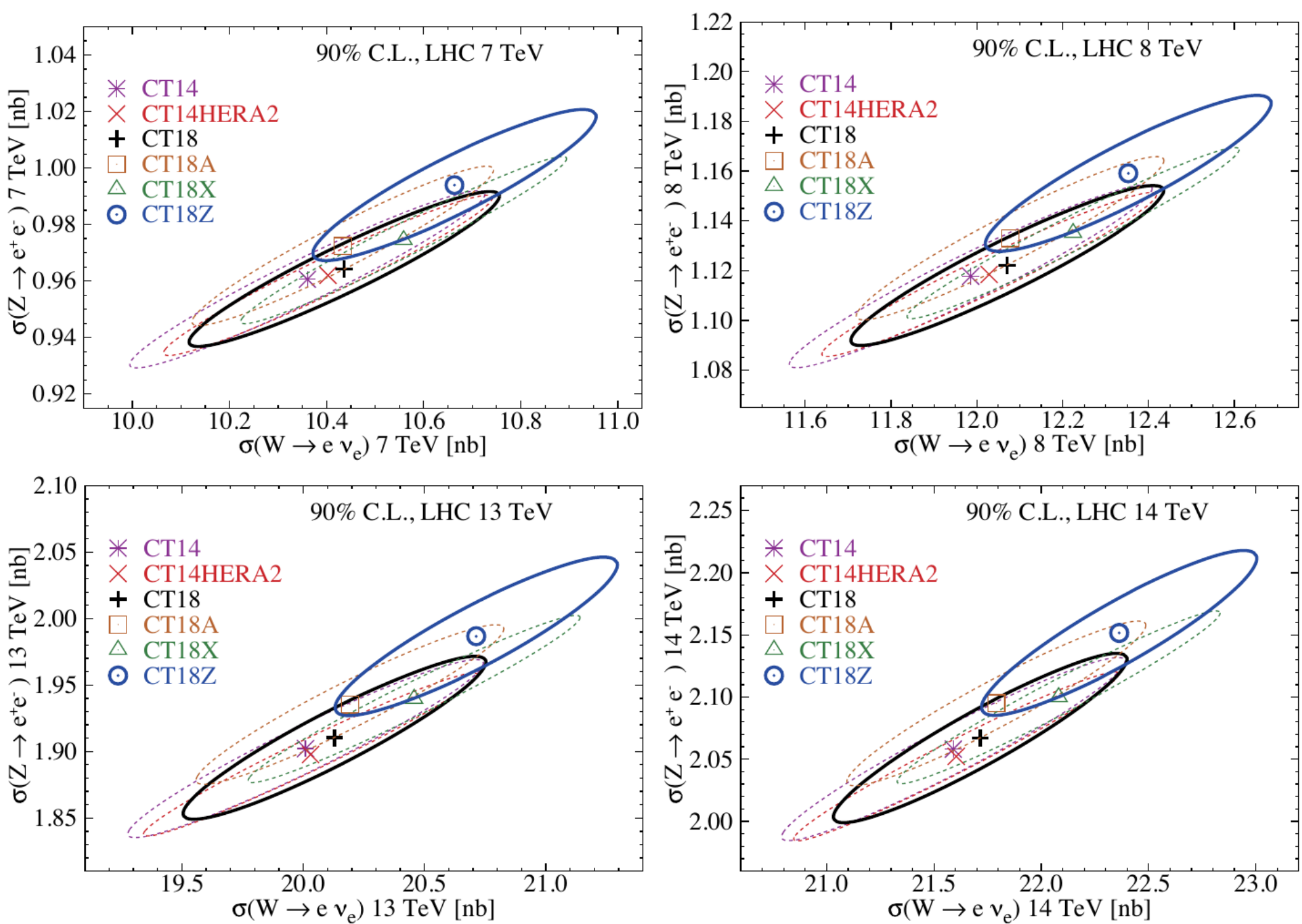
- Starting from CT18A, which contains the ATLAS 7 TeV ZW data(248), we select the strange asymmetry with one crossing from various trial parametrizations.



- Naively, we expect the F\_3 data and di-muon data would be sensitive to the  $s_v$  the most, and the correlation between  $s_v$  and data also agree with this expectation.

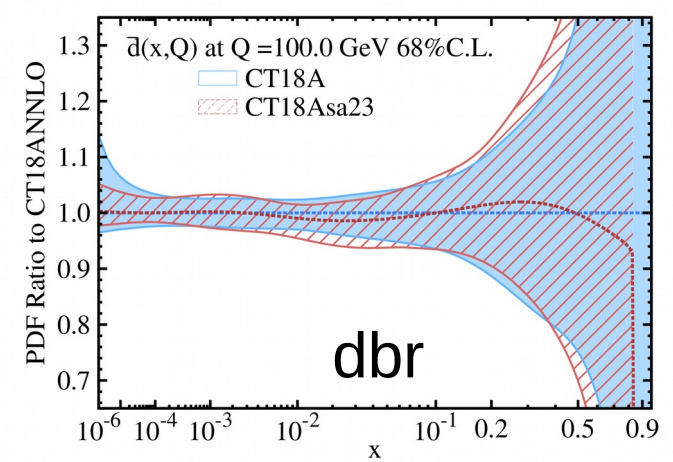
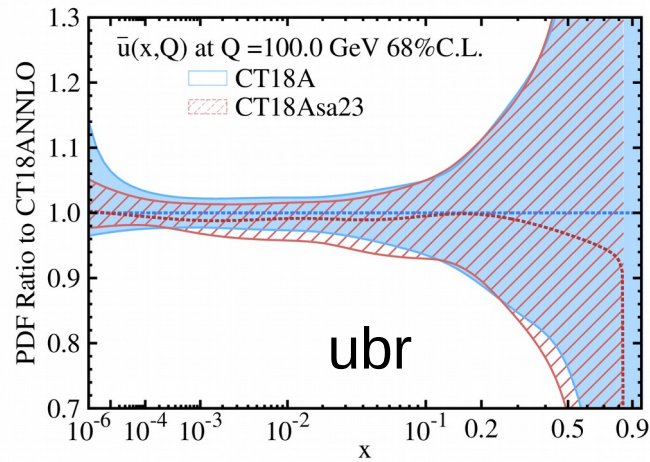
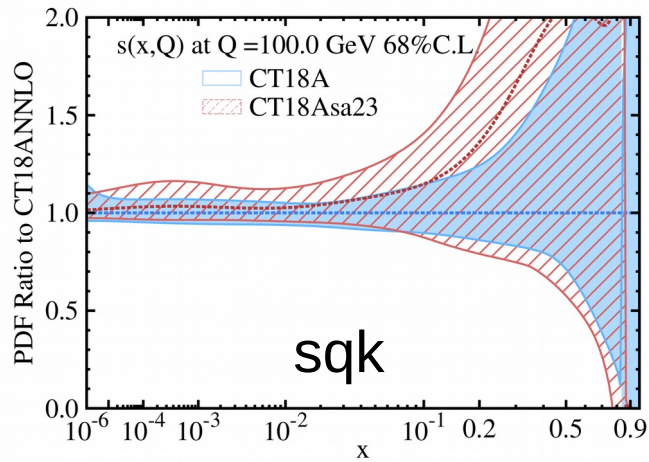
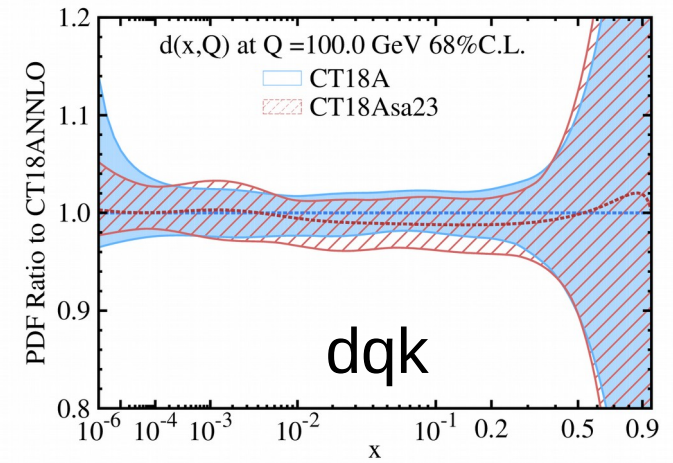
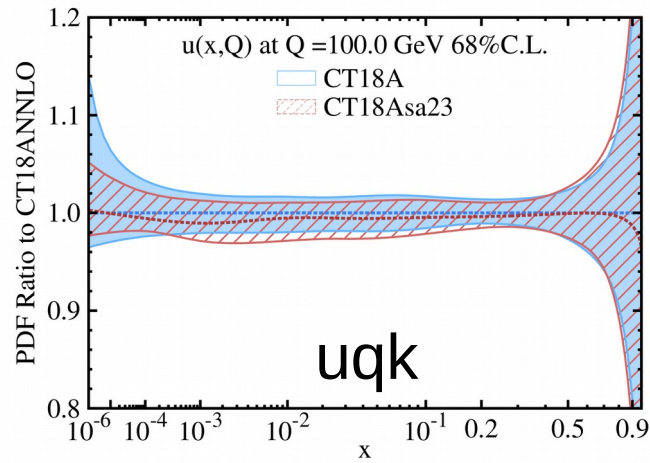
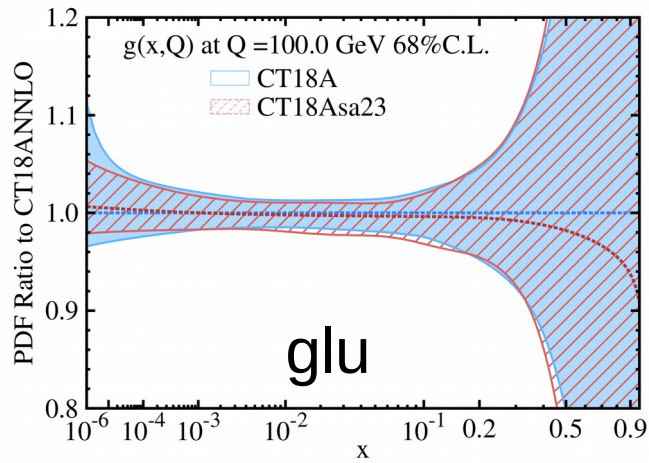


- The changing in Gaussian variable  $S_n$  shows, besides the di-muon data, it is the LHC Drell-Yan measurements, i.e. 245, 246, 248, 250, sensitive to  $s_v$ ; the F\_3 data 109 and 111 are not precise enough to constraint  $s_v$ .



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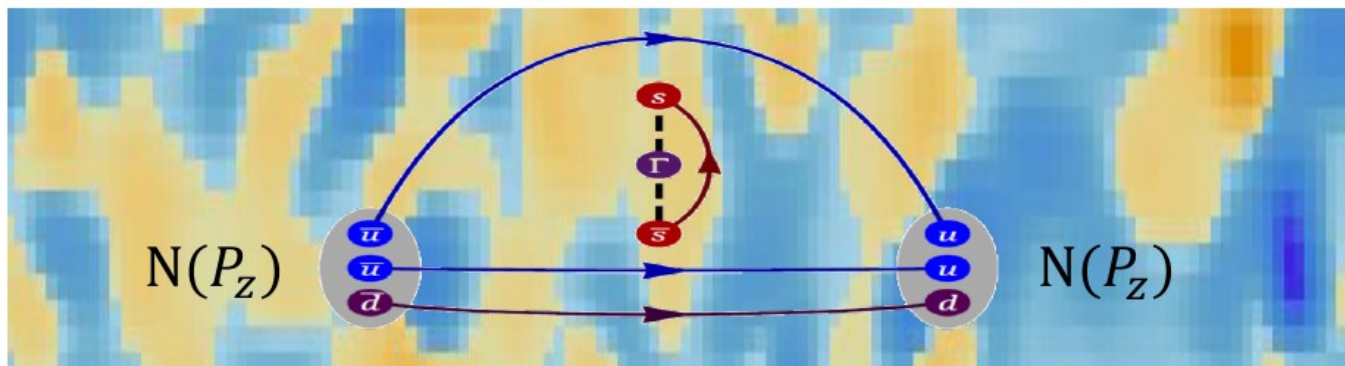




- The inclusion of non-zero  $s_v$  lead to the reduction of u and d quark, and enhancement of strange and its uncertainty.

# First Lattice Strange PDF

§ On the lattice, one needs to calculate the following



2005.12015, Zhang, Lin, Yoon

§ Results by MSULat/quasi-PDF method

⇒ Clover on 2+1+1 HISQ 0.12-fm 310-MeV QCD vacuum

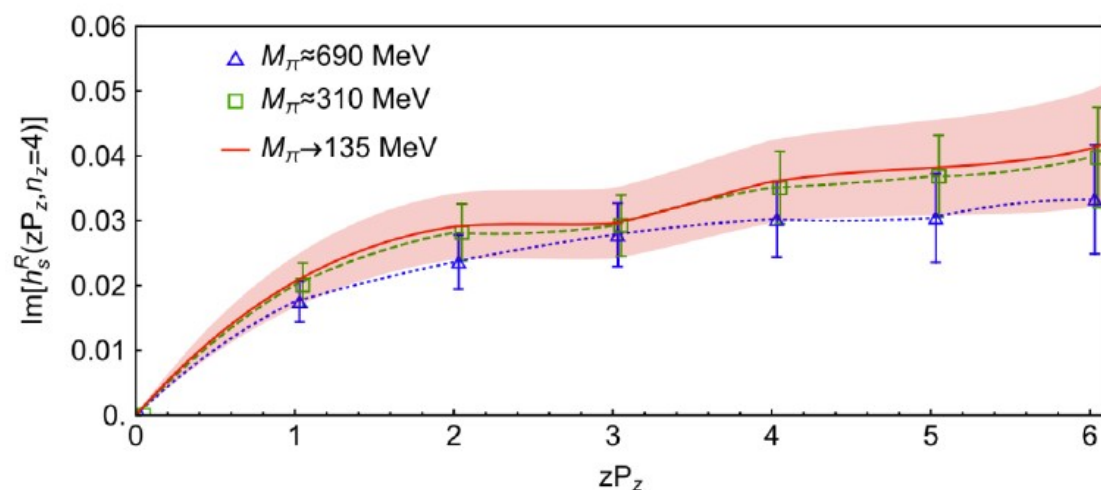
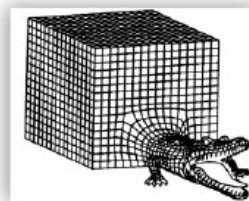
⇒ 7,184,000 strange loops

⇒ 344,832 nucleon correlators

⇒ RI/MOM renormalization

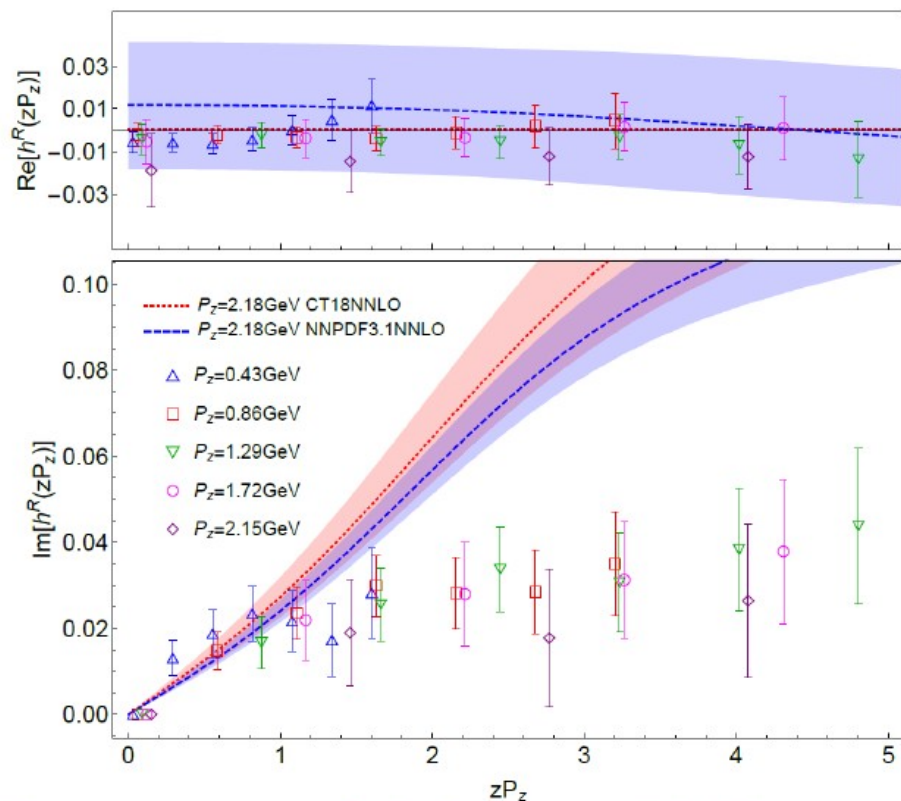
⇒ Extrapolated to

$$M_\pi \approx 140 \text{ MeV}$$



# First Lattice Strange PDF

## § Lattice matrix elements



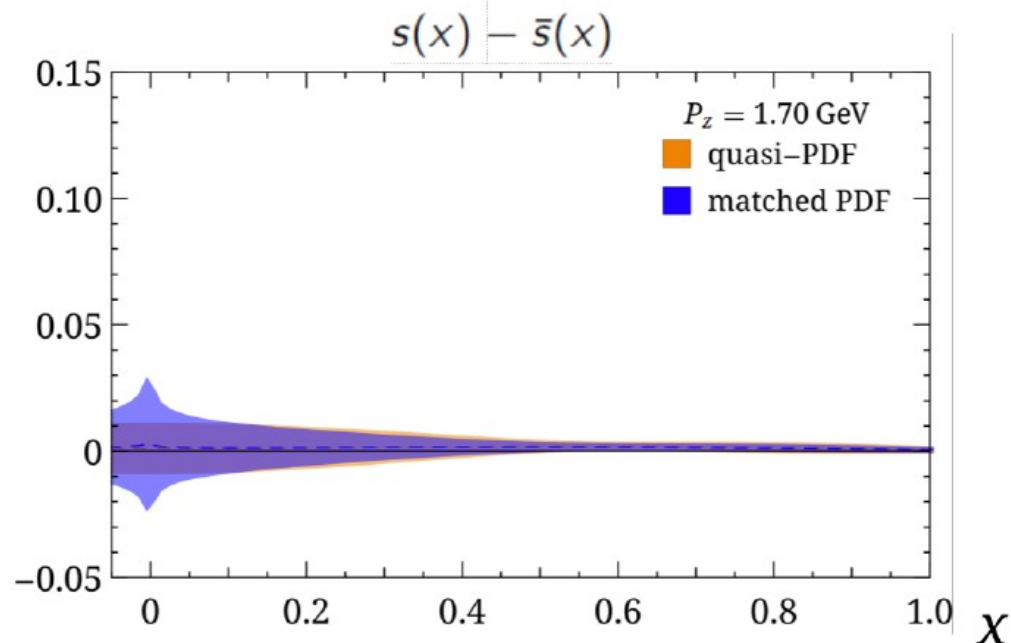
∞ Strange-antistrange symmetry

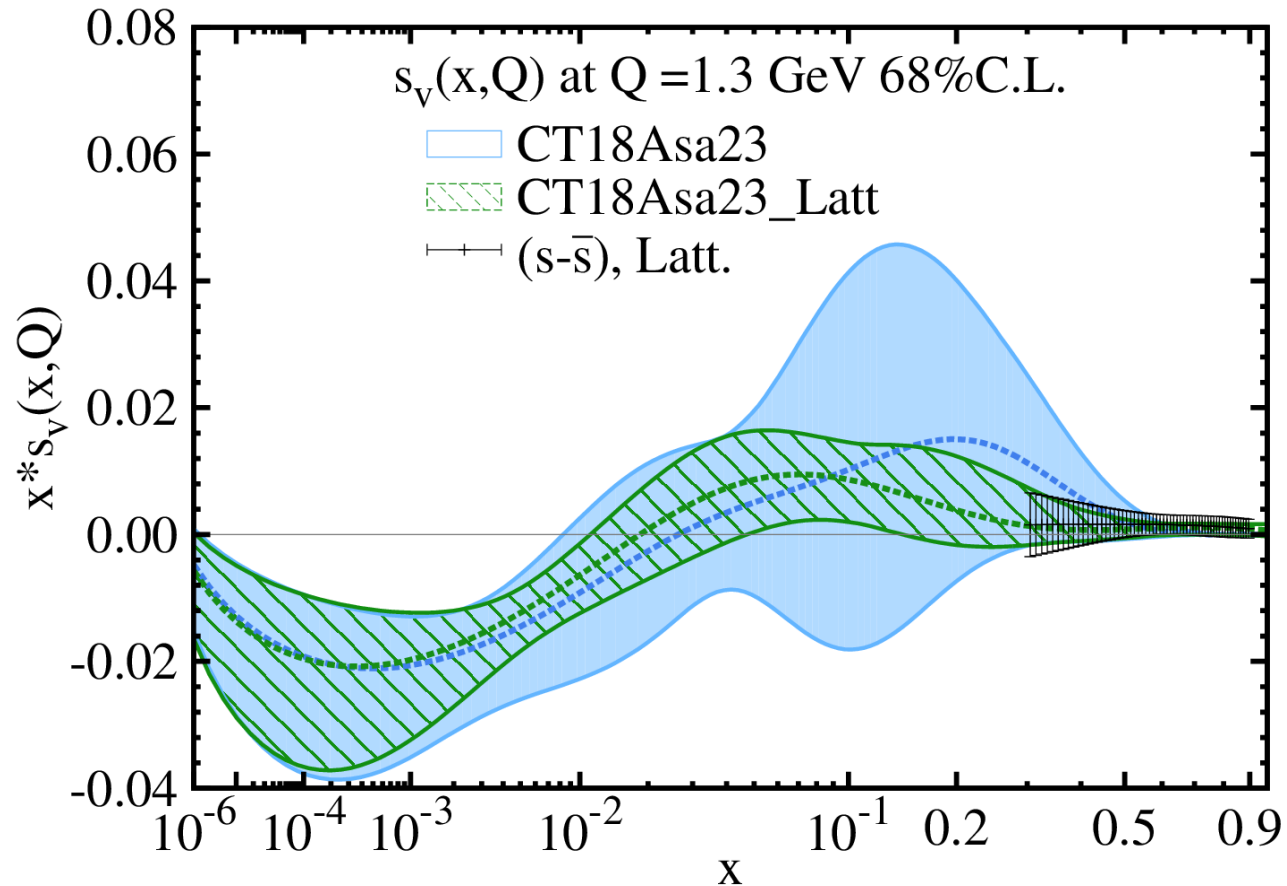
$$\text{Re}[h(z)] \propto \int dx (s(x) - \bar{s}(x)) \cos(xzP_z)$$

$$\text{Im}[h(z)] \propto \int dx (s(x) + \bar{s}(x)) \sin(xzP_z)$$

## § From quasi-PDF to PDF

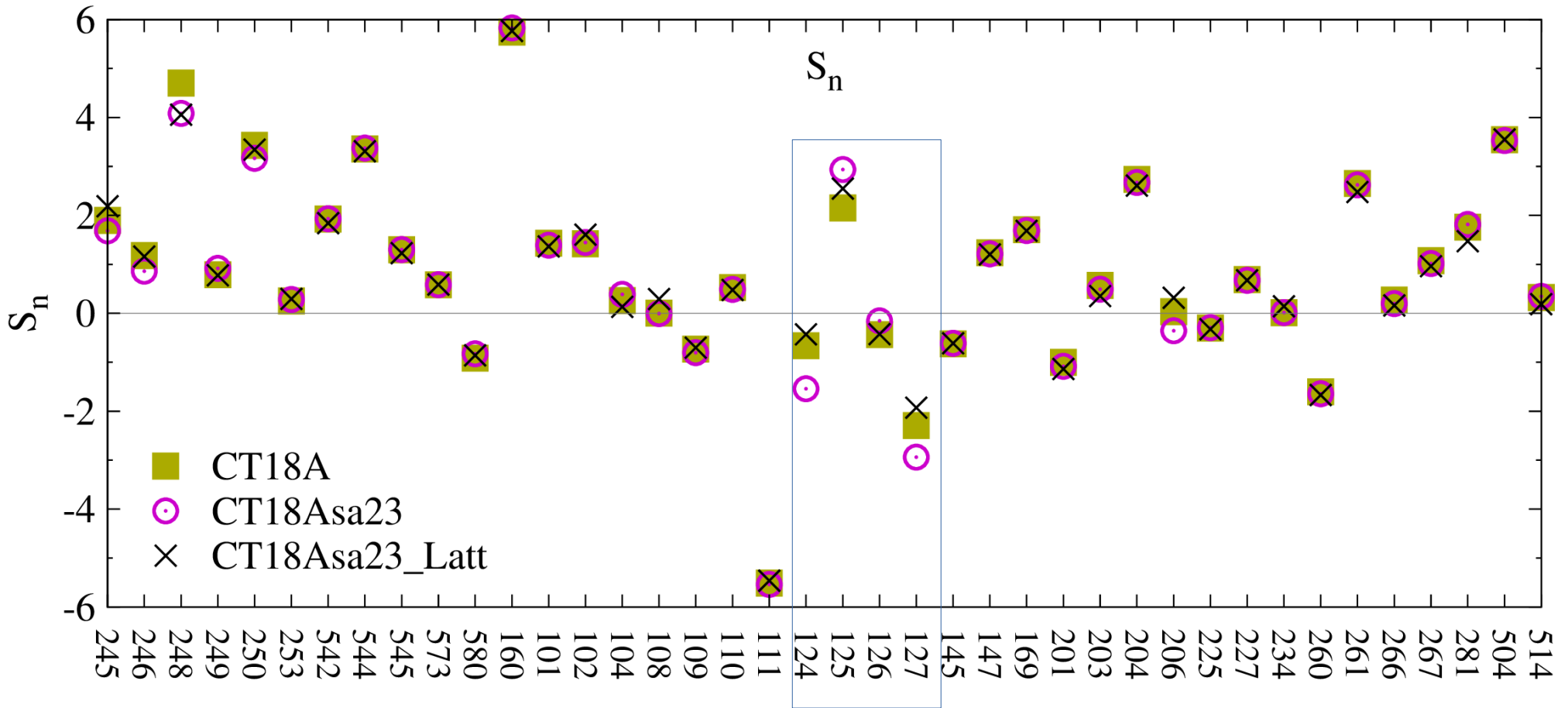
$$\tilde{f}_q(x, P_z) = \int_{-1}^1 \frac{dy}{|y|} f_q(y) C_{q/q}(x, y, P_z, \mu) + O\left(\frac{\Lambda_{QCD}^2}{x^2 P_z^2}, \frac{\Lambda_{QCD}^2}{(1-x)^2 P_z^2}\right)$$



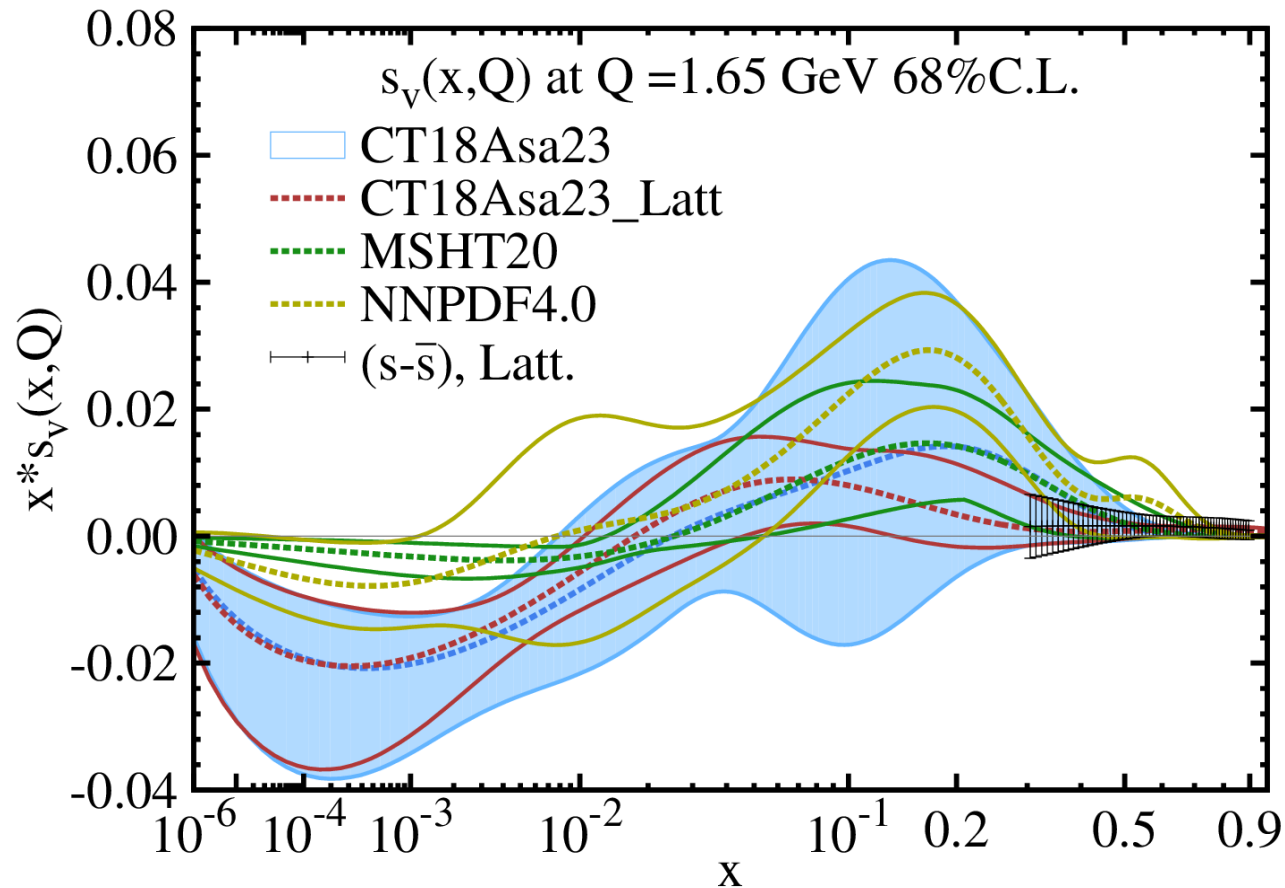


- The lattice calculation constraint the  $s_v$  for  $0.3 < x < 0.9$ , which overlap with the  $x$  region of di-muon data,  $0.015 < x < 0.336$ .
- The lattice constraint is treated as data:

$$\chi_{tot}^2 = \chi^2 + w \sum_i \left( \frac{f(x_i, Q) - f_{Latt}(x_i, Q)}{\epsilon_{Latt}} \right)^2$$



- The lattice calculation has little tension with the di-muon data.



- The central prediction of  $s_v$  in CT18Asa23 (blue) is almost identical to that of MSHT20 for  $x > 0.01$ , but with much larger uncertainty.
- Inclusion of constraint from lattice would pull down the central prediction of  $s_v$  and reduce the uncertainty.

# Summery

- Starting from CT18A, we consider non-zero  $s_v(x,Q)$  by using more flexible method.
- Not just the di-muon data NuTeV and CCFR, the LHC precise Drell-Yan data also sensitive to the  $s_v$ , while the  $F_3$  data CDHSW and CCFR are not precise enough to constraint  $s_v$ .
- By treating lattice calculation as data, the  $s_v$  receive strong constraint on both central prediction and uncertainty in large- $x$  region.