
Bayesian methods for extrapolations to stellar energies

Daniel Phillips
Ohio University



OHIO
UNIVERSITY

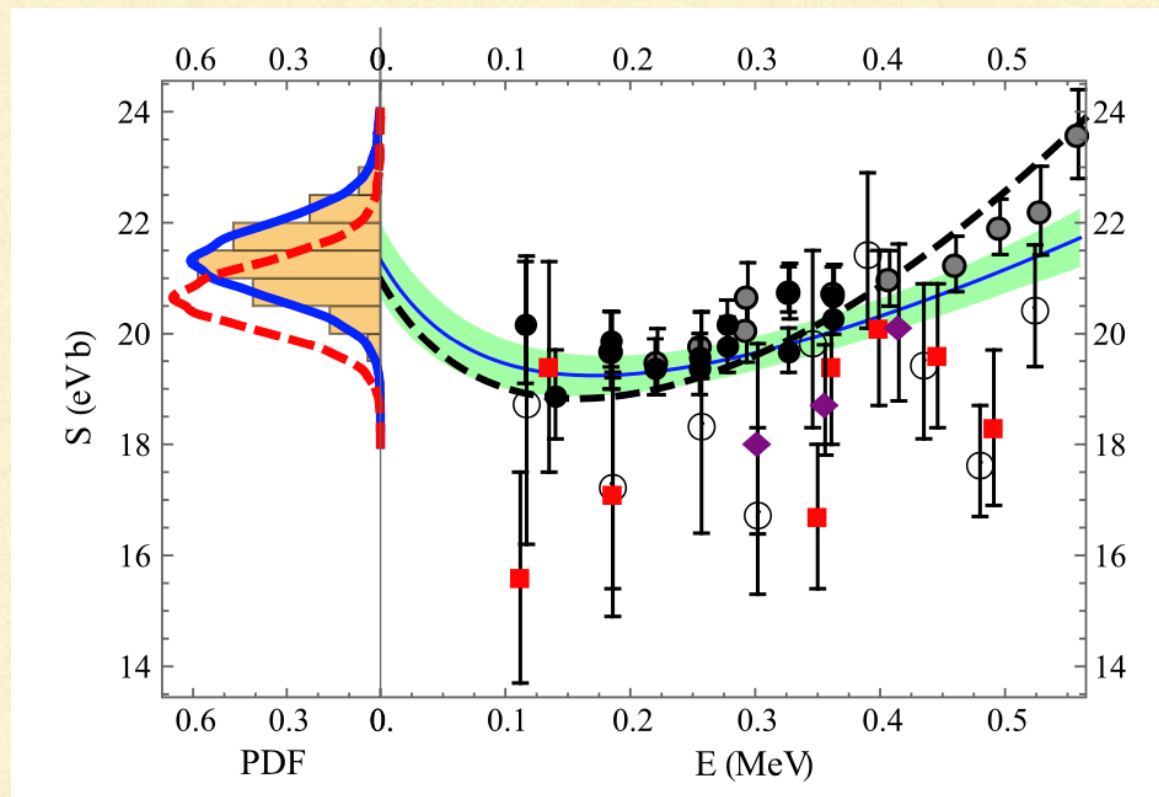
**RESEARCH FUNDED BY THE DOE OFFICE OF SCIENCE, NUCLEAR PHYSICS, THE
NSF OFFICE OF ADVANCED CYBERINFRASTRUCTURE AND THE NATIONAL
NUCLEAR SECURITY ADMINISTRATION**

Since the 2015 Long-Range Plan

- Several forefront analyses of solar-fusion cross sections adopted a Bayesian approach to the extrapolation of experimental data to solar energies
 - Done with EFT; R-matrix; polynomial; ab initio parameterizations of $S(E)$
 - Permits: discovery of non-gaussian (including multi-modal) solutions for parameters; straightforward propagation of parameter uncertainty to predicted quantities; modeling of systematic experimental uncertainties
-

Since the 2015 Long-Range Plan

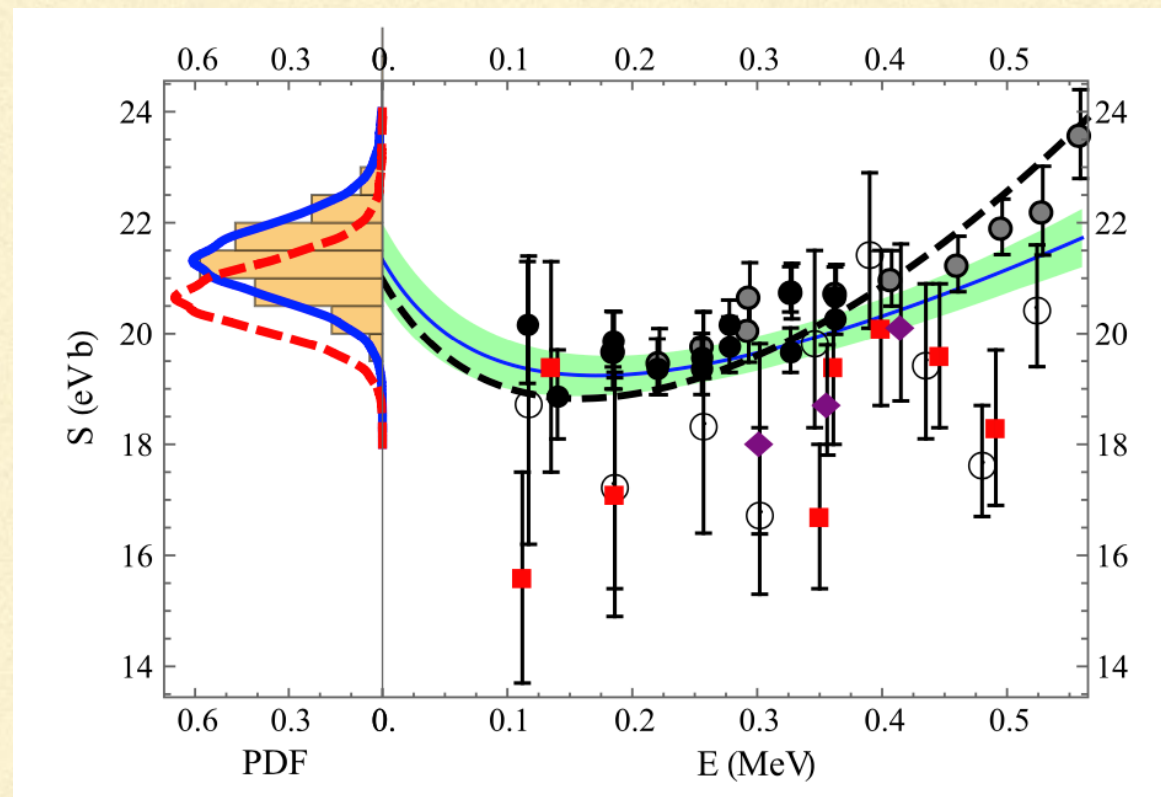
- Several forefront analyses of solar-fusion cross sections adopted a Bayesian approach to the extrapolation of experimental data to solar energies
- Done with EFT; R-matrix; polynomial; ab initio parameterizations of $S(E)$
- Permits: discovery of non-gaussian (including multi-modal) solutions for parameters; straightforward propagation of parameter uncertainty to predicted quantities; modeling of systematic experimental uncertainties



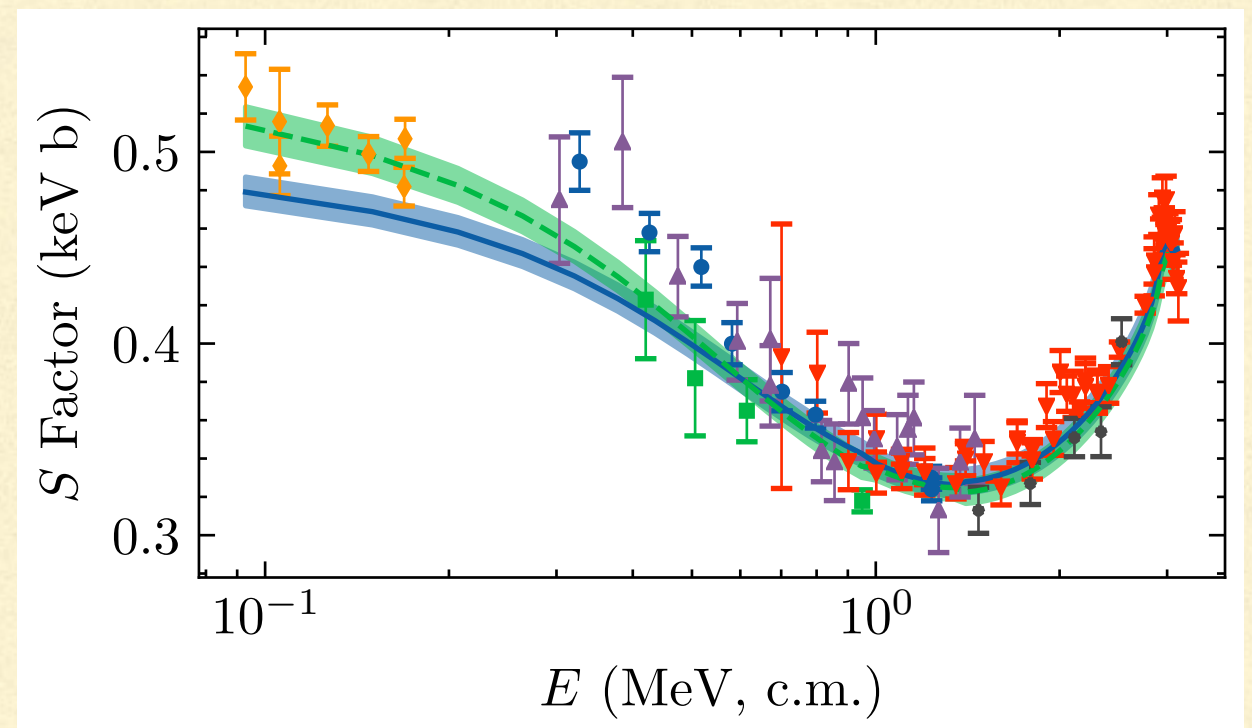
Zhang et al., PLB 751, 535 (2015)

Since the 2015 Long-Range Plan

- Several forefront analyses of solar-fusion cross sections adopted a Bayesian approach to the extrapolation of experimental data to solar energies
- Done with EFT; R-matrix; polynomial; ab initio parameterizations of $S(E)$
- Permits: discovery of non-gaussian (including multi-modal) solutions for parameters; straightforward propagation of parameter uncertainty to predicted quantities; modeling of systematic experimental uncertainties



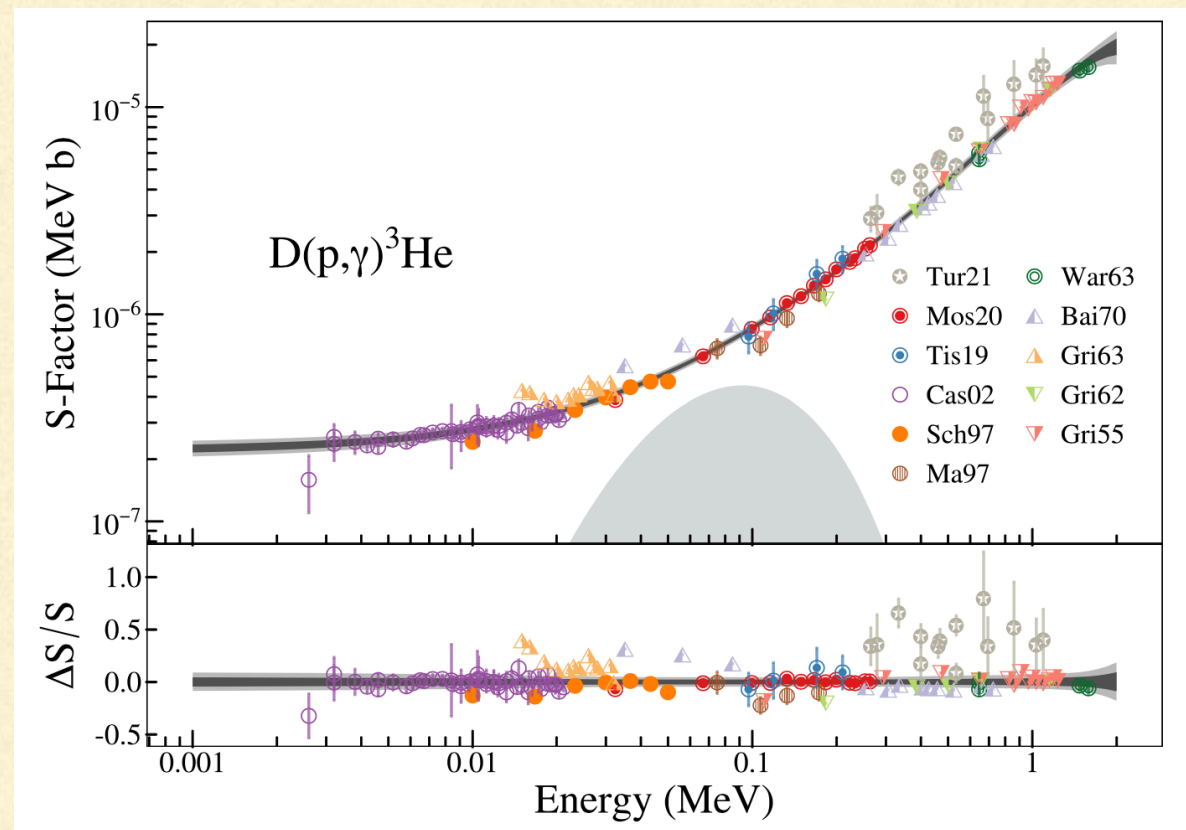
Zhang et al., PLB 751, 535 (2015)



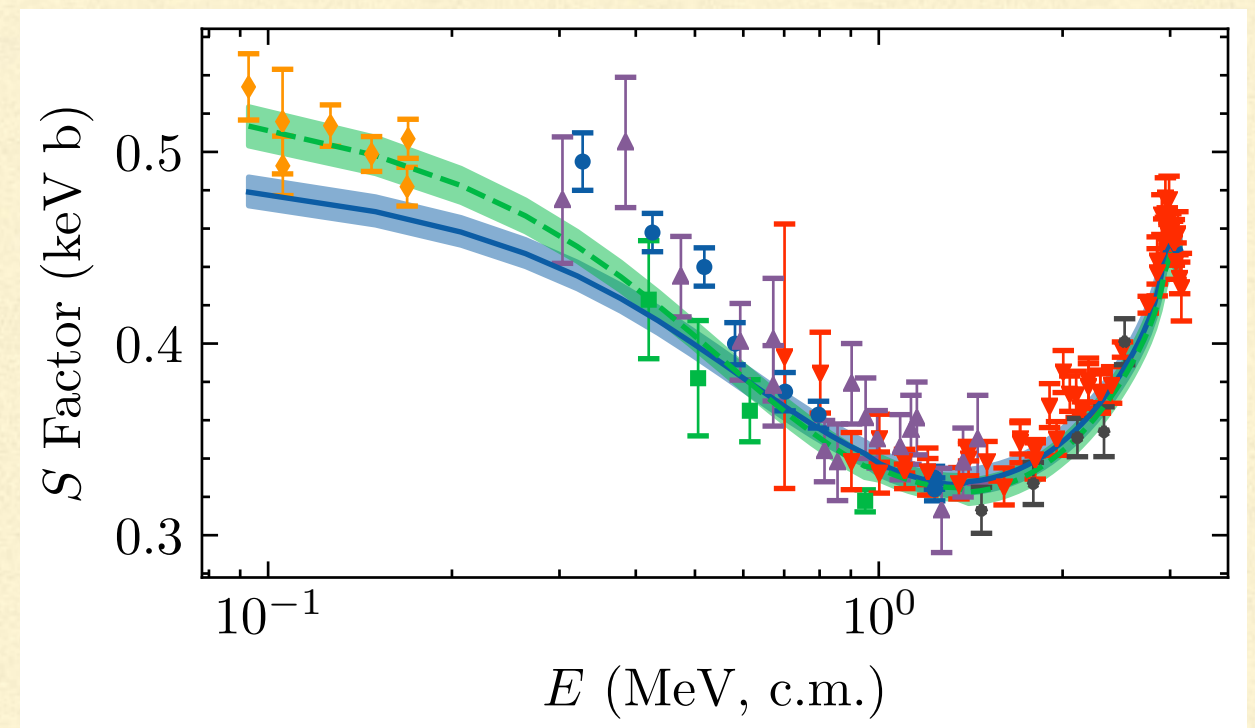
Odell et al., Front. Phys. 10 (2022) 888476

Since the 2015 Long-Range Plan

- Several forefront analyses of solar-fusion cross sections adopted a Bayesian approach to the extrapolation of experimental data to solar energies
- Done with EFT; R-matrix; polynomial; ab initio parameterizations of $S(E)$
- Permits: discovery of non-gaussian (including multi-modal) solutions for parameters; straightforward propagation of parameter uncertainty to predicted quantities; modeling of systematic experimental uncertainties



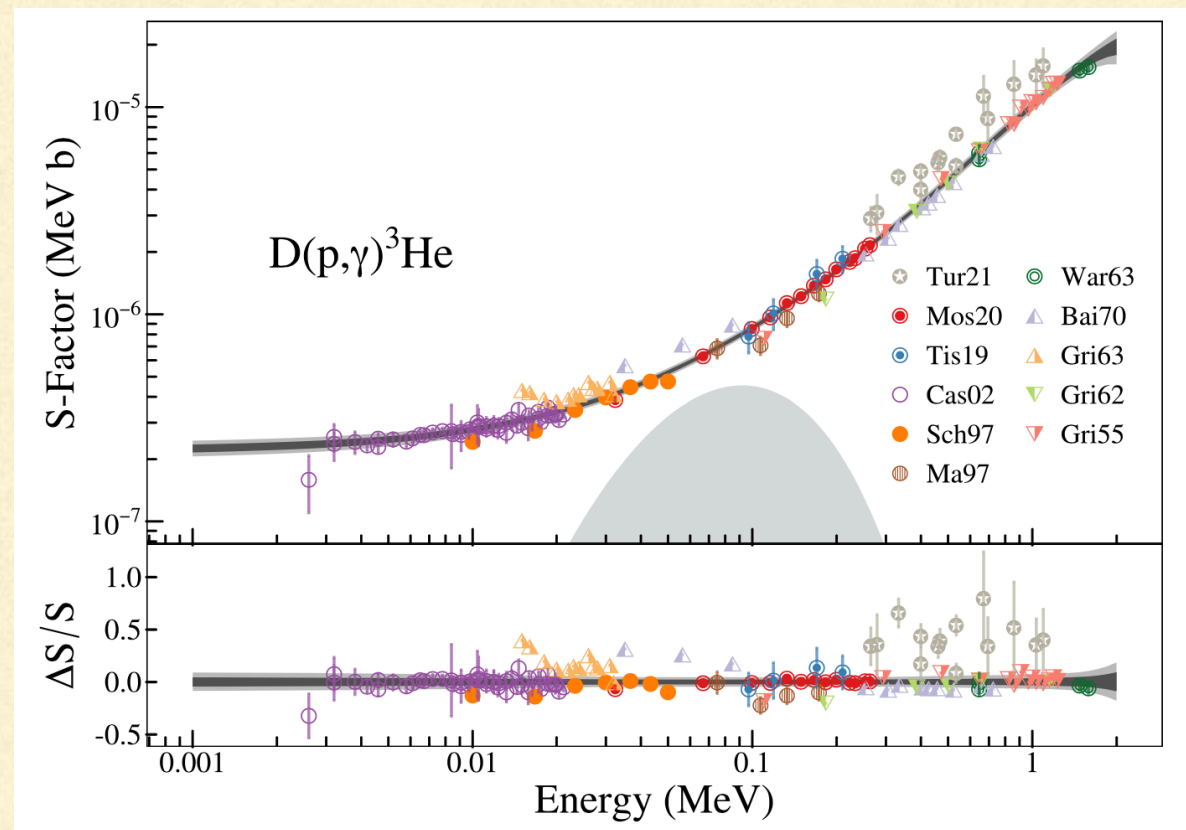
Moscoso et al., *Astrophys.J.* 923 (2021) 49



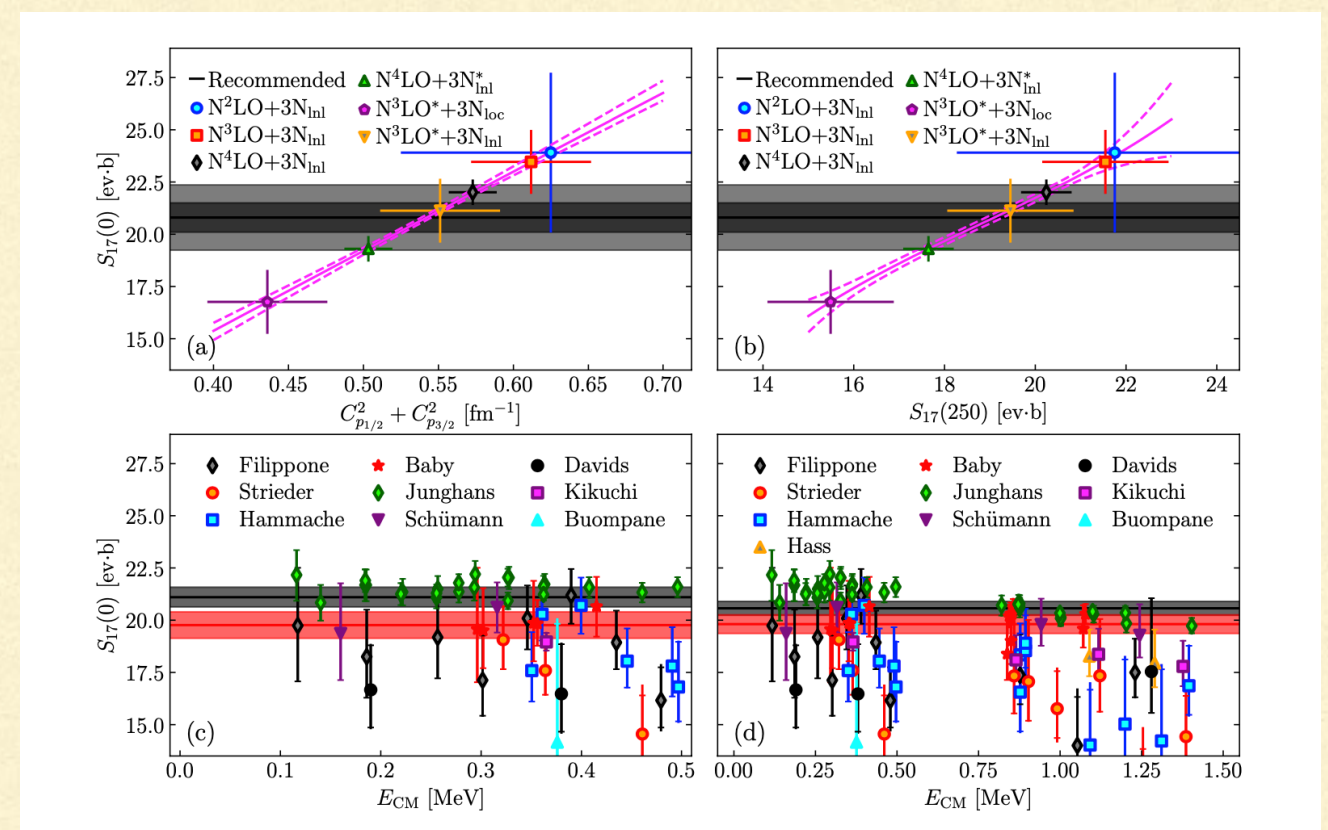
Odell et al., *Front. Phys.* 10 (2022) 888476

Since the 2015 Long-Range Plan

- Several forefront analyses of solar-fusion cross sections adopted a Bayesian approach to the extrapolation of experimental data to solar energies
- Done with EFT; R-matrix; polynomial; ab initio parameterizations of $S(E)$
- Permits: discovery of non-gaussian (including multi-modal) solutions for parameters; straightforward propagation of parameter uncertainty to predicted quantities; modeling of systematic experimental uncertainties



Moscoso et al., *Astrophys.J.* 923 (2021) 49



Kravvaris et al., arXiv:2202.11759

Needs

- Detailed discussion of systematic uncertainties, ideally with covariance matrices, in experimental publications; theory-experiment collaborations
- Collaboration with statisticians (e.g., through ISNET series of meetings, funding for inter-disciplinary collaboration) on forefront statistical approaches for these problems
- High-performance computing and/or emulators to run models and MC sampling of parameters
- Inter-model comparisons and Uncertainty Quantification

Disclaimer

- Focus is on extrapolations for $S(0)$ here; similar issues arise in other extrapolations from nuclear data, although modeling issues can be larger
 - Important work on neutron-spectrum unfolding, experimental design,
-