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# Model Uncertainty

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Ohio University



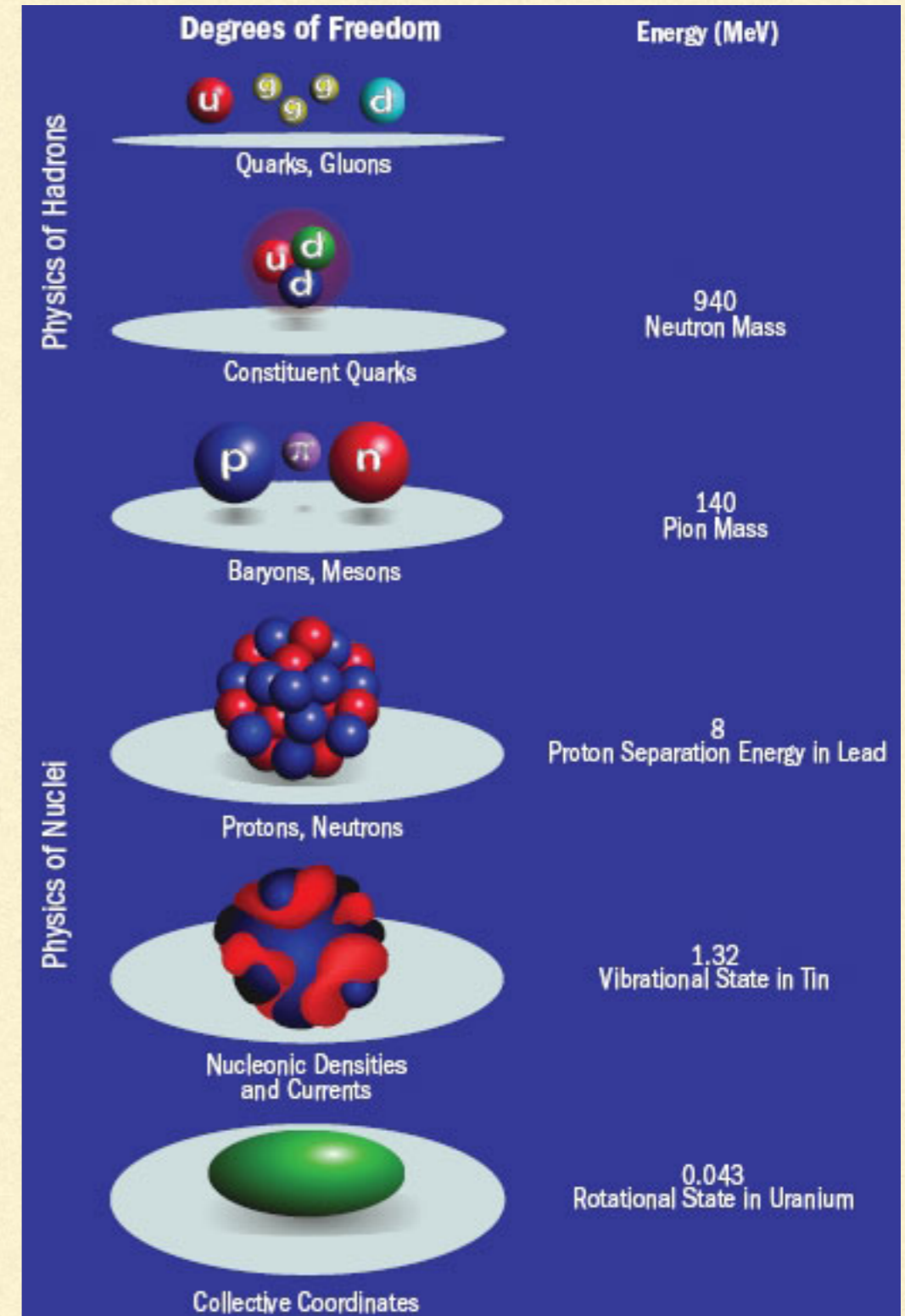
OHIO  
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AND THE DOE OFFICE OF SCIENCE, NUCLEAR PHYSICS**

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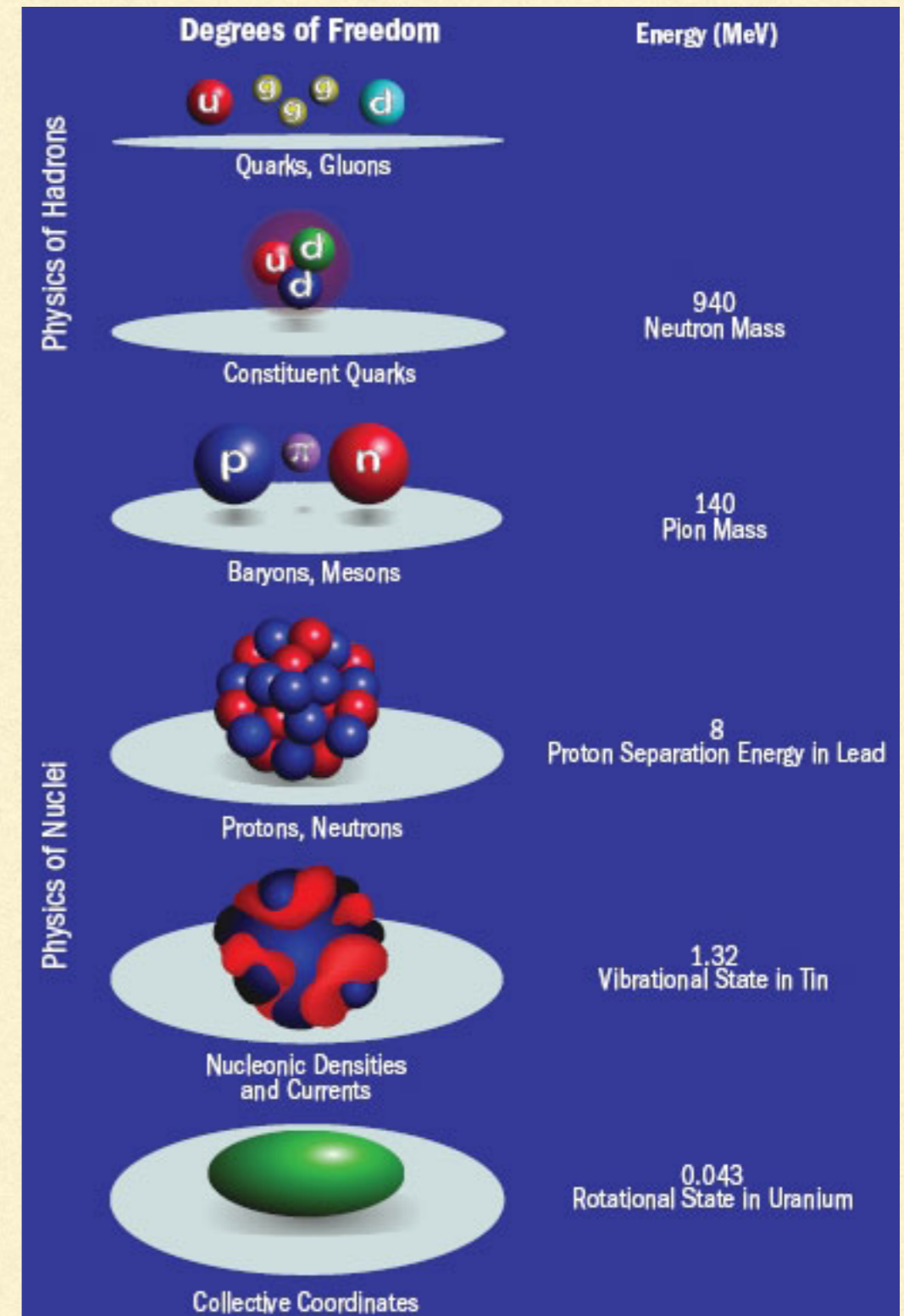
# Model Uncertainty in EFTs

- “Every useful nuclear-physics model is the leading order of some EFT”, T. Papenbrock



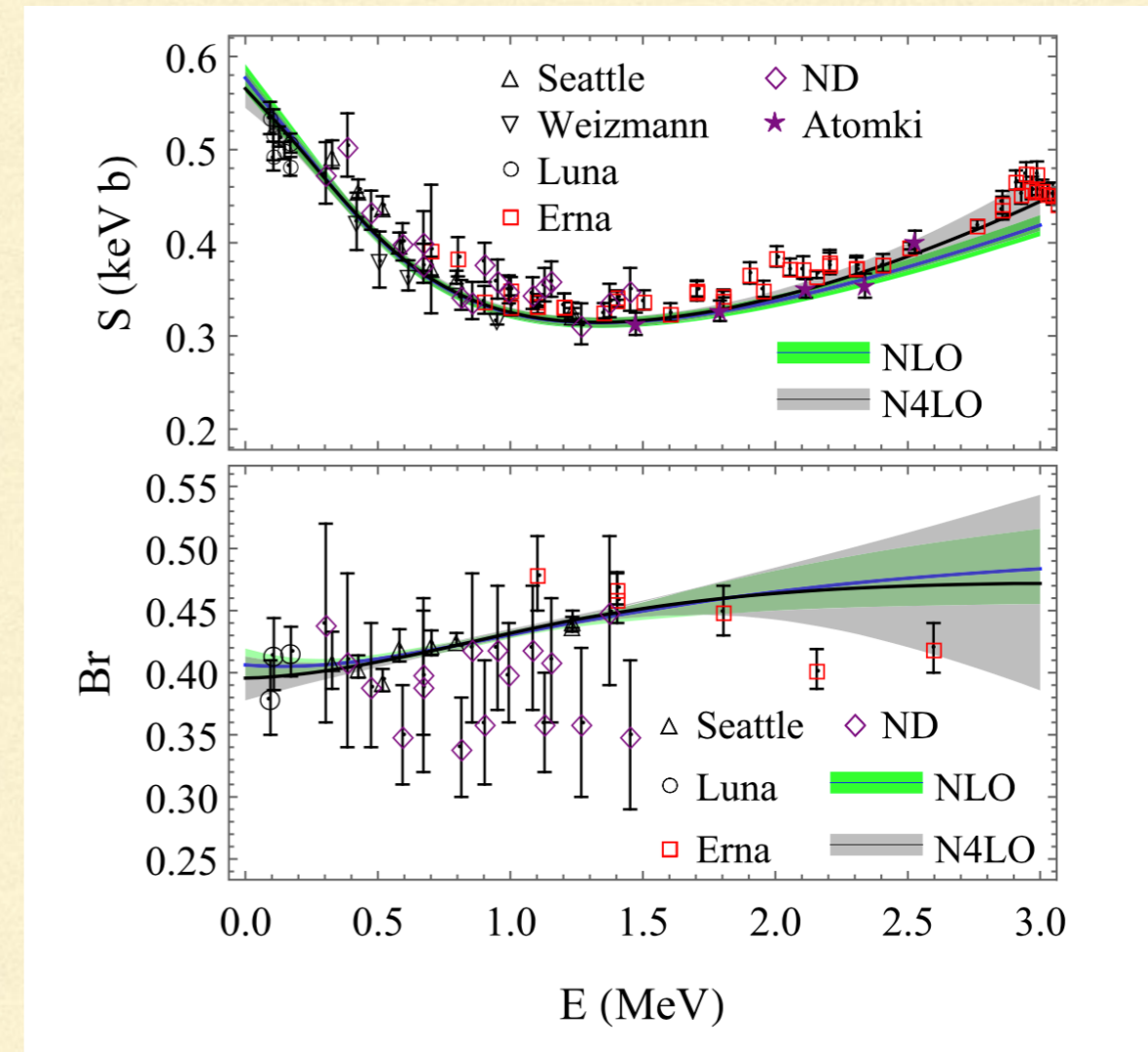
# Model Uncertainty in EFTs

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- EFTs are model independent: all models that share the EFT’s assumptions about low-energy dynamics will occupy a point in EFT parameter space. One path to assessing model uncertainty is to sample EFT parameters over reasonable ranges



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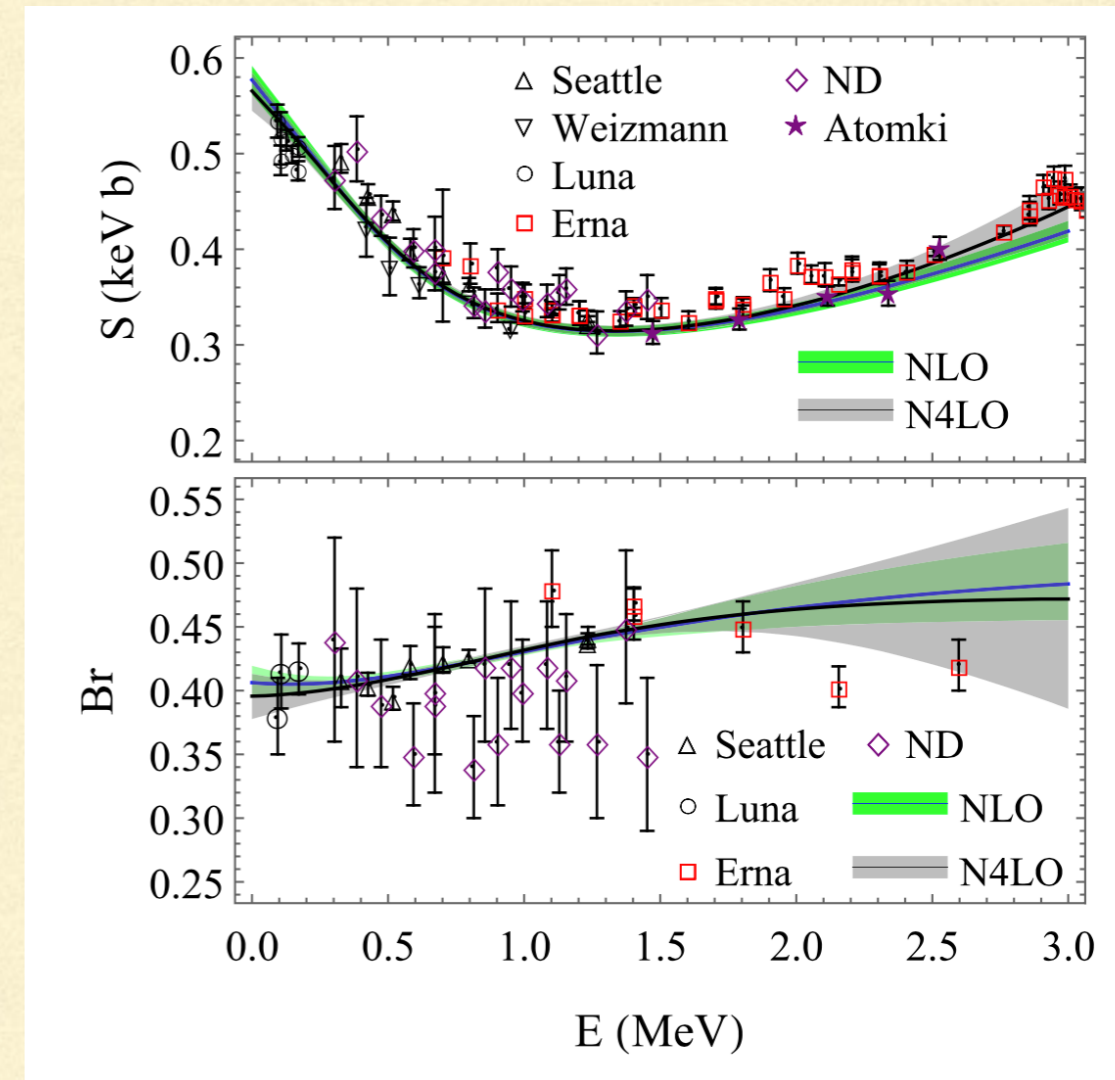


Zhang et al., *JPG* 47 (2020) 054002

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- EFTs are model independent: all models that share the EFT’s assumptions about low-energy dynamics will occupy a point in EFT parameter space. One path to assessing model uncertainty is to sample EFT parameters over reasonable ranges
- EFTs are a systematic expansion in small expansion parameter(s). So another path to model uncertainty is to assess the truncation uncertainty: that due to

$$\text{stopping } y = y_{\text{ref}} \sum_{n=0}^k c_n Q^n \text{ at order } k$$



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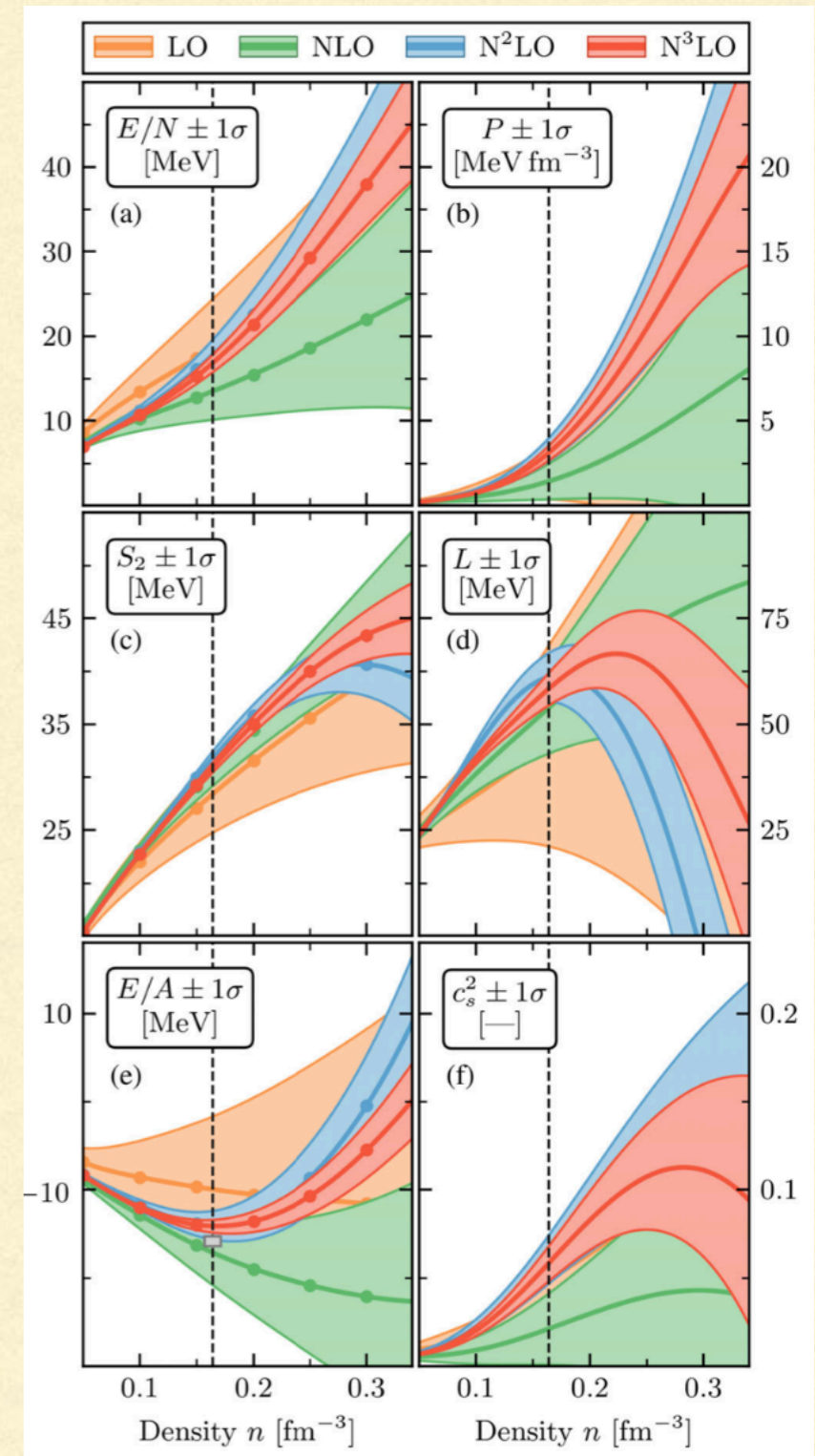
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# Future challenges

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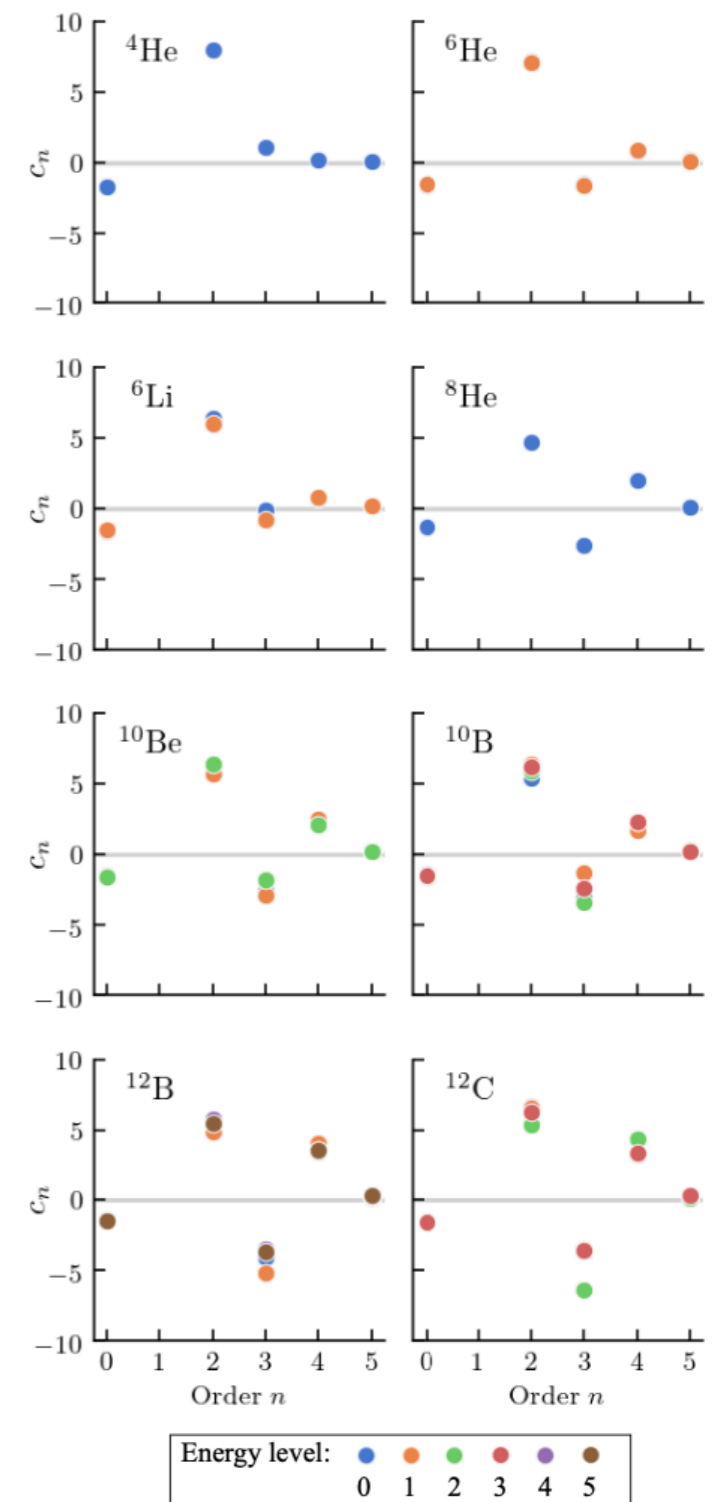
# Future challenges

- Tremendous progress in UQ for EFT since 2015 LRP. Now we need to assess the combined (& presumably correlated) effect of parameter uncertainty **and** truncation uncertainty, something few analyses so far have done. This will be computationally expensive; *fast and accurate emulators will be essential, interfaced with HPC resources for full-model runs*



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	$\mu_{3H}$	$\sigma_{np}$ [mb]	$\sigma_{nd}$ [mb]	$L_1$ fit
LO	2.75(95)	325.2±225.6	0.315(217)	N/A
NLO	2.62(31)	*334.2±79.7	0.180(43)	$\sigma_{np}$
NLO	*2.98(36)	370.0±88.0	0.345(82)	$\mu_{3H}$
NLO	2.83(34)	354.1±84.5	0.274(65)	$\sigma_{np}$ and $\mu_{3H}$
NNLO	*2.98(12)	*334.2±27.5	0.475(39)	$\sigma_{np}$
NNLO	*2.98(12)	*334.2±27.5	0.531(44)	$\mu_{3H}$
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Exp	2.979	334.2(5)	0.508(15)	N/A

Lin et al., arXiv:2210.15650

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- What about problems for which there is, as yet, no convergent EFT? Does Bayesian Model Mixing provide an accurate way forward?

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$$\text{pr}(y(x) | D) = \sum_{k=1}^K w_k(x) \text{pr}(y(x) | D, M_k)$$