

Progress in *Ab Initio* Nuclear Theory for Neutrinoless Double Beta Decay

Heiko Hergert

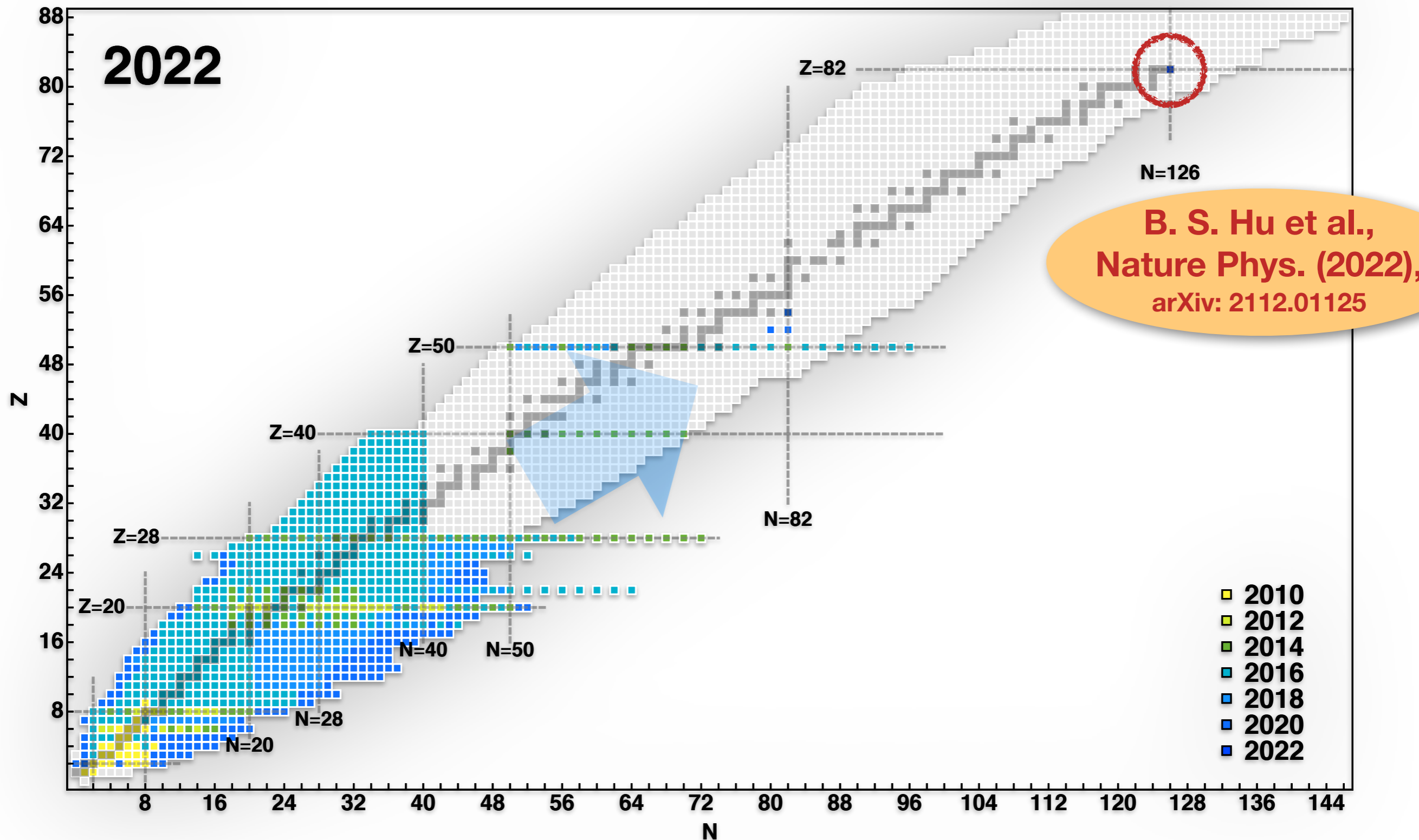
Facility for Rare Isotope Beams
& Department of Physics and Astronomy
Michigan State University



Progress in *Ab Initio* Calculations



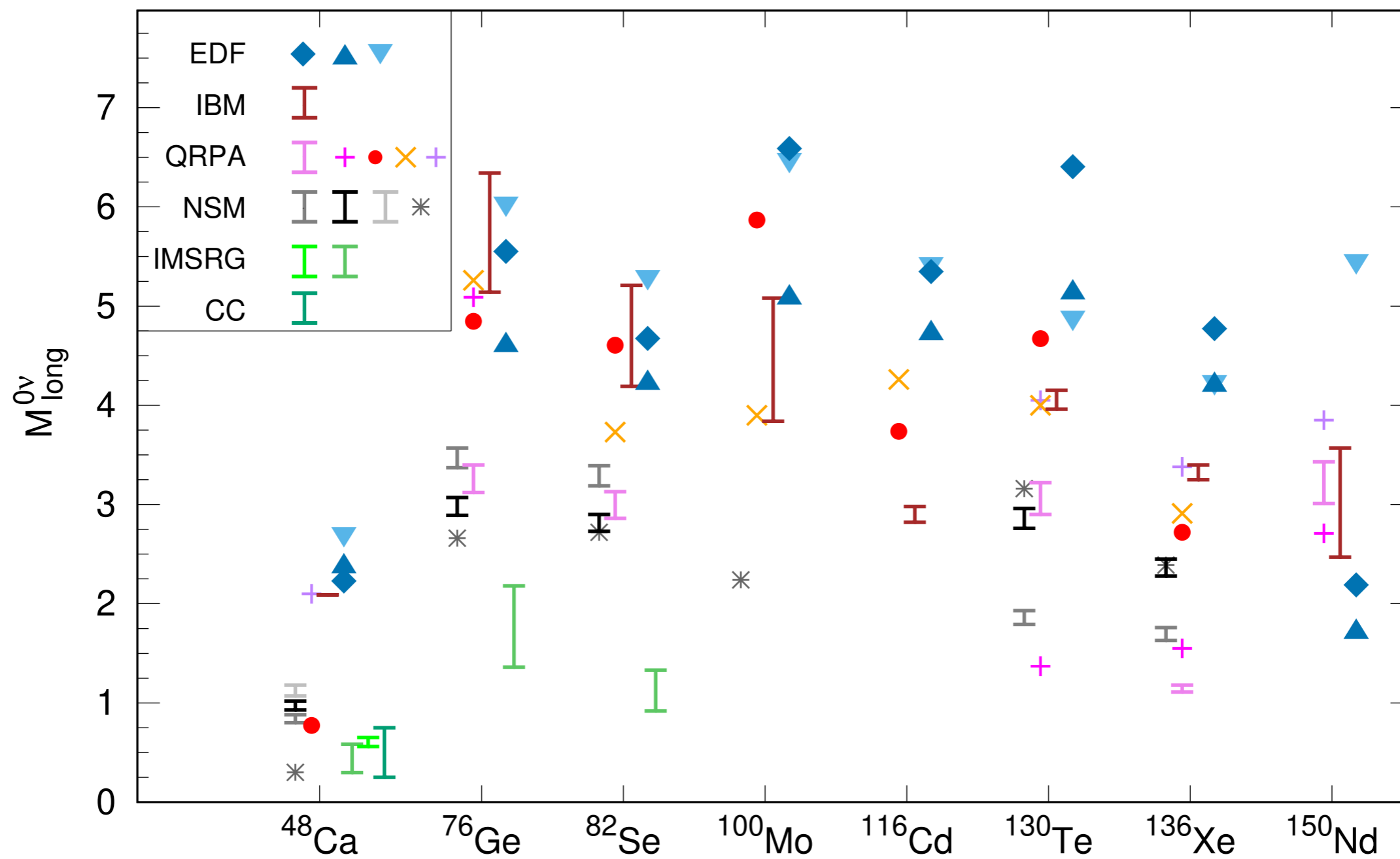
[cf. HH, *Front. Phys.* 8, 379 (2020)]



Nuclear Matrix Elements: Status



M. Agostini et al., to appear in RMP, arXiv: 2202.01787



(Multi-Reference) In-Medium Similarity Renormalization Group

HH, Phys. Scripta **92**, 023002 (2017)

HH, S. K. Bogner, T. D. Morris, A. Schwenk, and K. Tsukiyama, Phys. Rept. **621**, 165 (2016)

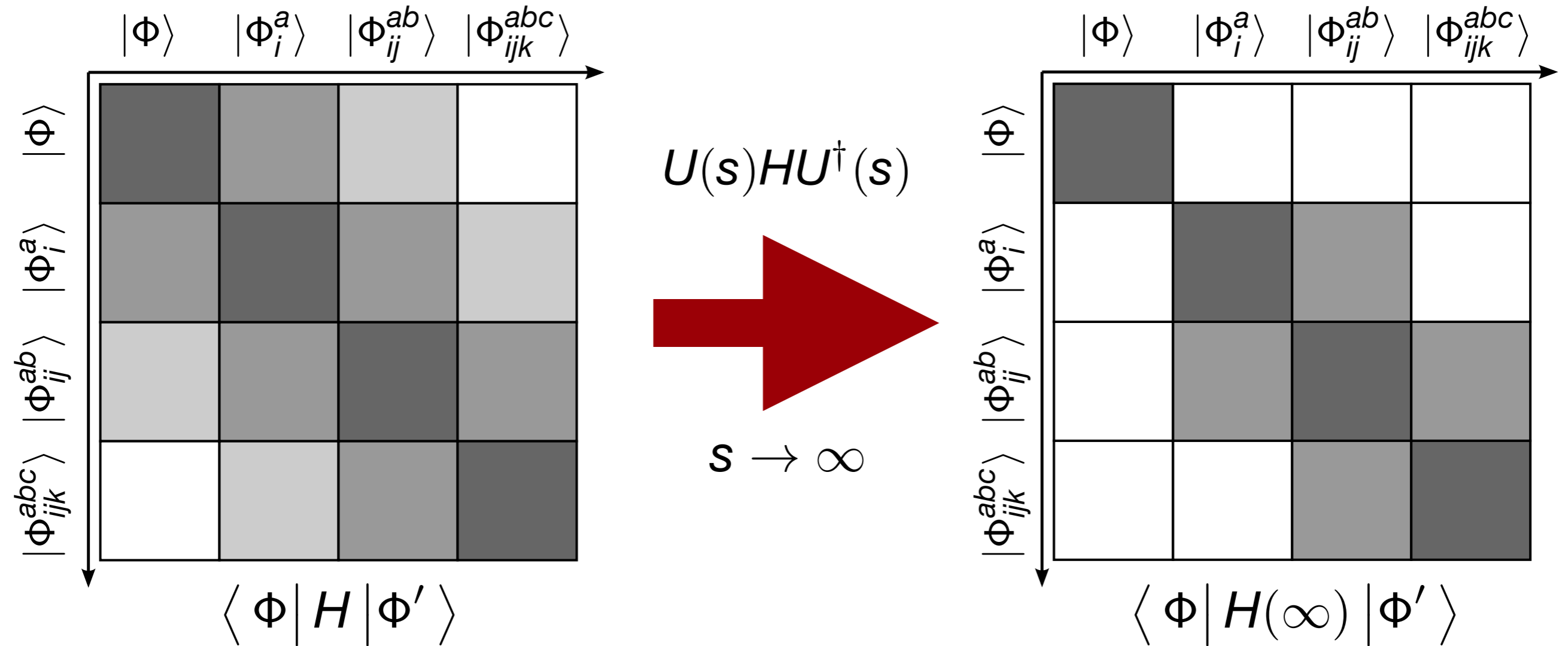
HH, S. K. Bogner, T. Morris, S. Binder, A. Calci, J. Langhammer, R. Roth, Phys. Rev. C **90**, 041302 (2014)

HH, S. Binder, A. Calci, J. Langhammer, and R. Roth, Phys. Rev. Lett **110**, 242501 (2013)

K. Tsukiyama, S. K. Bogner, A. Schwenk, PRL **106**, 222502 (2011)

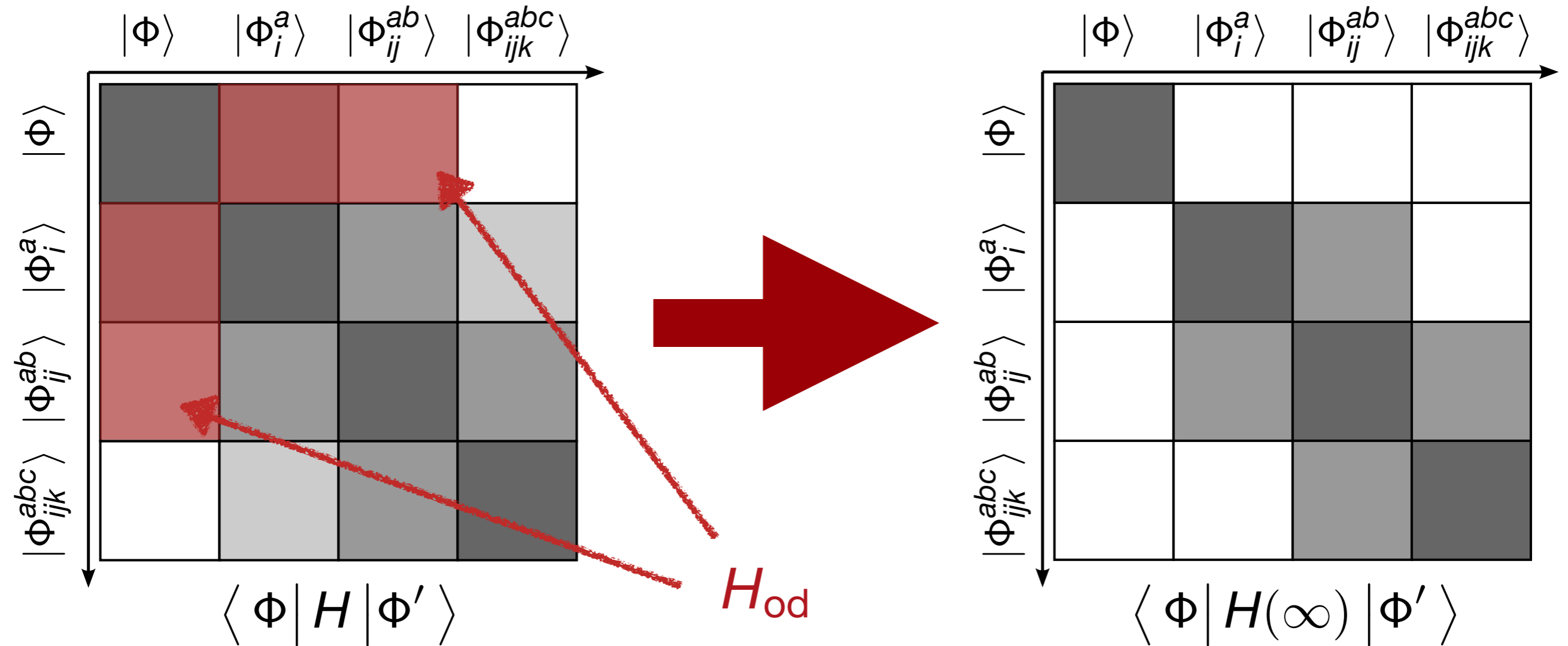
S. K. Bogner, R. J. Furnstahl, and A. Schwenk, Prog. Part. Nucl. Phys. **65**, 94

Decoupling in A-Body Space



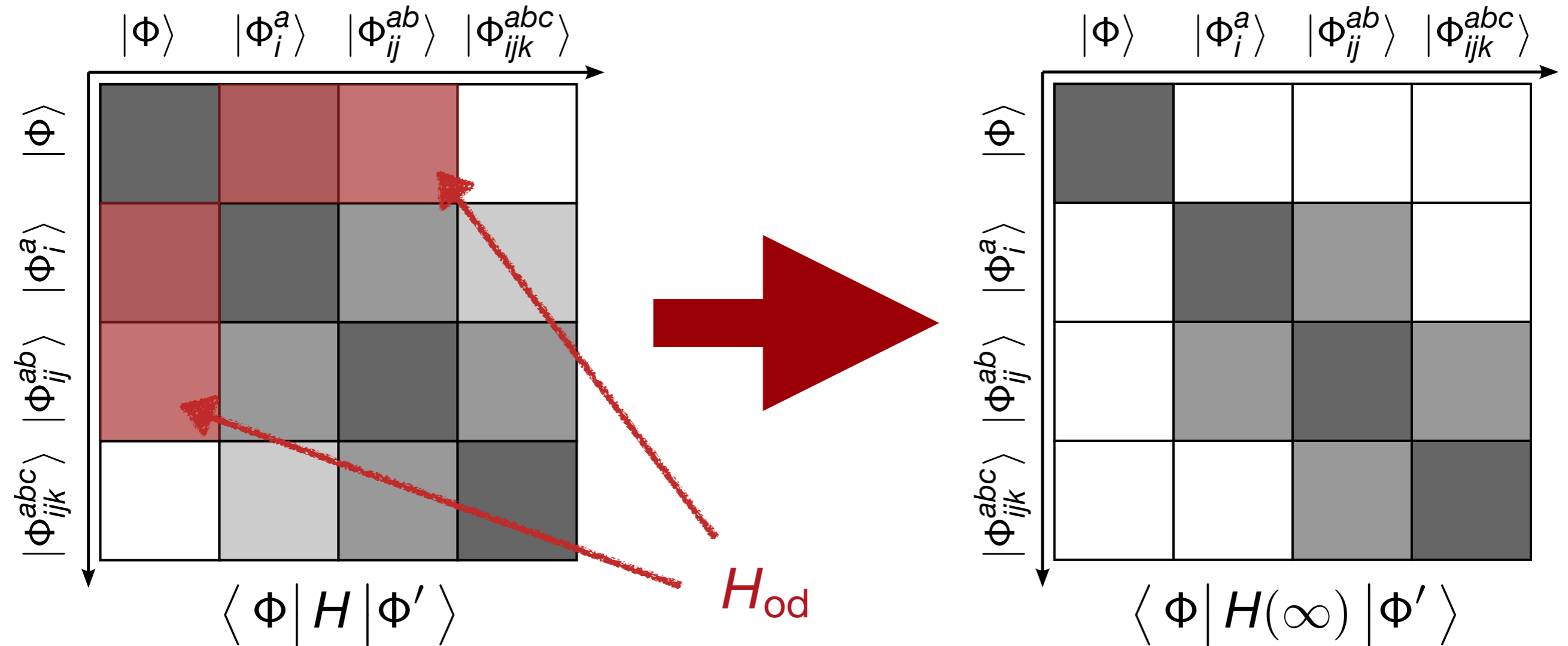
goal: decouple reference state $|\Phi\rangle$
from excitations

Flow Equation



$$\frac{d}{ds} H(s) = [\eta(s), H(s)], \quad \text{e.g.,} \quad \eta(s) \equiv [H_d(s), H_{od}(s)]$$

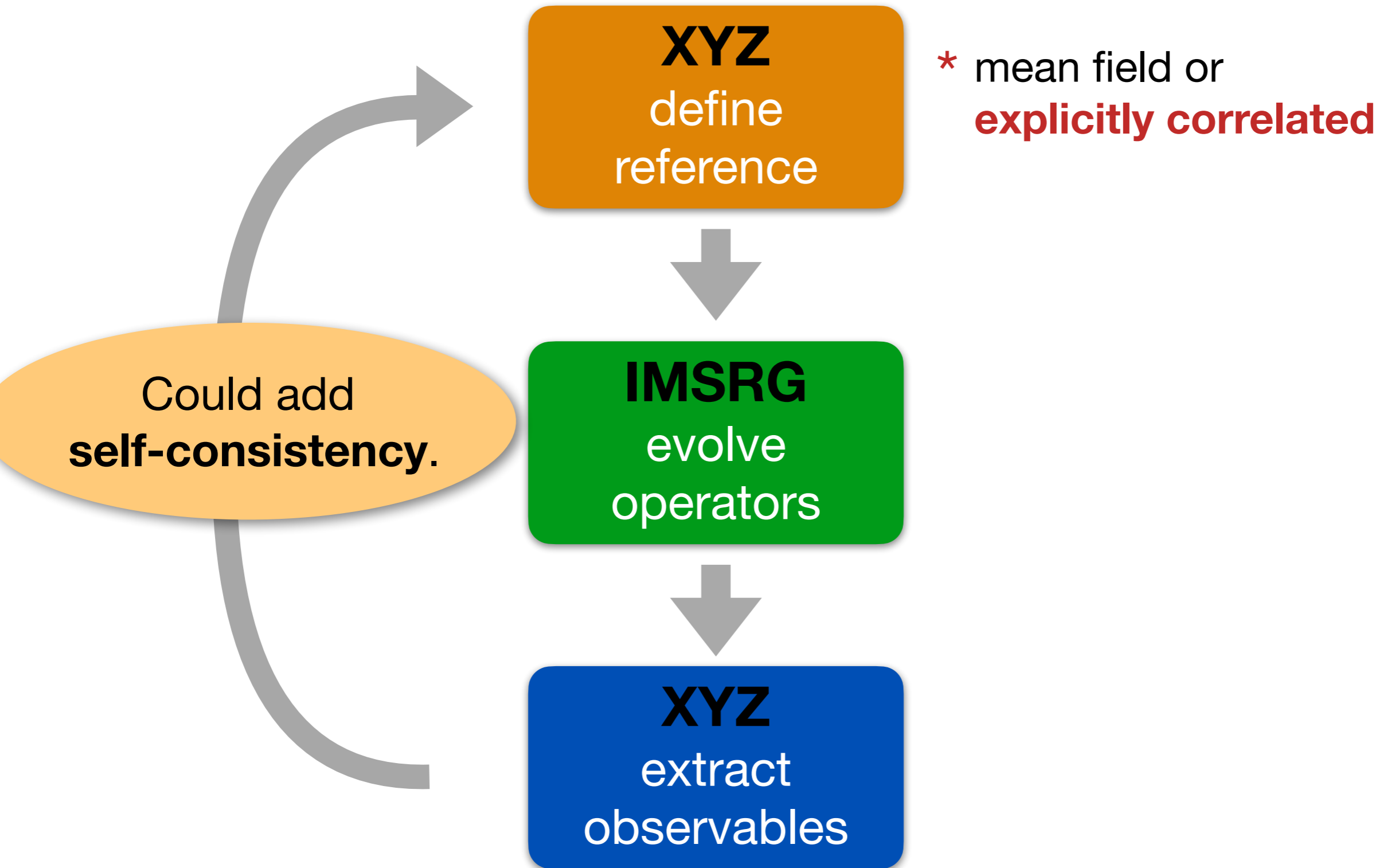
Flow Equation



$$\frac{d}{ds} H(s) = [\eta(s), H(s)],$$

Operators truncated at **two-body level** - matrix is never constructed explicitly!

IMSRG-Improved Methods



IMSRG-Improved Methods



- **IMSRG for closed and open-shell nuclei: IM-HF and IM-PHFB**

- HH, Phys. Scripta, Phys. Scripta 92, 023002 (2017)
- HH, S. K. Bogner, T. D. Morris, A. Schwenk, and K. Tuskuyama, Phys. Rept. 621, 165 (2016)

- **Valence-Space IMSRG (VS-IMSRG)**

- S. R. Stroberg, HH, S. K. Bogner, J. D. Holt, Ann. Rev. Nucl. Part. Sci. 69, 165

- **In-Medium No Core Shell Model (IM-NCSM)**

- E. Gebrerufael, K. Vobig, HH, R. Roth, PRL 118, 152503

- **In-Medium Generator Coordinate Method (IM-GCM)**

- J. M. Yao, J. Engel, L. J. Wang, C. F. Jiao, HH PRC 98, 054311 (2018)
- J. M. Yao et al., PRL 124, 232501 (2020)

XYZ
define
reference

IMSRG
evolve
operators

XYZ
extract
observables

Merging IMSRG and CI: Valence-Space IMSRG

Review:

S. R. Stroberg, HH, S. K. Bogner, and J. D. Holt, *Ann. Rev. Part. Nucl. Sci.* **69**, 165 (2019)

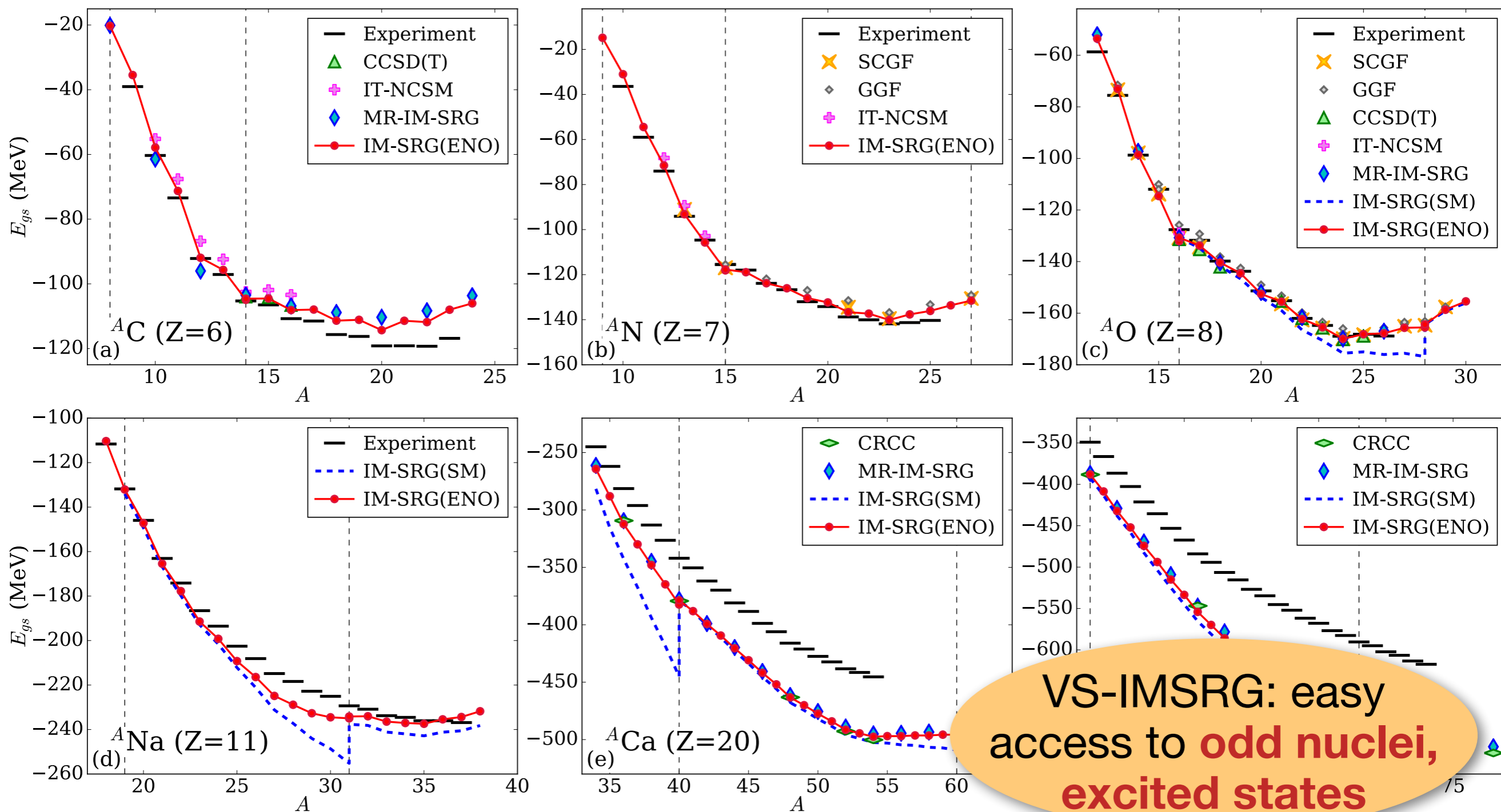
Full CI:

E. Gebrerufael, K. Vobig, HH, and R. Roth, *Phys. Rev. Lett.* **118**, 152503 (2017)

Ground-State Energies



S. R. Stroberg, A. Calci, HH, J. D. Holt, S. K. Bogner, R. Roth, A. Schwenk, *PRL* **118**, 032502 (2017)
 S. R. Stroberg, HH, S. K. Bogner, J. D. Holt, *Ann. Rev. Part. Nucl. Sci.* **69**, 307 (2019)

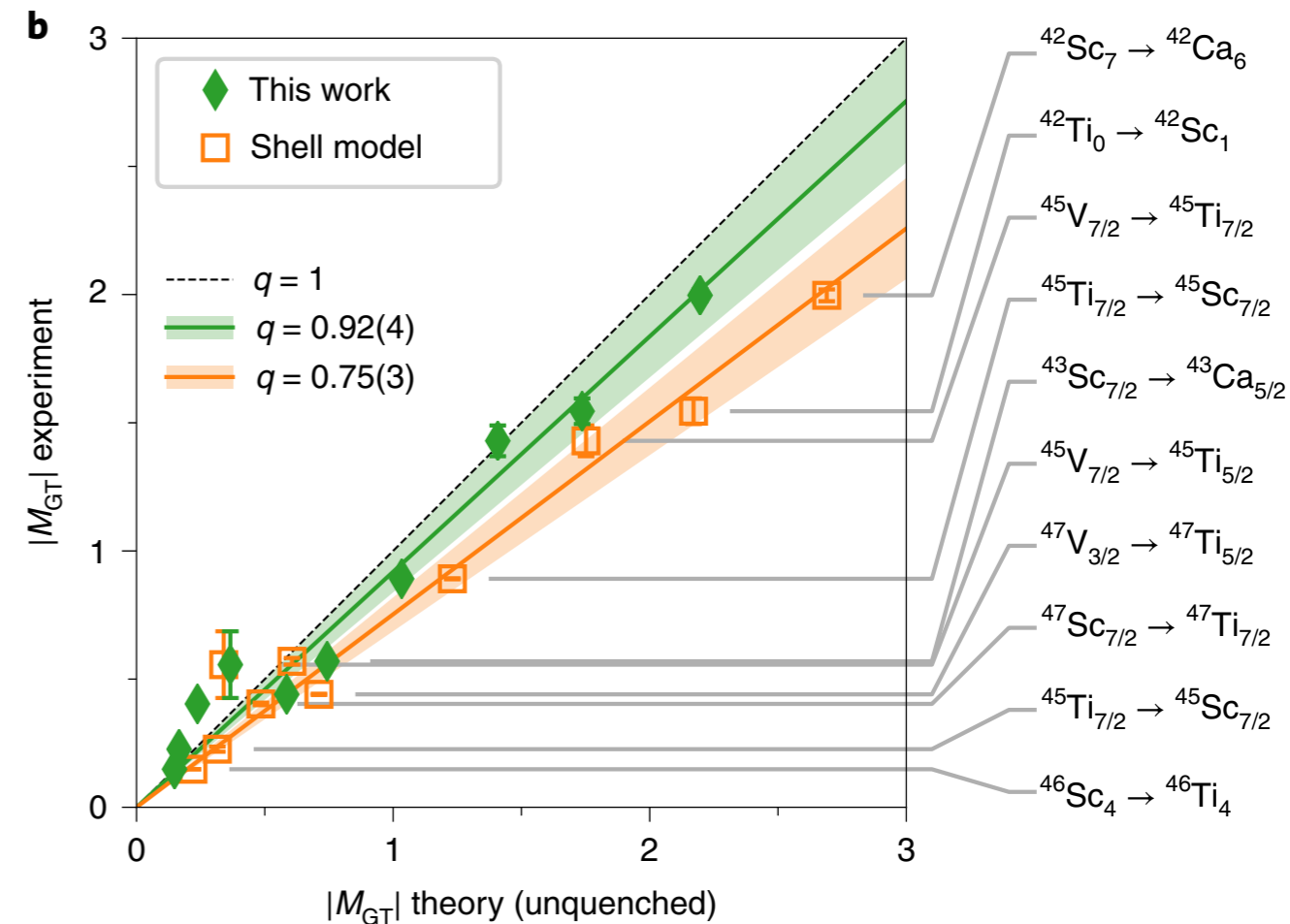
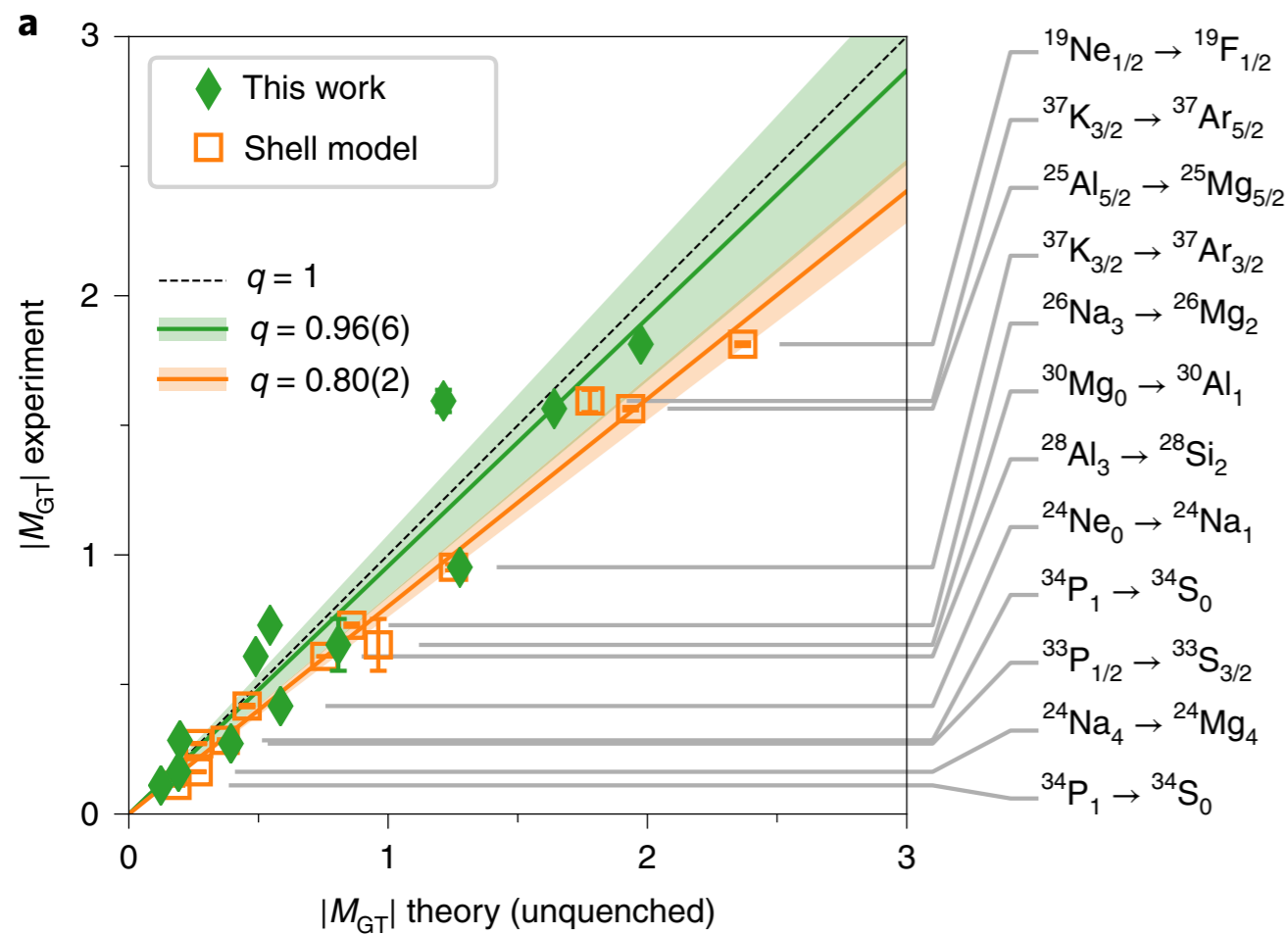


VS-IMSRG: easy access to odd nuclei, excited states

Quenching of Gamow-Teller Decays



P. Gysbers et al., Nature Physics 15, 428 (2019)



- **empirical Shell model** calculations require **quenching factors** of the weak axial-vector coupling g_A
- **VS-IMSRG** explains this through consistent **renormalization** of transition operator, incl. **two-body currents**

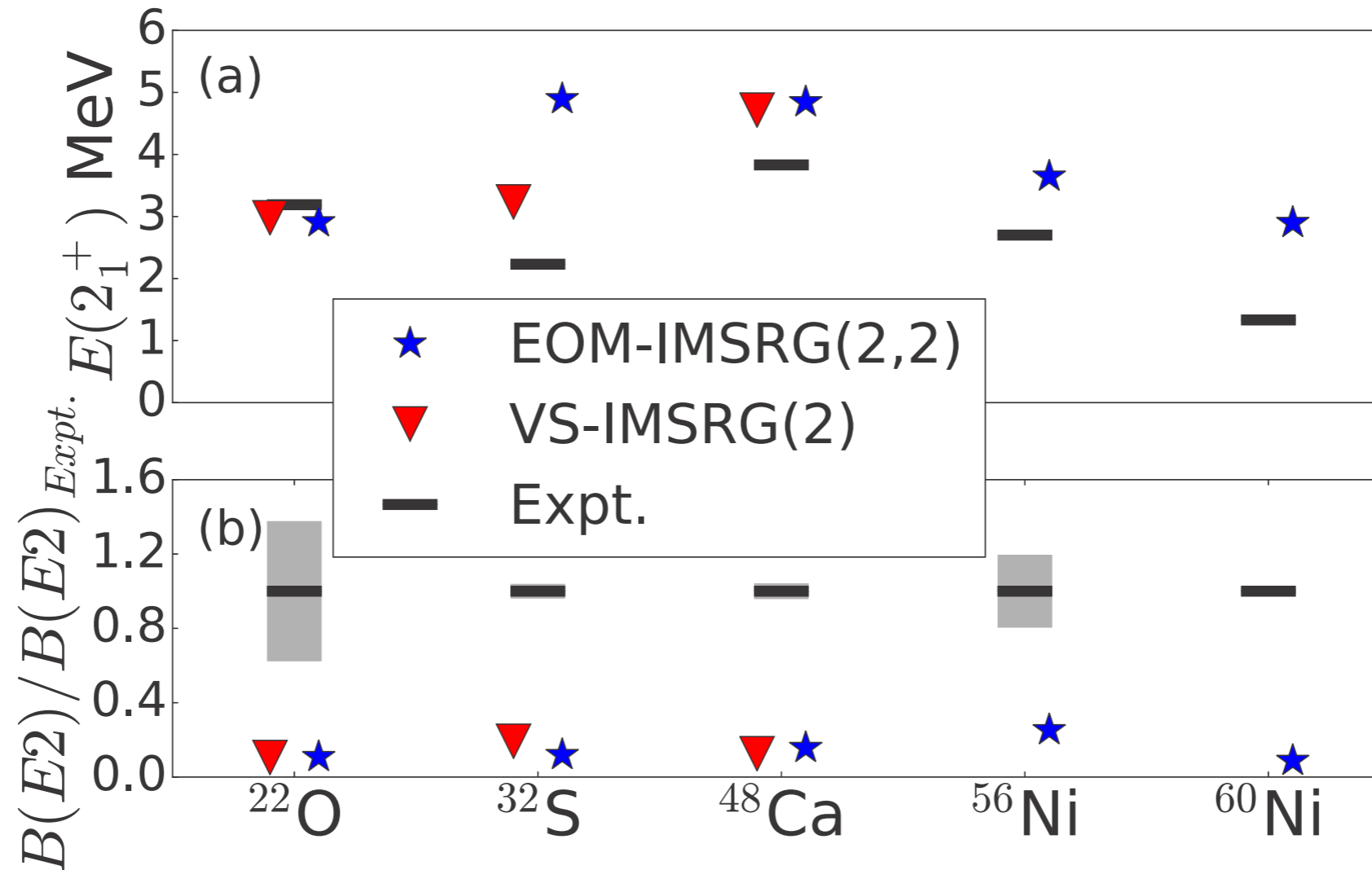
Transitions



N. M. Parzuchowski, S. R. Stroberg et al., *PRC* **96**, 034324

S. R. Stroberg, HH, S. K. Bogner, J. D. Holt, *Ann. Rev. Part. Nucl. Sci.* **69**, 307 (2019)

S. R. Stroberg et al. *PRC* **105**, 034333 (2022)



- **$B(E2)$ much too small:** missing collectivity due to intermediate 3p3h, ... states that are truncated in IMSRG evolution (**static correlation**)

Capturing Collective Correlations: In-Medium Generator Coordinate Method

J. M. Yao, A. Belley, R. Wirth, T. Miyagi, C. G. Payne, S. R. Stroberg, HH, J. D. Holt, PRC **103**, 014315 (2021)

J. M. Yao, B. Bally, J. Engel, R. Wirth, T. R. Rodriguez, HH, PRL **124**, 232501 (2020)

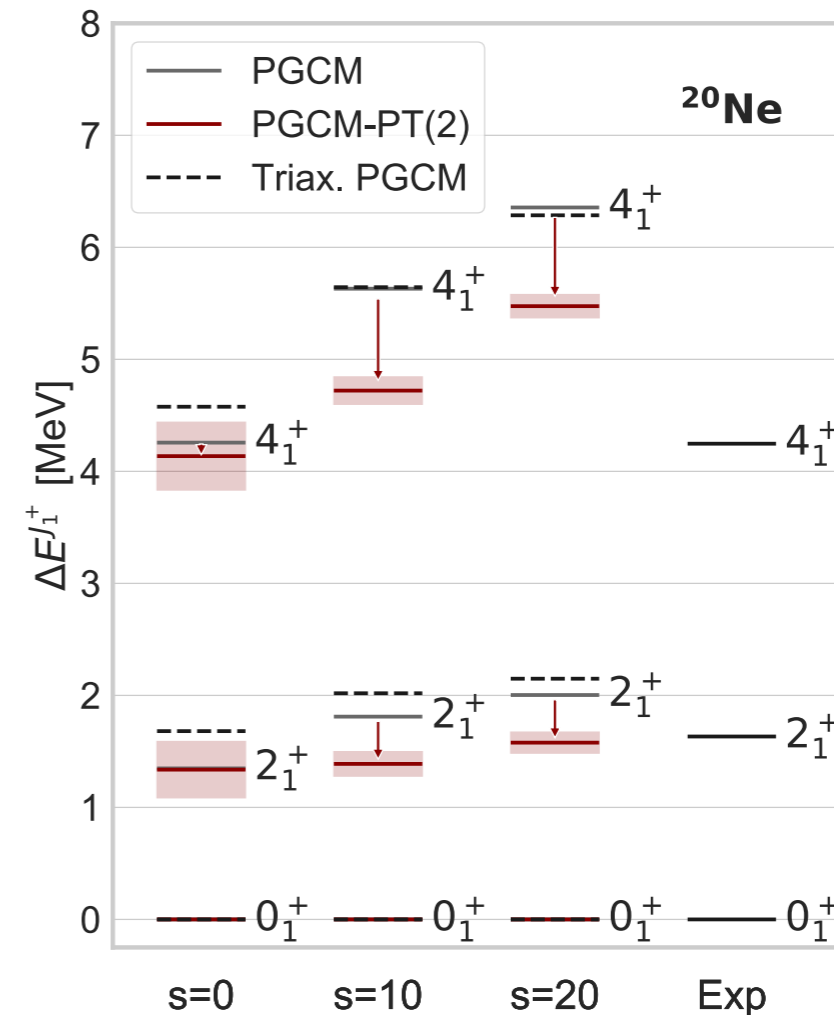
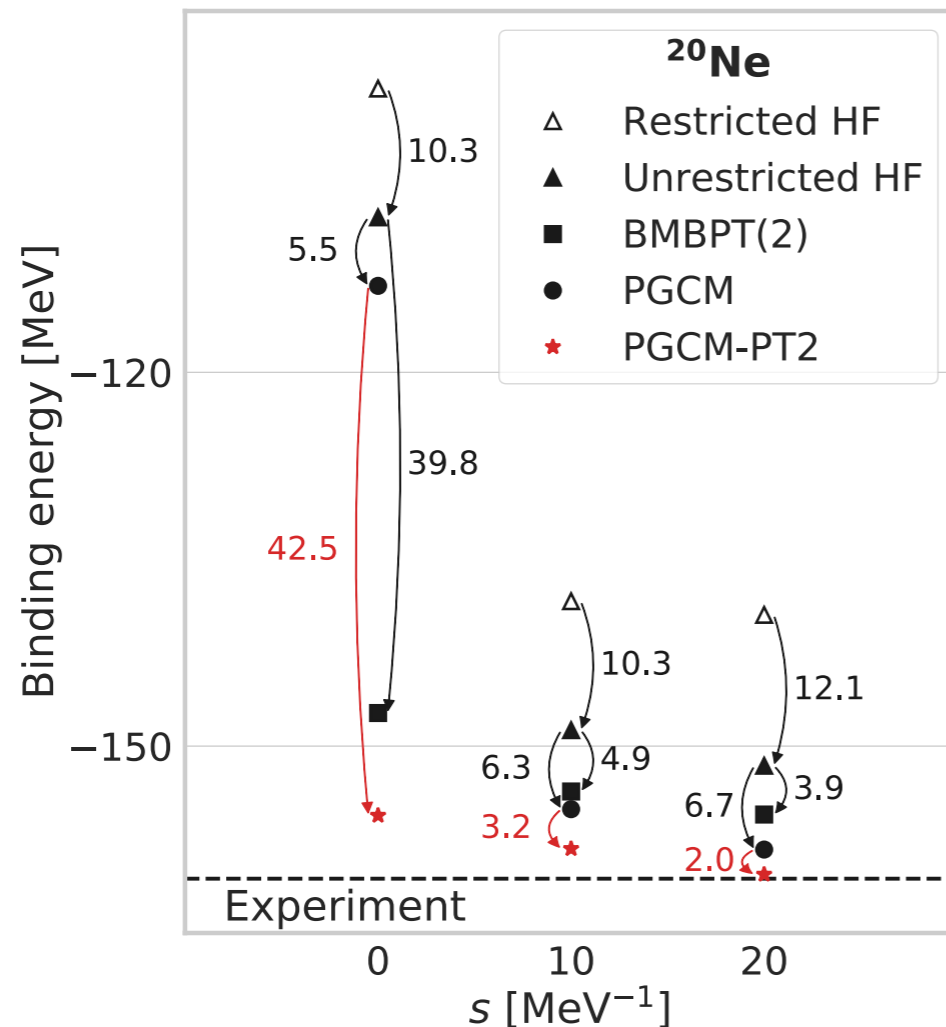
J. M. Yao, J. Engel, L. J. Wang, C. F. Jiao, H. H., PRC **98**, 054311 (2018)

HH, J. M. Yao, T. D. Morris, N. M. Parzuchowski, S. K. Bogner and J. Engel, J. Phys. Conf. Ser. 1041, 012007 (2018)

Perturbative Enhancement of IM-GCM



M. Frosini et al., EPJA 58, 64 (2022)



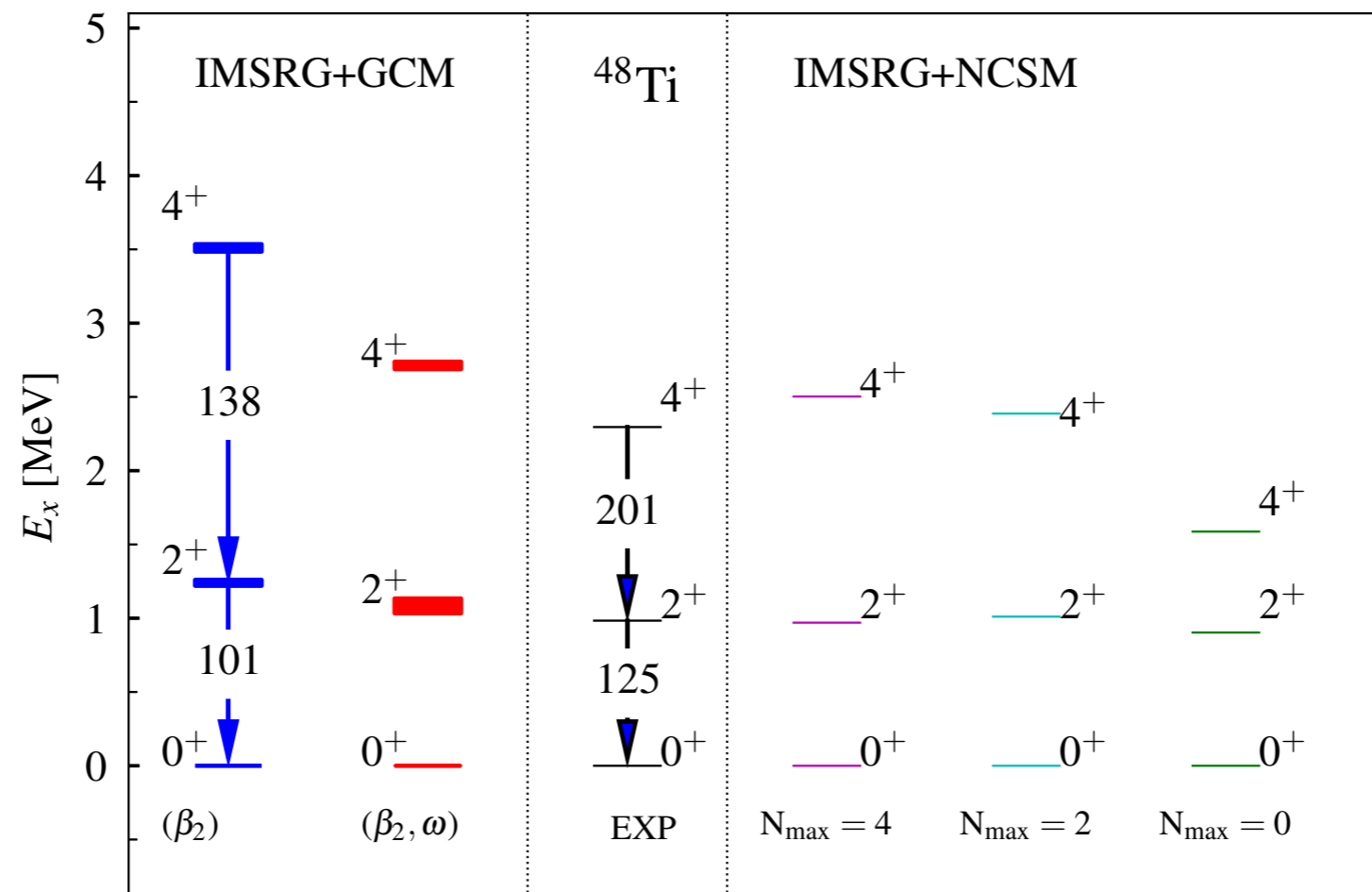
- s-dependence is a **built-in diagnostic tool** for IM-GCM (**not available in phenomenological GCM**)
- if operator and wave function offer sufficient degrees of freedom, evolution of observables is unitary
- need **richer references and/or IMSRG(3)** for certain observables

IM-GCM: $0\nu\beta\beta$ Decay of ^{48}Ca



J. M. Yao et al., PRL **124**, 232501 (2020); *HH, Front. Phys.* **8**, 379 (2020)

EM1.8/2.0, $\hbar\Omega = 16$ MeV

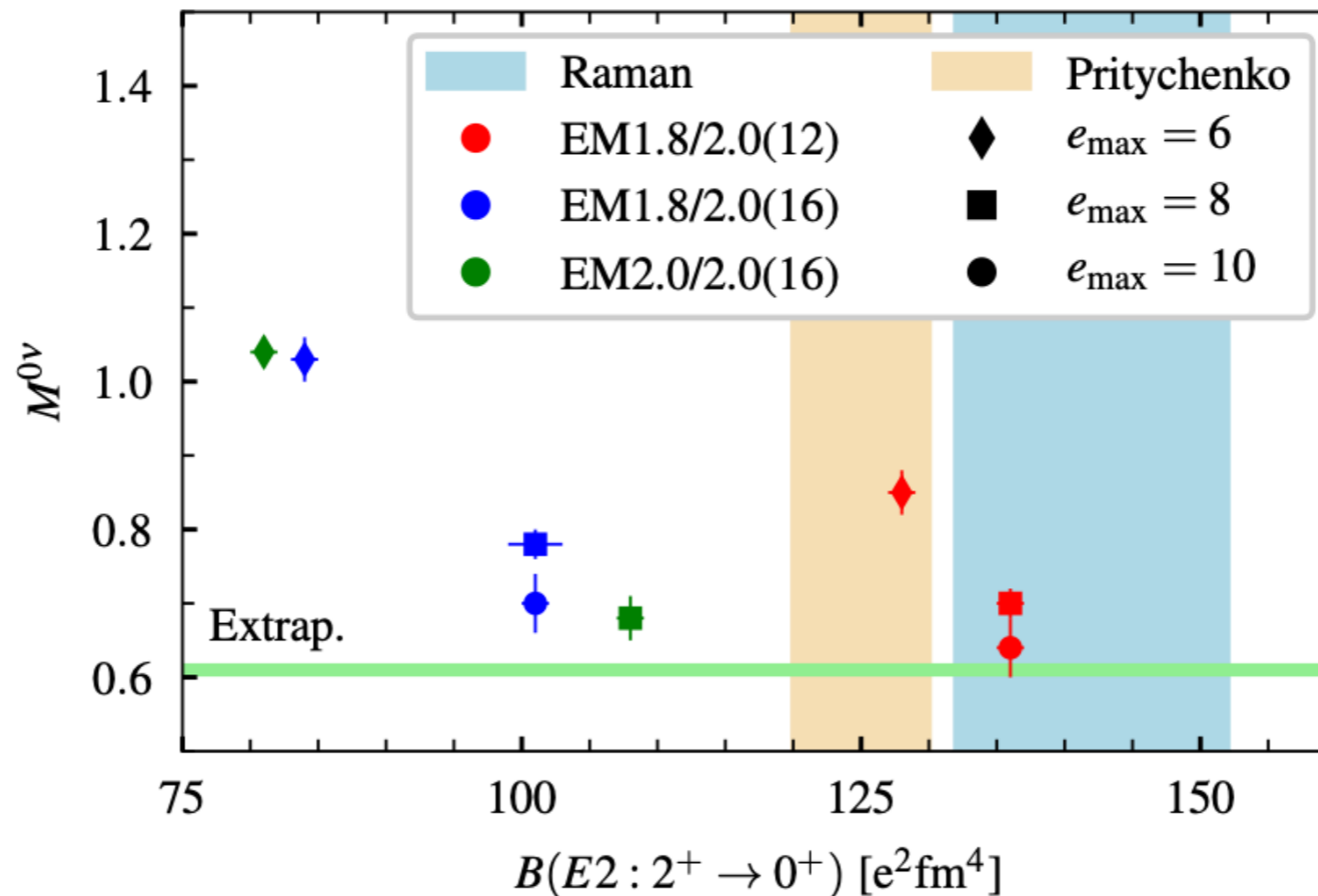


- richer GCM state through **cranking**
- **consistency** between IM-GCM and IM-NCSM

$0\nu\beta\beta$ Decay of ^{48}Ca



J. M. Yao et al., PRL 124, 232501 (2020); PRC 103, 014315 (2021)

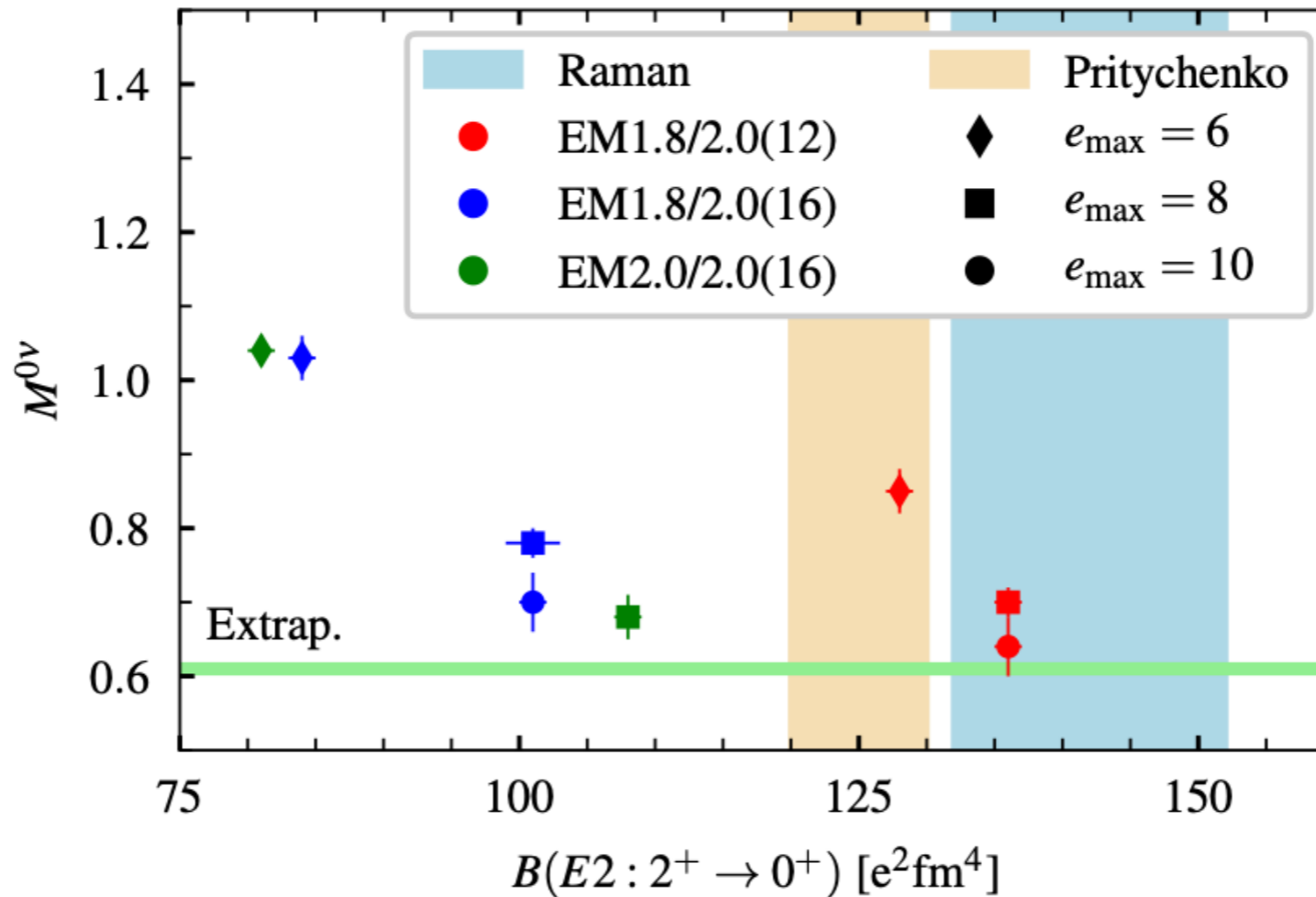


- NME from different methods **consistent** for consistent interactions & transition operators
(A. Belley et al., PRL 126, 042502, S. Novario et al., PRL 126, 182502)
- interpretation and features differ from empirical approaches (e.g., only **weak correlation** between NME and B(E2) value)

$0\nu\beta\beta$ Decay of ^{48}Ca



J. M. Yao et al., PRL 124, 232501 (2020); PRC 103, 014315 (2021)



- NME from different methods **consistent** for consistent interactions & transition operators

(A. Belley et al., PRL 126, 042502, S. Novario et al., PRC 103, 014315 (2021))

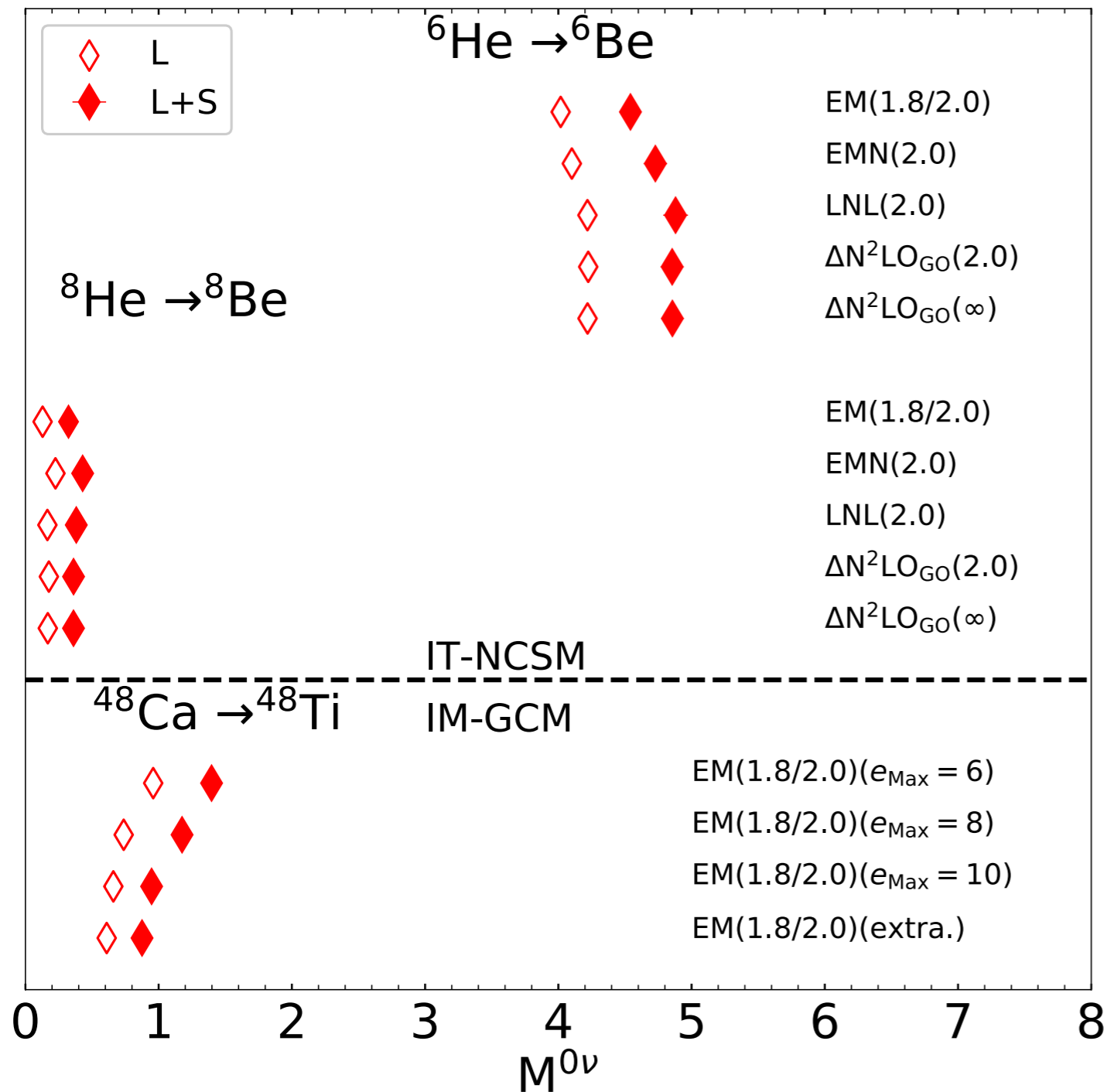
- interpretation and features differ from e.g. ^{48}Ca only **weak correlation** between NME and $B(E2)$

not the full story yet: improve IMSRG truncations, additional GCM correlations, include currents, ...

Counterterm in $0\nu\beta\beta$ Operator



R. Wirth, J. M. Yao, H. Hergert, PRL 127, 242502 (2021)

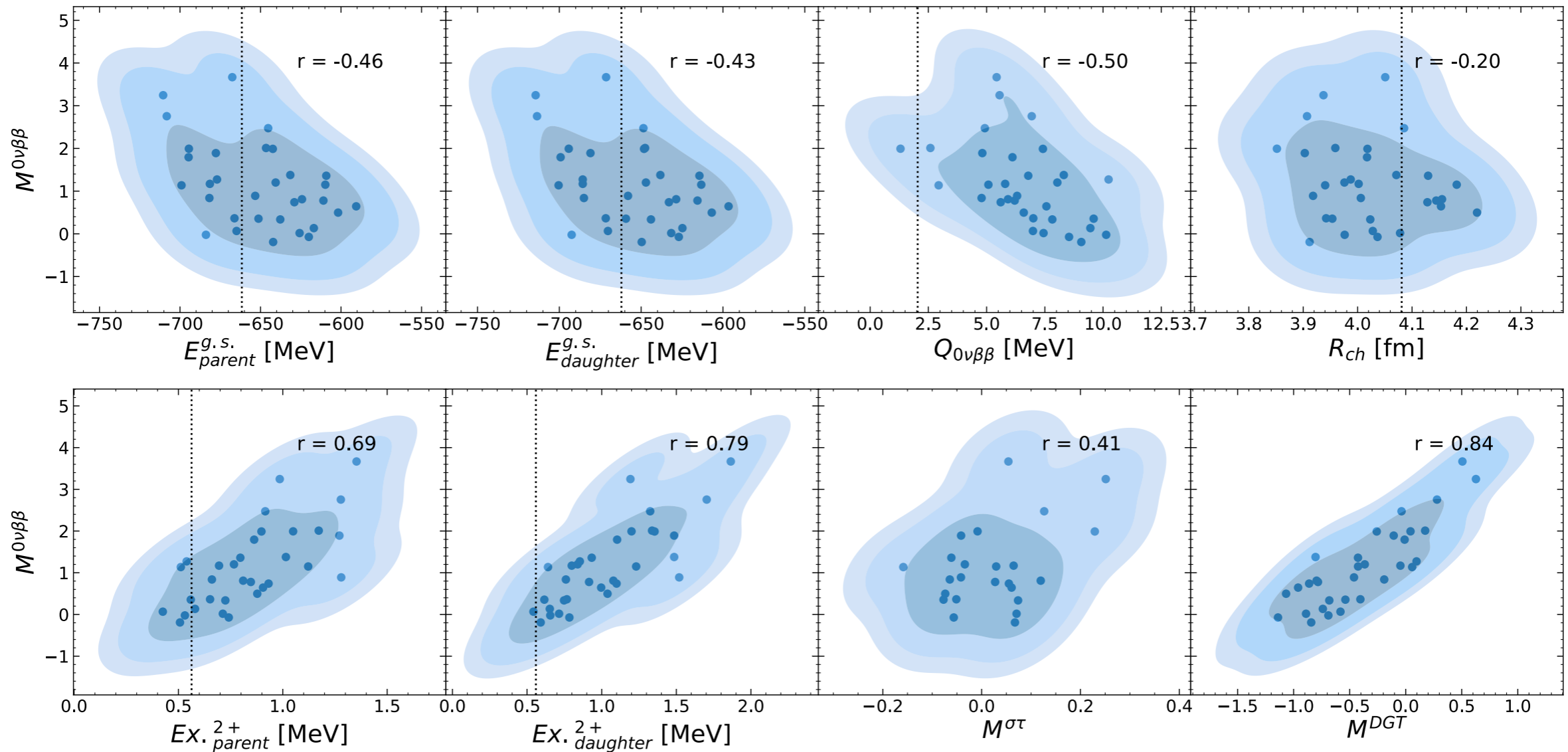


- Cirigliano et al.: RG invariance of the DBD transition operator requires **contact term**
- Counter term yields **robust enhancement**
- varied EFT orders, RG scales, interactions
- **Next:**
 - more interactions
 - inclusion of currents
 - LEC sensitivity / UQ

Correlations Revisited



A. Belley et al., arXiv:2210.05809 [nucl-th]; also see J. M. Yao et al., PRC 106, 014315



^{76}Ge , VS-IMSRG, 34 non-implausible Δ -full N2LO interactions
(cf. B.S. Hu et al., Nature Phys.)

- possible correlation with **Double Gamow Teller** transition, **2^+ energies** (but the latter only in ^{76}Ge)

Looking Ahead

What is Next?



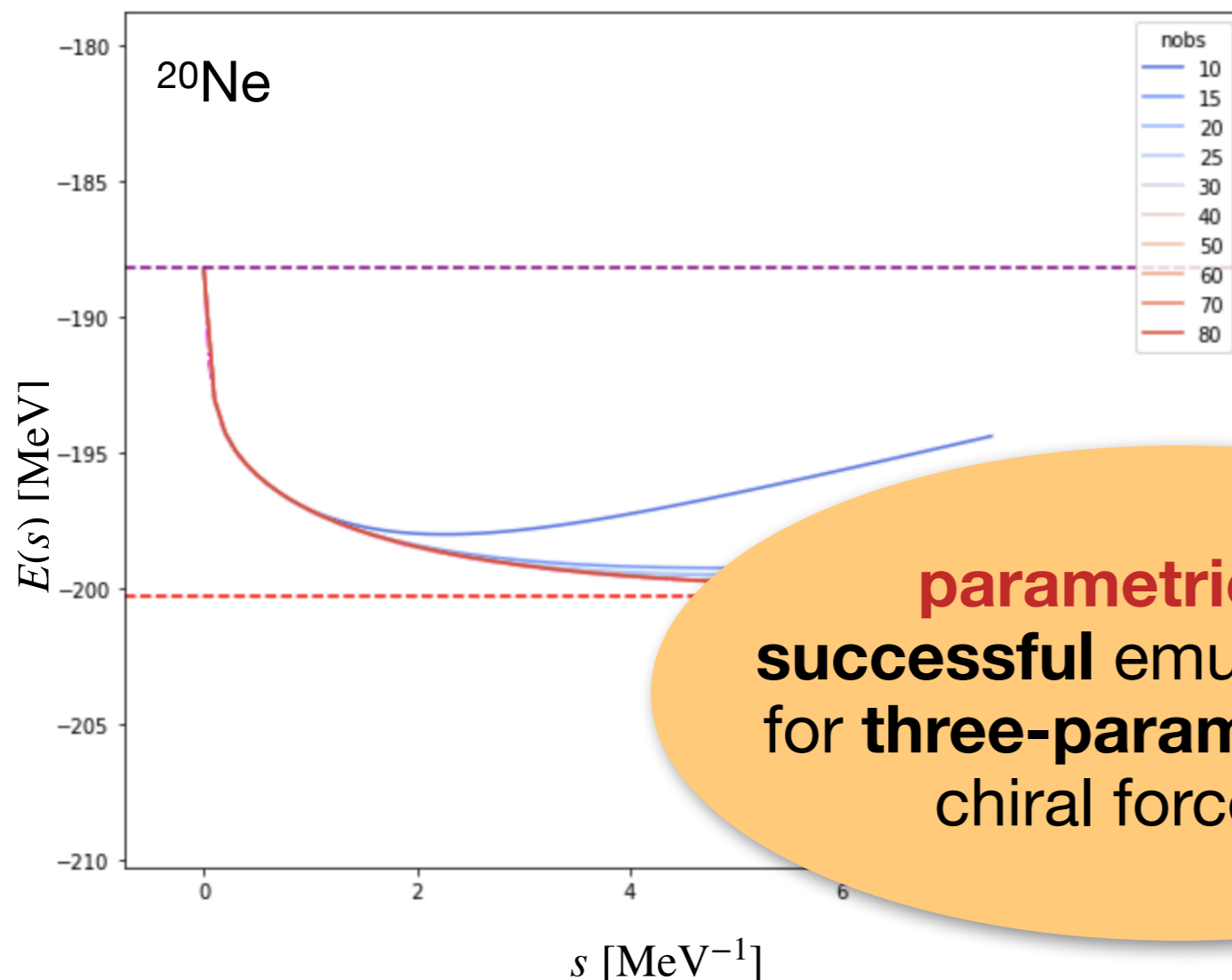
- **Neutrinoless Double Beta Decay** matrix elements for ^{76}Ge and other candidates
 - studies with **multiple complementary methods**: IM-GCM, VS-IMSRG, Coupled Cluster (w/angular momentum projection), ...
 - use VS-IMSRG for heavy lifting in parameter sensitivity analysis & UQ because IM-GCM is too costly
 - **accelerate IMSRG & IM-GCM** (GPUs, factorization, Machine Learning, ...)
[A. M. Romero et al., PRC 104, 054317; J. M. Yao et al., arXiv:2211.02797]
- **Uncertainty Quantification / Sensitivity Analysis**
 - need cheap **surrogate models (emulators)**

Emulating IMSRG Flows



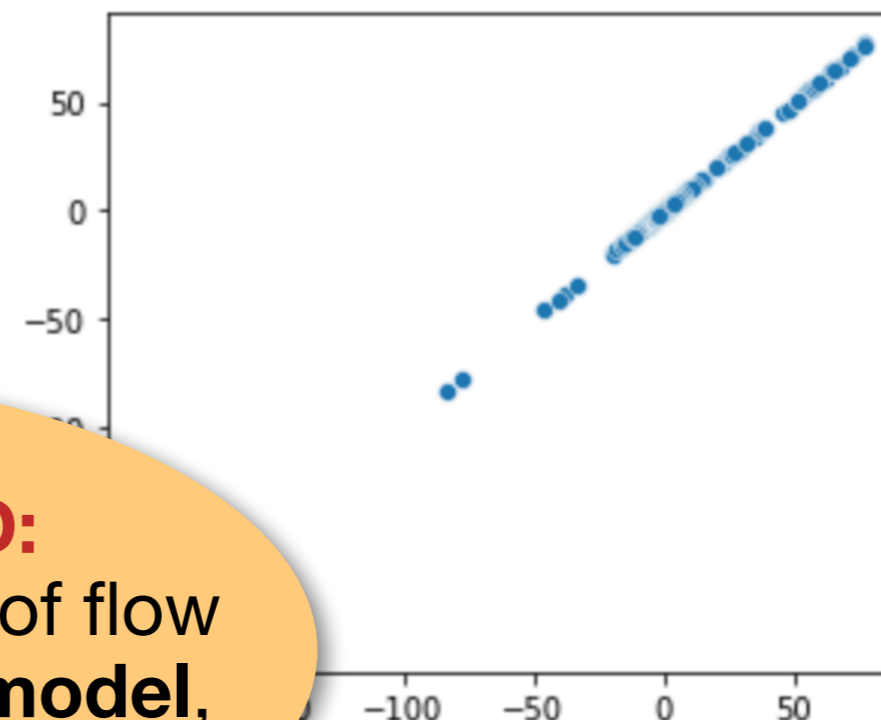
J. Davison, J. Crawford, S. Bogner, HH, in preparation

EM(500) N³LO, $\lambda = 2.0 \text{ fm}^{-1}$



$H_{\text{DMD}}(s)$ vs. $H_{\text{IMSRG}}(s)$

$s = 5.25$



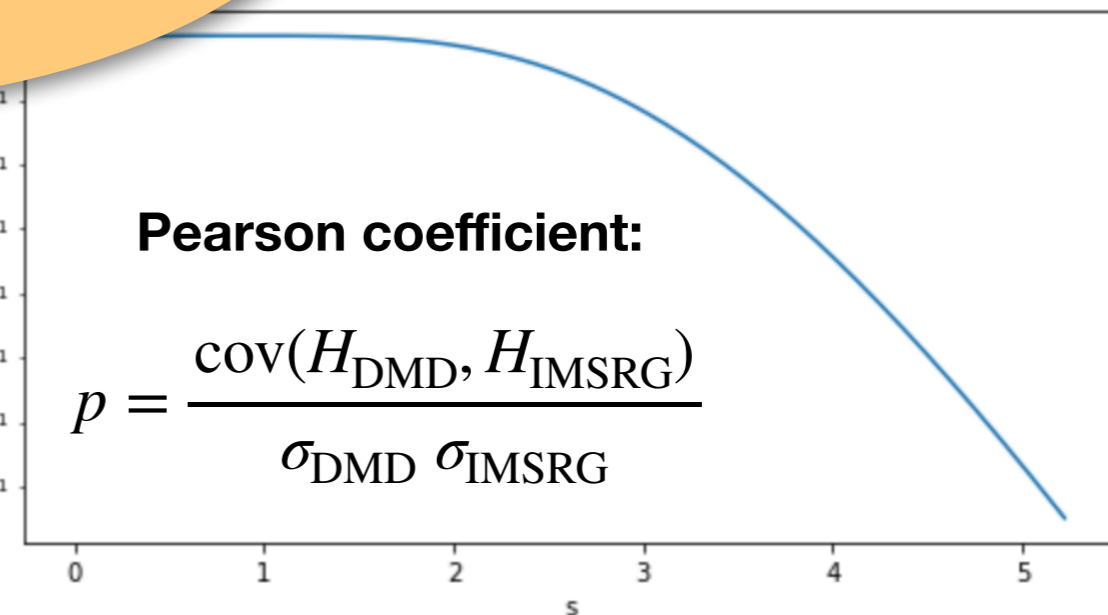
parametric DMD:
successful emulation of flow
 for **three-parameter model**,
 chiral forces next

Dynamic Mode Decomposition
emulator “learns” **all flowing**
operator coefficients from
 snapshots!

correlation
 9.9999×10^{-1}
 9.9998×10^{-1}
 9.9997×10^{-1}
 9.9996×10^{-1}
 9.9995×10^{-1}
 9.9994×10^{-1}
 9.9993×10^{-1}

Pearson coefficient:

$$p = \frac{\text{COV}(H_{\text{DMD}}, H_{\text{IMSRG}})}{\sigma_{\text{DMD}} \sigma_{\text{IMSRG}}}$$



Additional Opportunities



- use wave functions to explore **other NLDBD mechanisms** or other transitions
- (provided the **same scale and scheme** is used as for the Hamiltonian)
- towards **precise beta decays & Schiff moments**
 - develop IM-GCM for **odd nuclei**
 - tackle nuclei for which **large multi-shell valence-spaces** make VS-IMSRG difficult or prohibitive
- **(sensitive) feedback on EFTs**

Some References



Toward the discovery of matter creation with neutrinoless double-beta decay

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(Dated: November 11, 2022)

The discovery of neutrinoless double-beta decay could soon be within reach. This hypothetical ultra-rare nuclear decay offers a privileged portal to physics beyond the Standard Model of particle physics. Its observation would constitute the discovery of a matter-creating process, corroborating leading theories of why the universe contains more matter than antimatter, and how forces unify at high energy scales. It would also prove that neutrinos and anti-neutrinos are not two distinct particles, but can transform into each other, with their mass described by a unique mechanism conceived by Majorana. The recognition that neutrinos are not massless necessitates an explanation and has boosted interest in neutrinoless double-beta decay. The field stands now at a turning point. A new round of experiments is currently being prepared for the next decade to cover an important region of parameter space. In parallel, advances in nuclear theory are laying the groundwork to connect the nuclear decay with the underlying new physics. Meanwhile, the particle theory landscape continues to find new motivations for neutrinos to be their own antiparticle. This review brings together the experimental, nuclear theory, and particle theory aspects connected to neutrinoless double-beta decay, to explore the path toward — and beyond — its discovery.

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Neutrinoless Double-Beta Decay: A Roadmap for Matching Theory to Experiment

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Towards Precise and Accurate Calculations of Neutrinoless Double-Beta Decay: Project Scoping Workshop Report

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arXiv:2202.01787

arXiv:2203.12169

arXiv:2207.01085

[plus J. de Vries, HH, E. Mereghetti, S. Pastore, in prep.]

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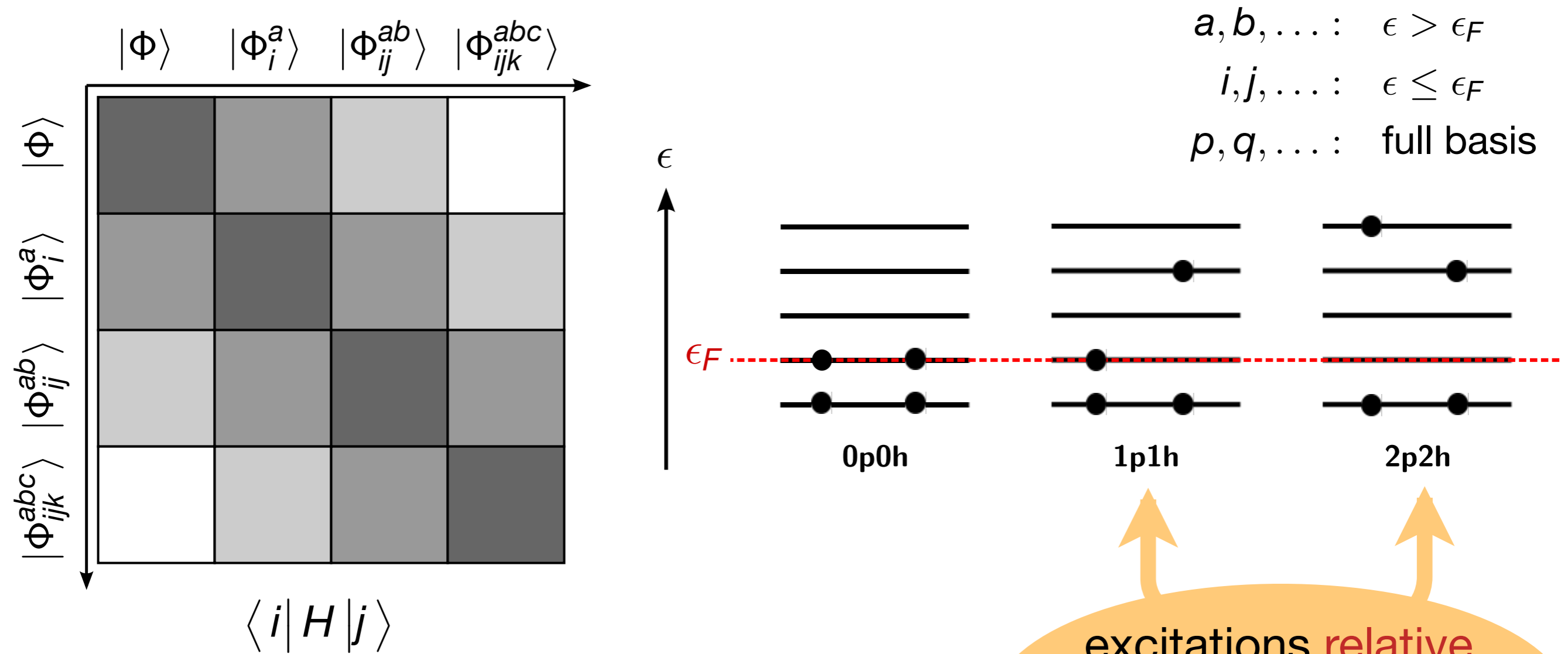
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Grants: US Dept. of Energy, Office of Science, Office of Nuclear Physics **DE-SC0017887** and **DE-SC0018083**
(SciDAC-4 NUCLEI Collaboration)



Supplements

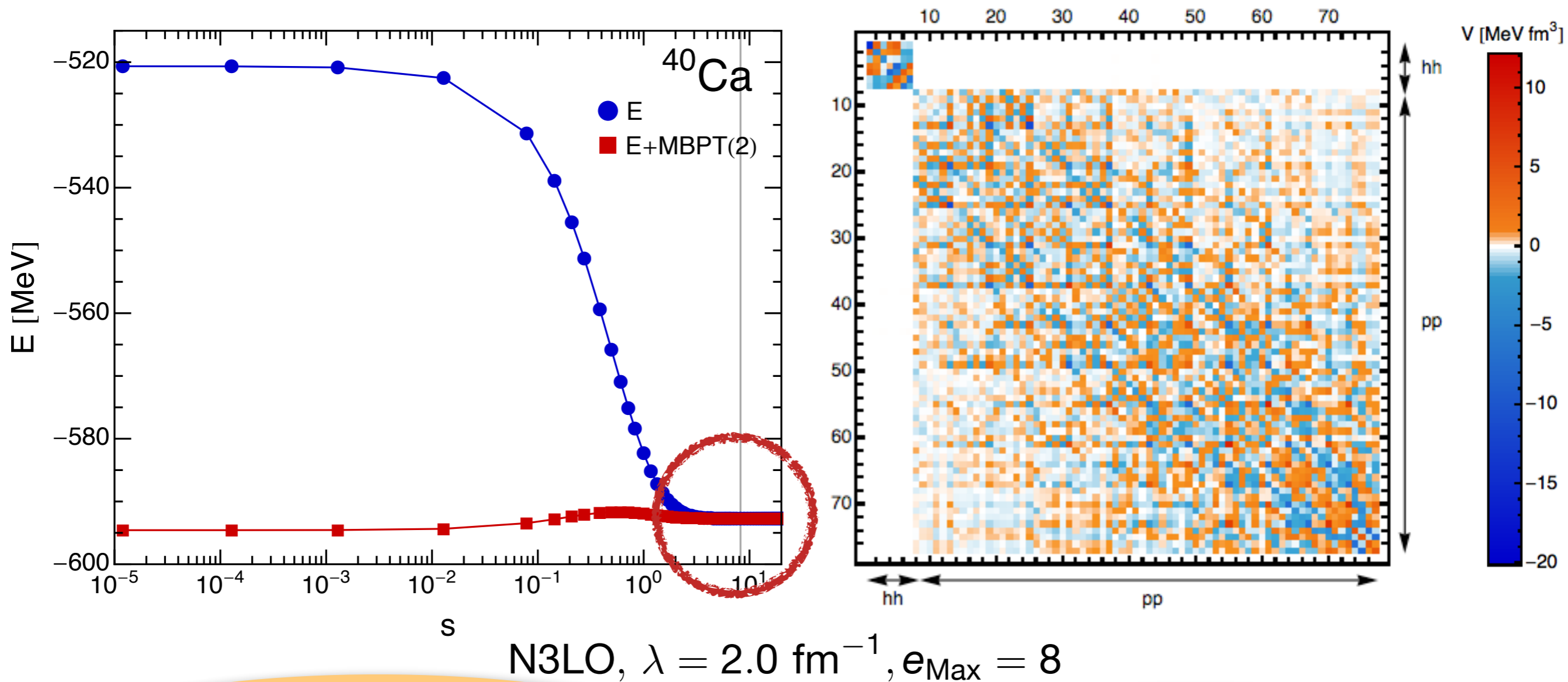
Transforming the Hamiltonian



excitations **relative** to reference state: **normal-ordering**

- reference state: **single Slater determinant**

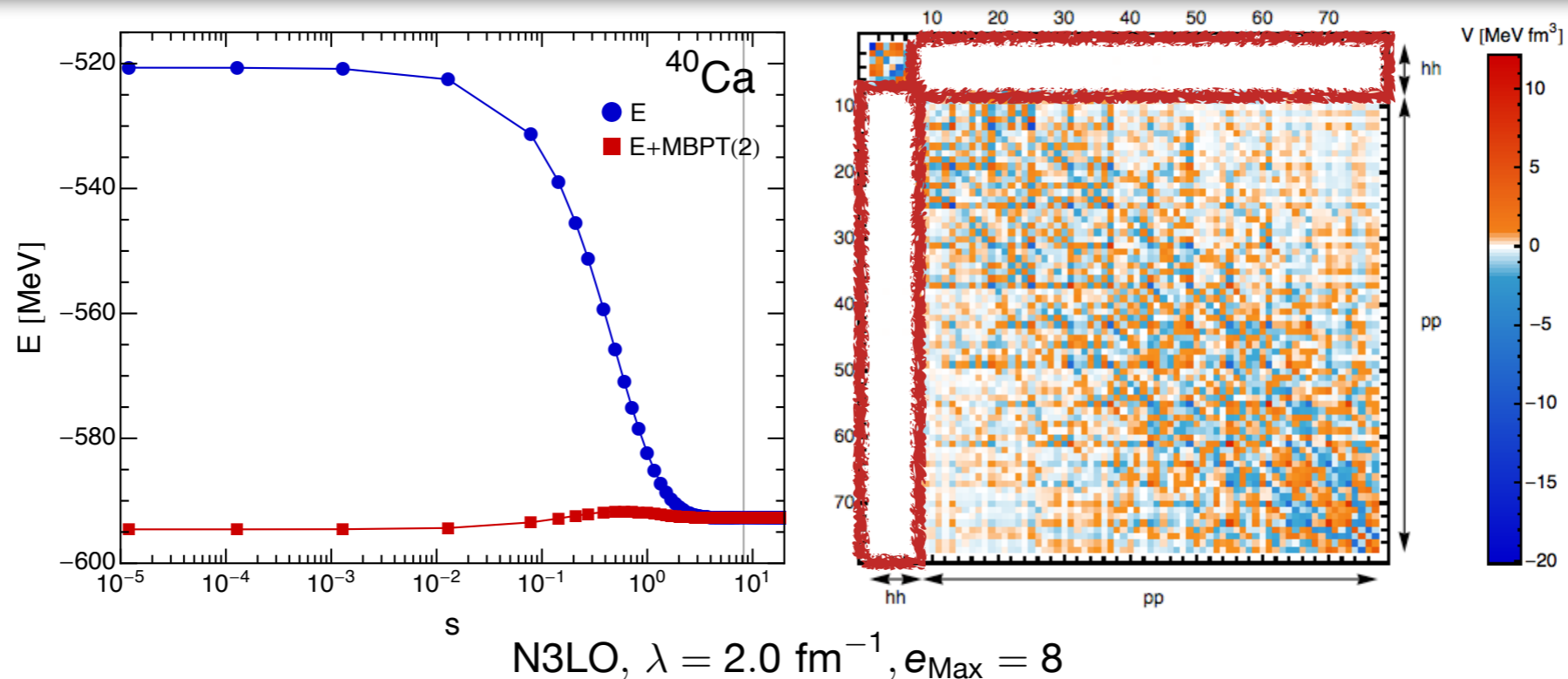
Decoupling



non-perturbative
resummation of MBPT series
(**correlations**)

off-diagonal couplings
are rapidly driven to zero

Decoupling



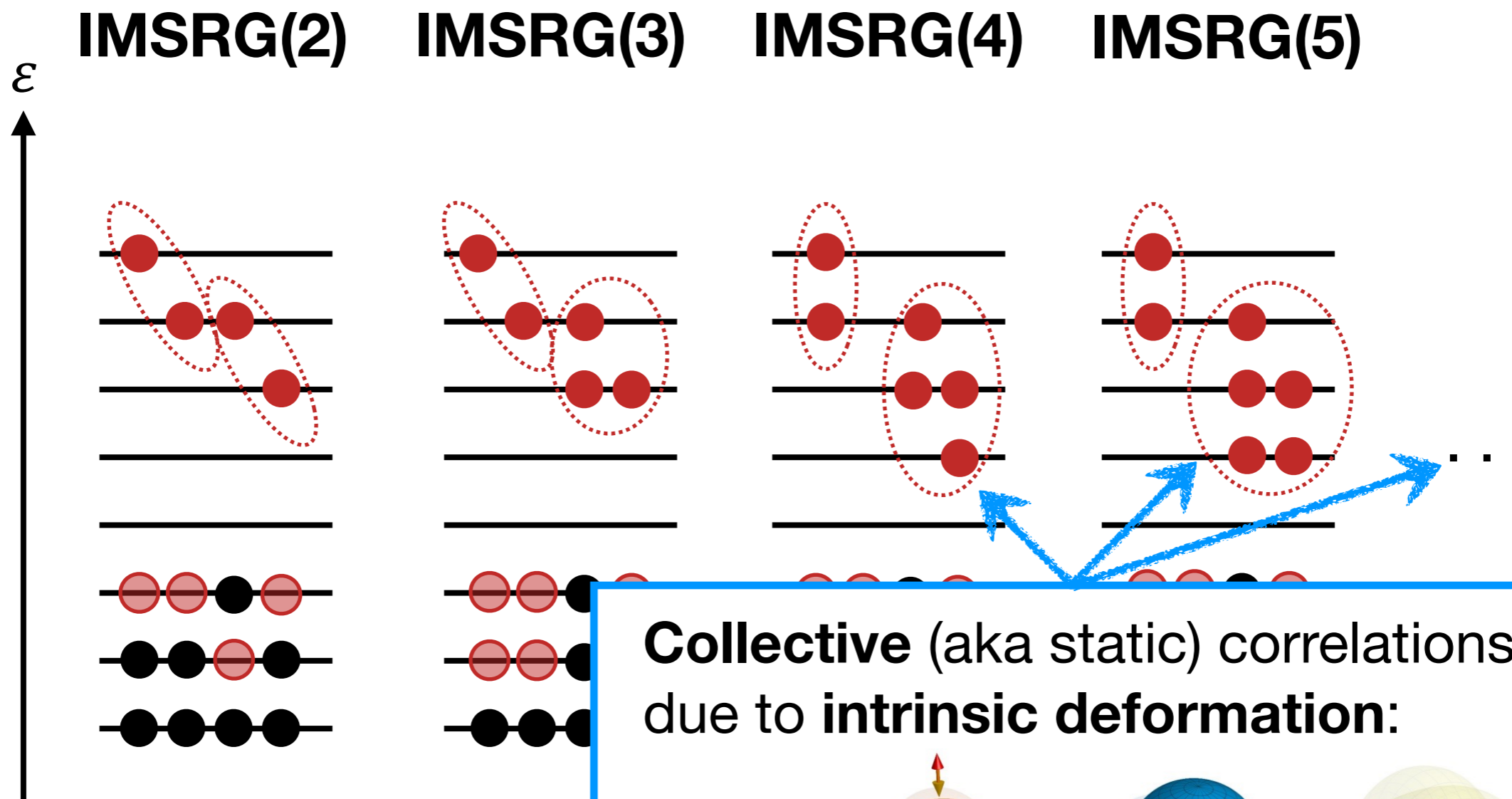
- absorb correlations into **RG-improved Hamiltonian**

$$U(s) H U^\dagger(s) U(s) |\Psi_n\rangle = E_n U(s) |\Psi_n\rangle$$

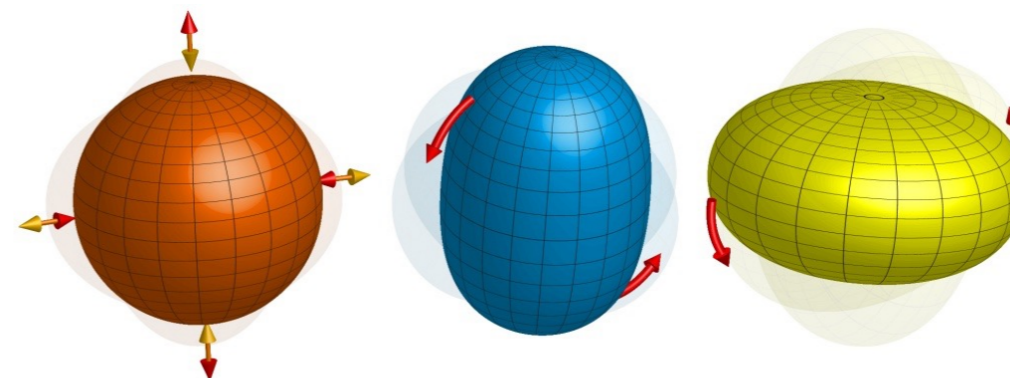
- reference state is ansatz for transformed, **less correlated** eigenstate:

$$U(s) |\Psi_n\rangle \stackrel{!}{=} |\Phi\rangle$$

Correlated Reference States

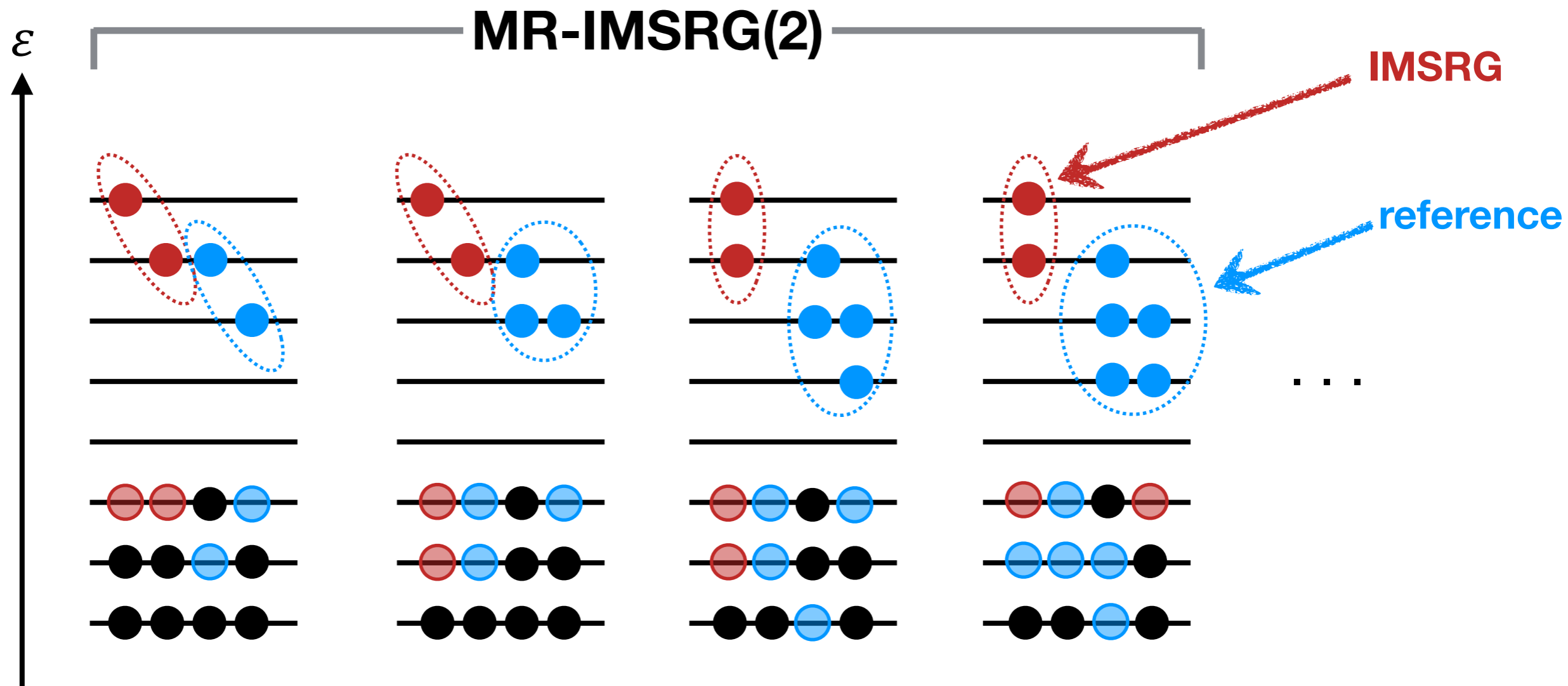


Collective (aka static) correlations, e.g. due to **intrinsic deformation**:



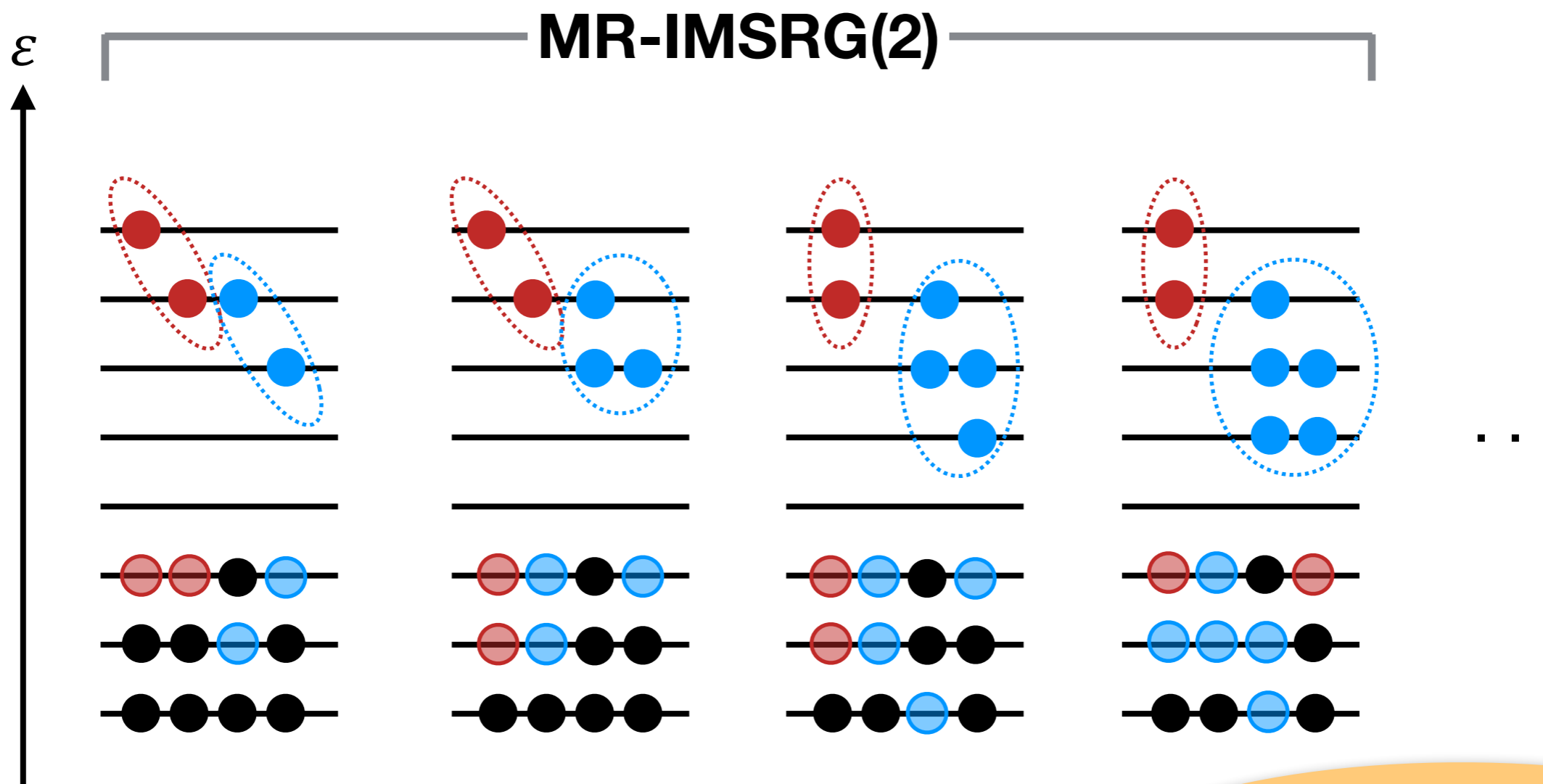
“standard” IMS
Slater determinan

Correlated Reference States



MR-IMSRG: build correlations on top of **already correlated** state (e.g., from a method that describes static correlation well)

Correlated Reference States



MR-IMSRG: build correlations
already correlated state (e.g., from
 describes static correlation

**use generalized
 normal ordering with
 2B,... densities**