



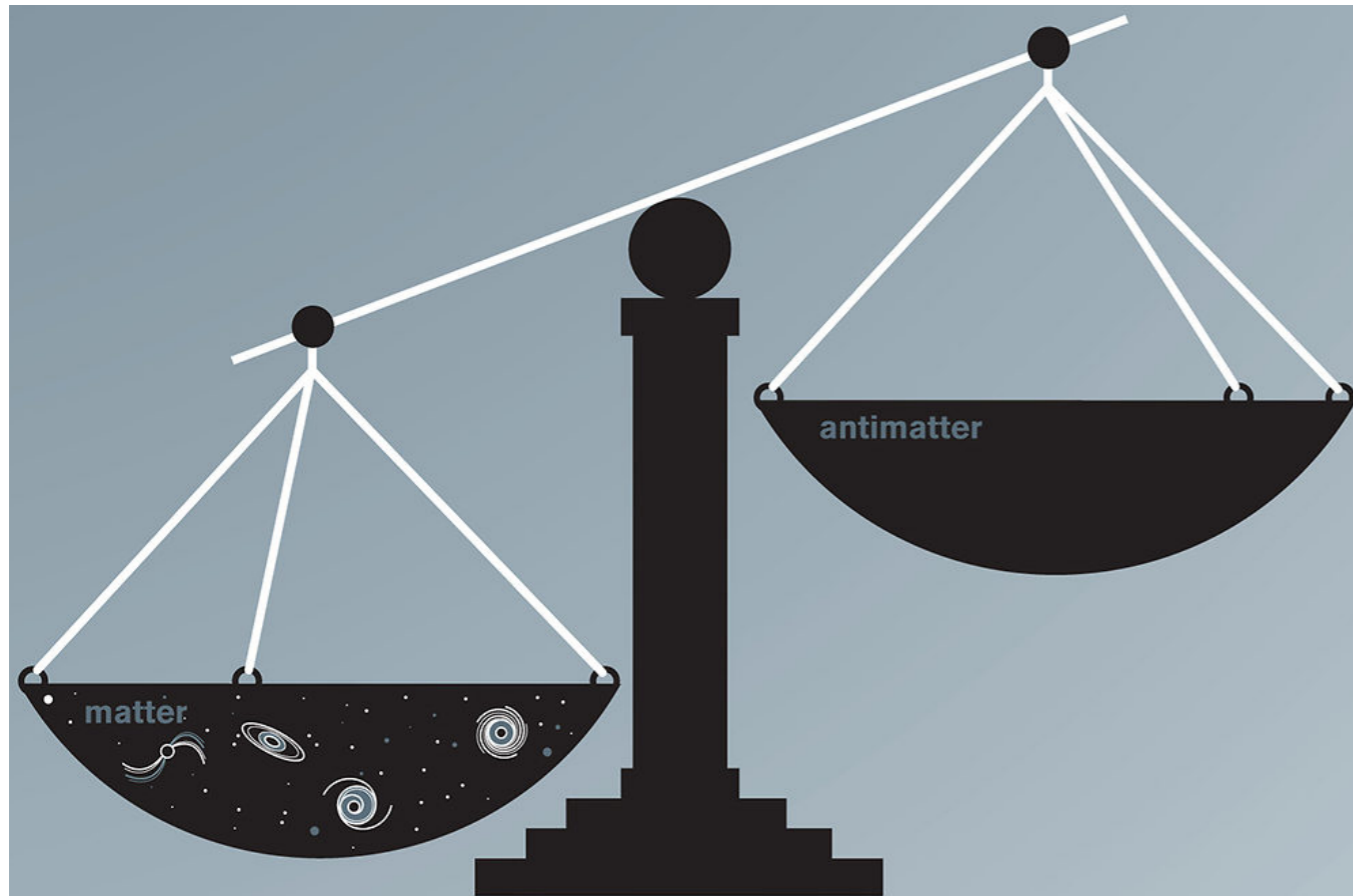
Strong PV in the nucleon?

Matteo Cerutti

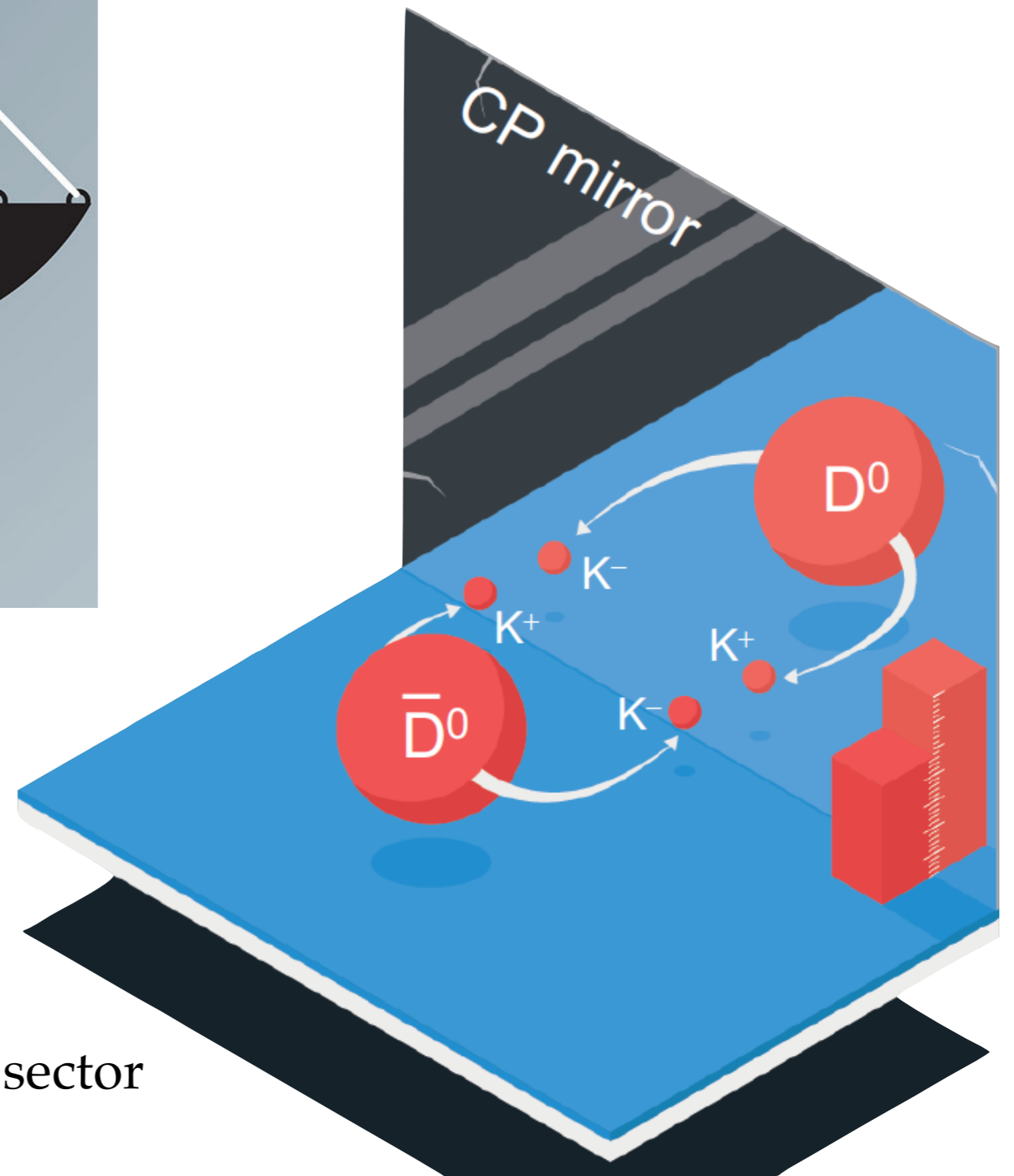
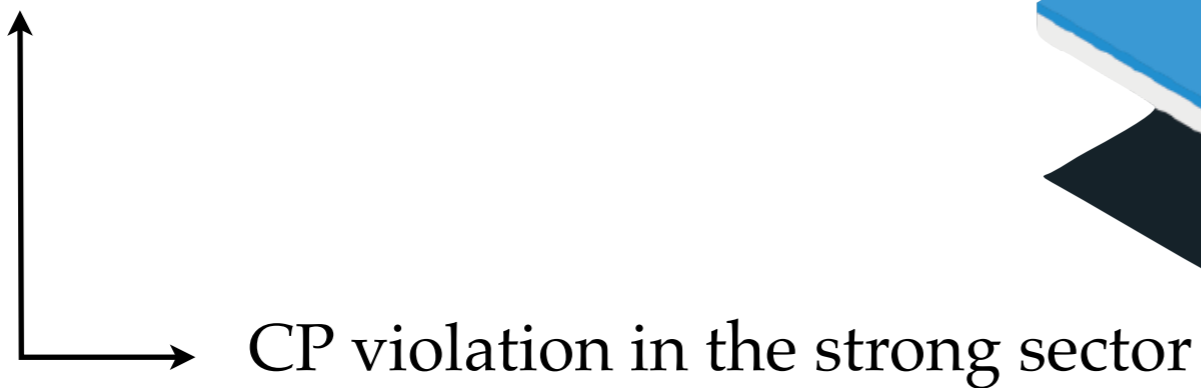
Bacchetta, MC, Manna, Radici, Zheng, PLB 849 (2024)



Motivations



matter-antimatter imbalance



Motivations

EW sector

CP violation is included

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EW sector

Weak CP

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too small...



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$$\mathcal{L}'_{\text{QCD}} = \mathcal{L}_{\text{QCD}} + \mathcal{L}^{\text{CP}}$$



Motivations

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$$\mathcal{L}'_{\text{QCD}} = \mathcal{L}_{\text{QCD}} + \mathcal{L}^{\text{CP}}$$

θ -term



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$$\mathcal{L}'_{\text{QCD}} = \mathcal{L}_{\text{QCD}} + \mathcal{L}^{\text{CP}}$$

θ -term



Nucleon electric dipole moment



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Strong CP

$$\mathcal{L}'_{\text{QCD}} = \mathcal{L}_{\text{QCD}} + \mathcal{L}^{\text{CP}}$$

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“Strong CP problem”

Nucleon electric dipole moment

never measured...



Motivations

P-symmetry

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QCD sector

QCD Lagrangian is assumed to be invariant under parity transformations

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*Are there any effects of QCD
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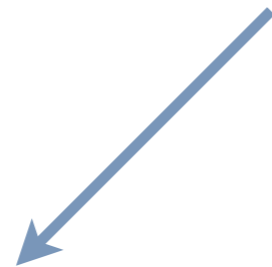
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Terms from EW sector

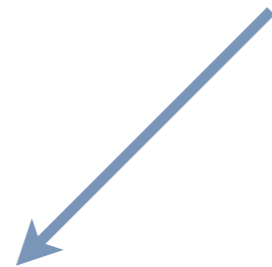
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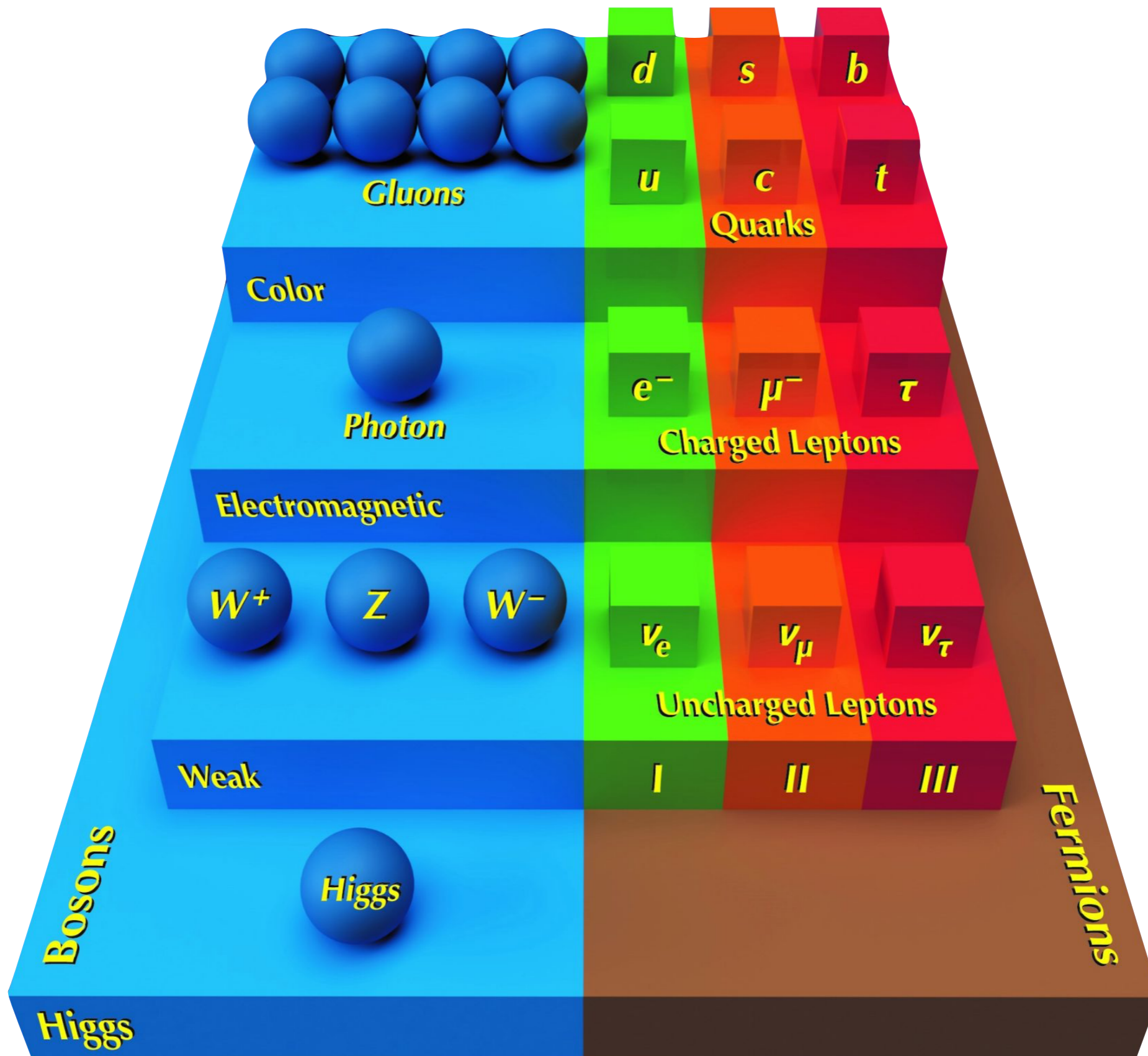
Weak P-violation

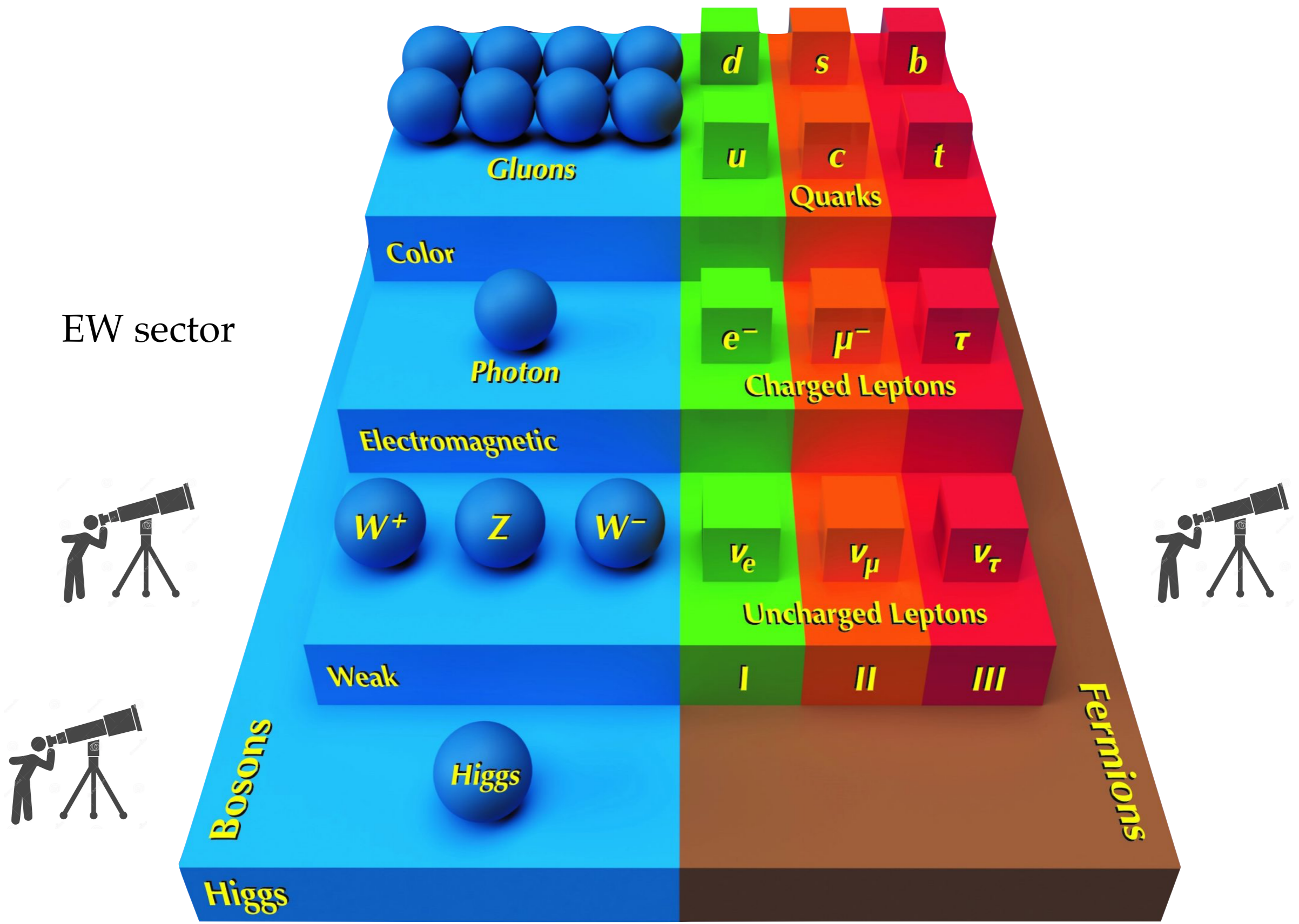


Terms from QCD sector

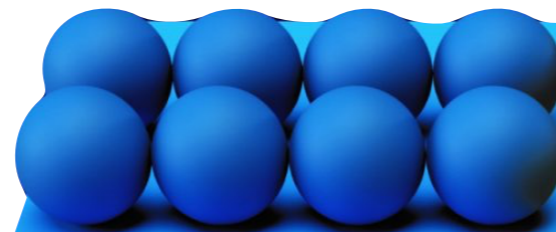
Strong P-violation







QCD sector



Gluons

Color

d

s

b

u

c

t

Quarks



EW sector



Photon

Electromagnetic

e^-

μ^-

τ

Charged Leptons



W^+

Z

W^-

ν_e

ν_μ

ν_τ

Uncharged Leptons



Weak

I

II

III



Bosons



Higgs

Fermions

Higgs

Which implications could the
presence of strong P-violation cause
to inclusive DIS?

DIS Cross Section

$$\frac{d^3\sigma}{dx_B dy d\phi_S} = \frac{\alpha^2 y}{2Q^4} L_{\mu\nu}(l, l', \lambda_e) 2MW^{\mu\nu}(q, P, S)$$

In general

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$$\eta^\gamma = 1 \quad \eta^{\gamma Z} = \left(\frac{G_F M_Z^2}{2\sqrt{2}\pi\alpha} \right) \frac{Q^2}{Q^2 + M_Z^2} \quad \eta^Z = (\eta^{\gamma Z})^2$$

Partonic Correlator (unpolarized)

Integrated correlator

$$\Phi_{ij}(x_B) = \int \frac{d\xi^-}{2\pi} e^{ik \cdot \xi} \langle P | \bar{\psi}_j(0) \psi_i(\xi) | P \rangle_{\xi^+ = \xi_T = 0}$$

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$$\Phi(x) = \Phi_{\text{PE}}(x) + \Phi_{\text{PV}}(x)$$

DIS in collinear framework

Quark Polarization

Nucleon Pol.

	U	L	T
U	$f_1(x)$		
L		$g_1(x)$	
T			$h_1(x)$

DIS in collinear framework

PDFs occurring in DIS processes

Quark Polarization

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DIS in collinear framework

PDFs occurring in DIS processes **with P violation**

Quark Polarization

	U	L	T
U	$f_1(x)$	$g_1^{PV}(x)$	
L		$g_1(x)$	
T			$h_1(x)$

Nucleon Pol.

Neutral-Current DIS

$$\frac{d\sigma^\pm}{dxdy} = \frac{2\pi\alpha^2}{xyQ^2} \left[\begin{aligned} & \left(Y_+ + \gamma^2 y^2 / 2 \right) (F_{2UU} + \lambda F_{2LU}^\pm) \\ & - y^2 (F_{L,UU} + \lambda F_{L,LU}^\pm) \\ & - \frac{Y_-}{\sqrt{1 + \gamma^2}} (x F_{3UU}^\pm + \lambda x F_{3LU}) \end{aligned} \right]$$

$$\frac{d\sigma^\pm}{dxdy} = \frac{2\pi\alpha^2}{xyQ^2} \left[Y_+ F_2^\pm - y^2 F_L^\pm \mp Y_- x F_3^\pm \right]$$

Particle Data Group, Tanabashi, et al., PRD 98 (2018)

Focus: structure function $xF_3(x, Q^2)$

$$xF_{3LU}(x, Q^2) = xF_3^{(\gamma)} - g_V^e \eta_{\gamma Z} xF_3^{(\gamma Z)} + (g_V^e{}^2 + g_A^e{}^2) \eta_Z xF_3^{(Z)}$$

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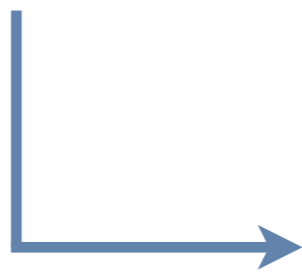
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Additional contributions
due to the new PV parton
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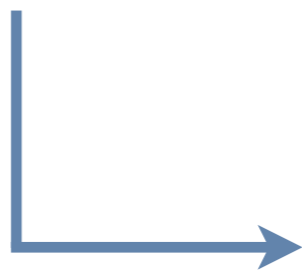
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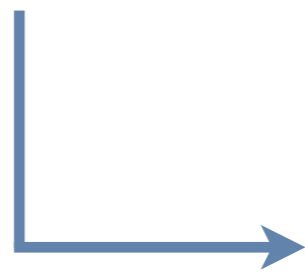
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**MAIN INNOVATION
OF PV-HYPOTHESIS**



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Phenomenology

Experimental information

PVDIS Asymmetry

$$A_{PV} \equiv \frac{d\sigma(\lambda = 1) - d\sigma(\lambda = -1)}{d\sigma(\lambda = 1) + d\sigma(\lambda = -1)}$$

PVDIS Collaboration, *Nature* 506 (2014)
D. Wang et al., *Phys.Rev.C* 91 (2015)

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$$Y_{\pm} = 1 \pm (1 - y)^2$$

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$$= \frac{Y_+ \boxed{F_{2LU}} - y^2 \boxed{F_{L,LU}} - Y_- \boxed{x F_{3LU}}}{Y_+ \boxed{F_{2UU}} - y^2 \boxed{F_{L,UU}} - Y_- \boxed{x F_{3UU}}}$$

Contribution of g_1^{PV} in each of
the structure functions due to
 γZ and Z channels

$$Y_{\pm} = 1 \pm (1 - y)^2$$

Available experimental data sets

HERA dataset (Run I + II combined)

H1 Collaboration, Eur. Phys. J. C 78 (2018)

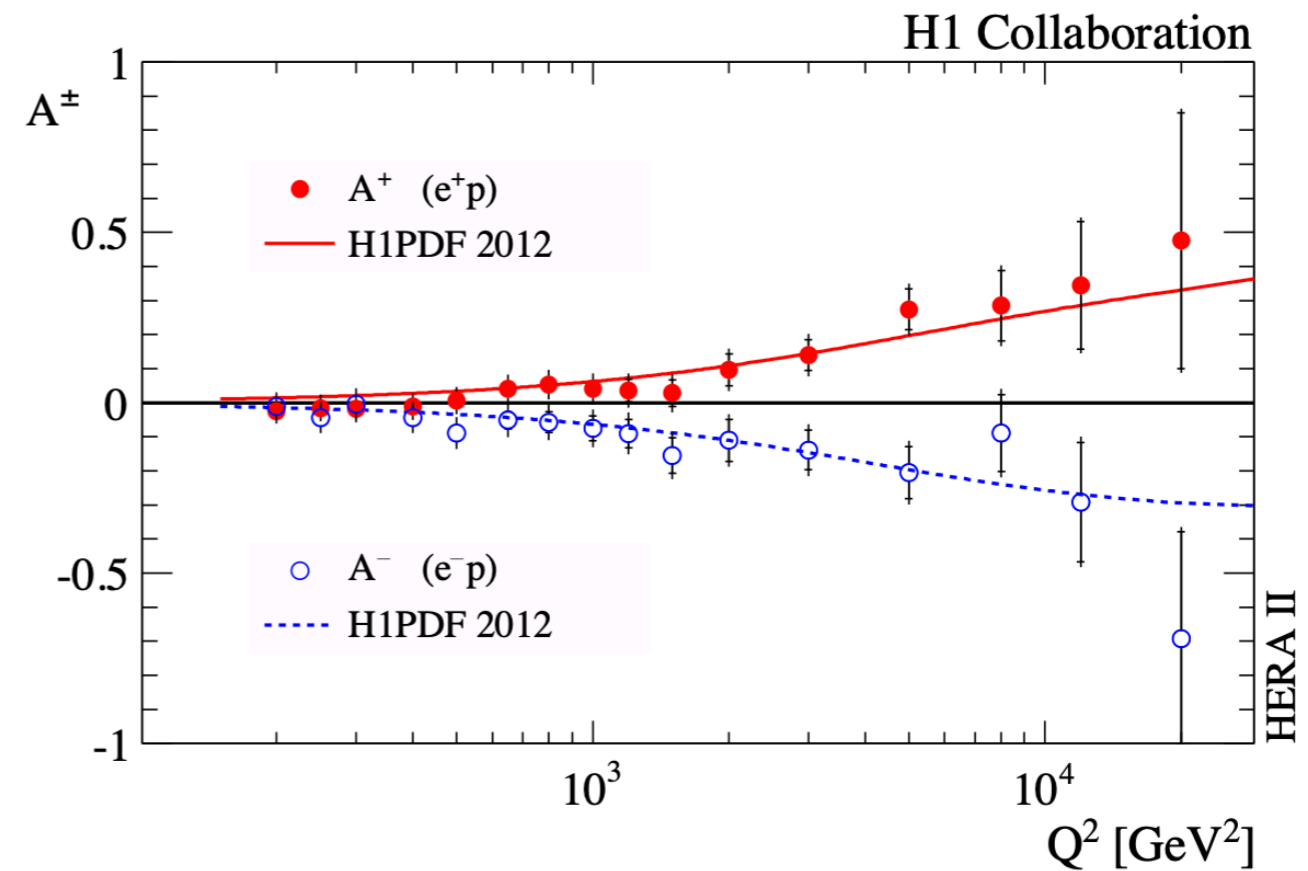
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e^+ asymmetry: 136 data

e^- asymmetry: 138 data



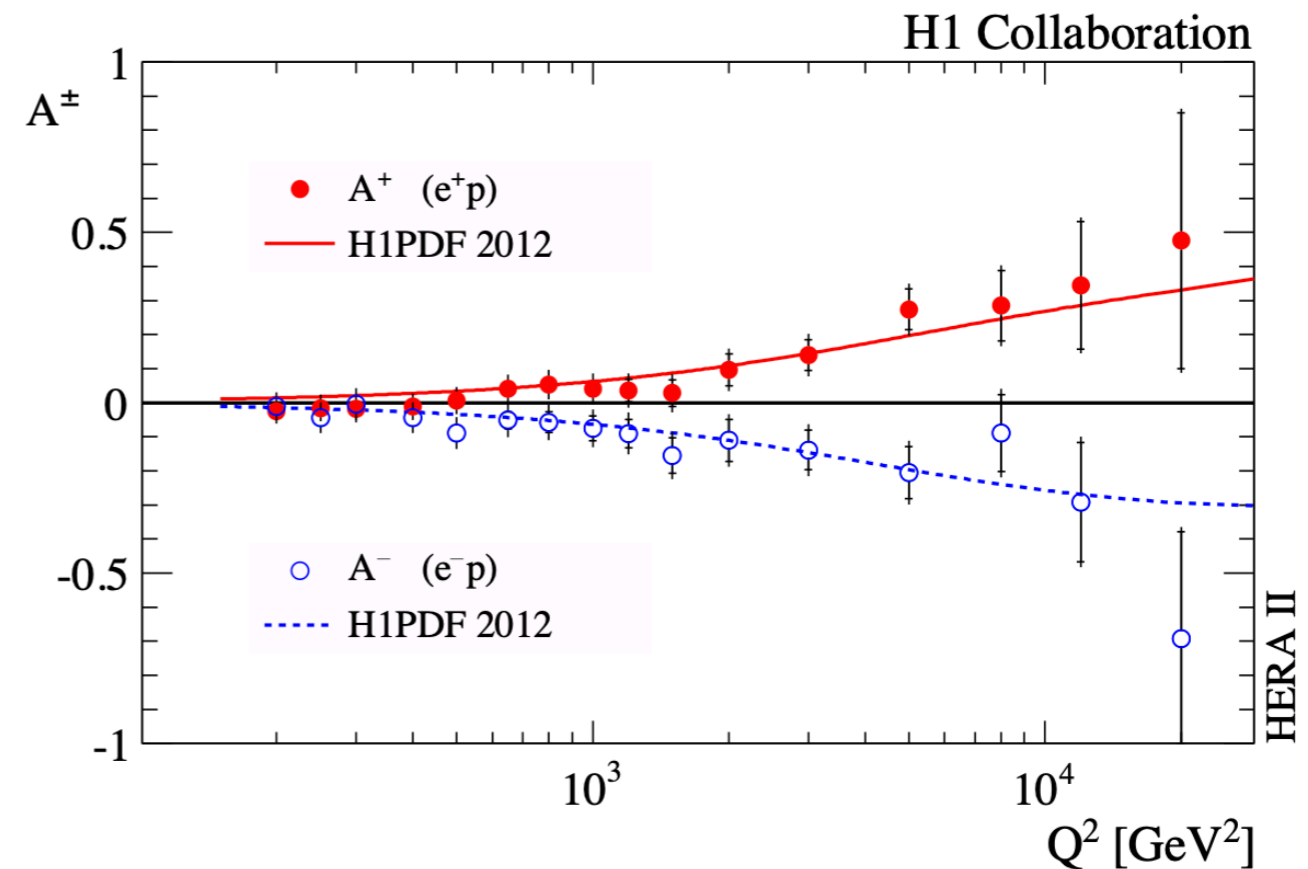
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JLab6 PVDIS dataset

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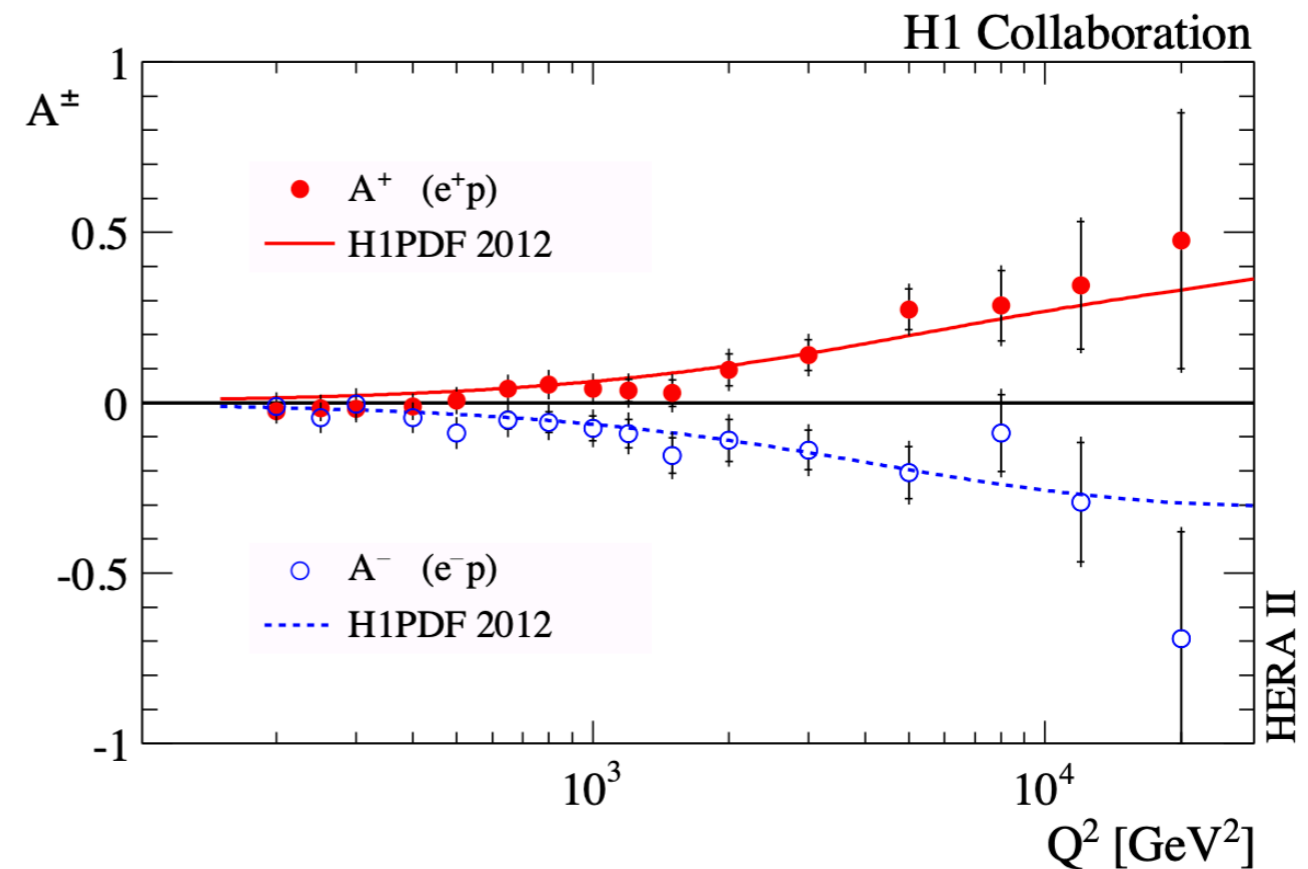
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e^- asymmetry: 2 data

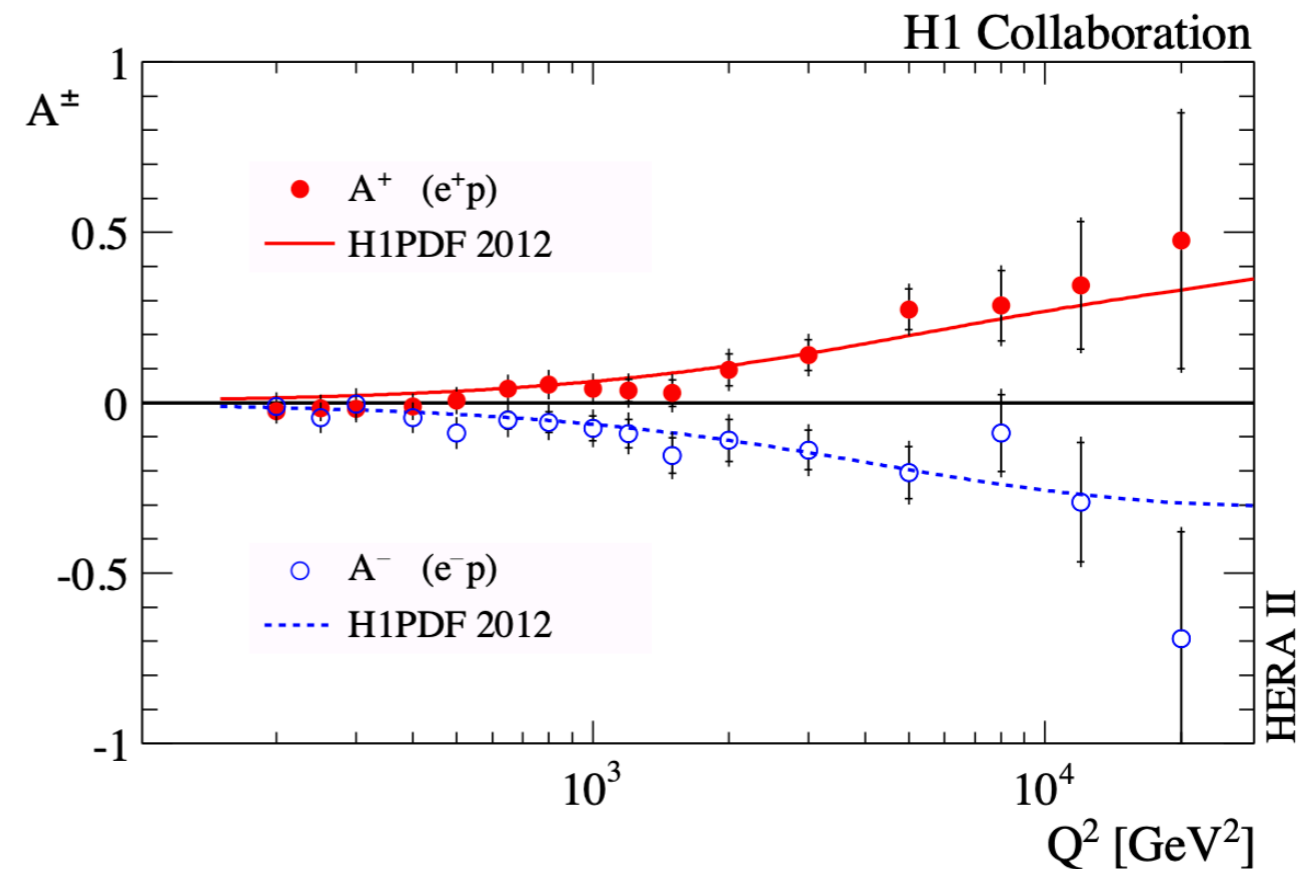
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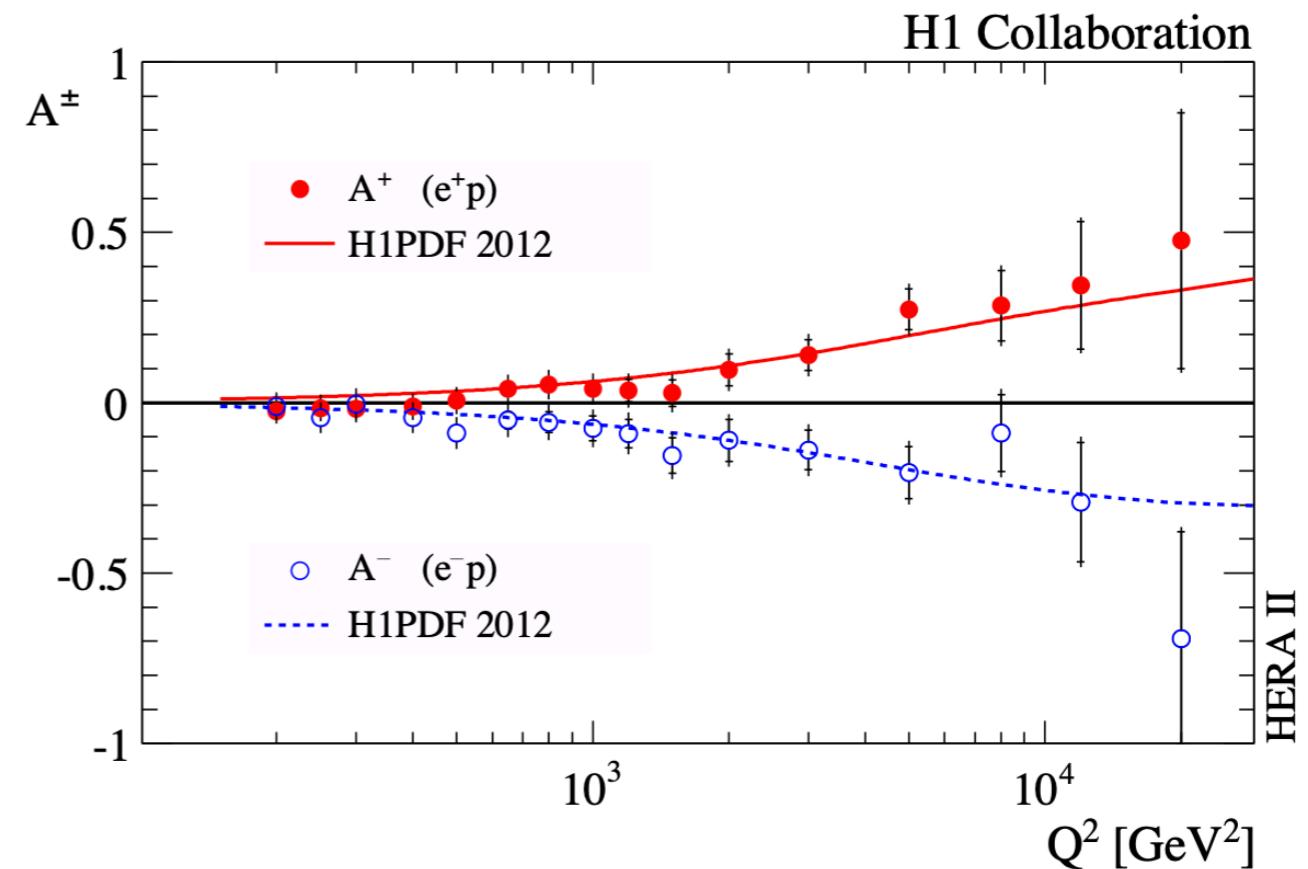
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e^- asymmetry: 11 data

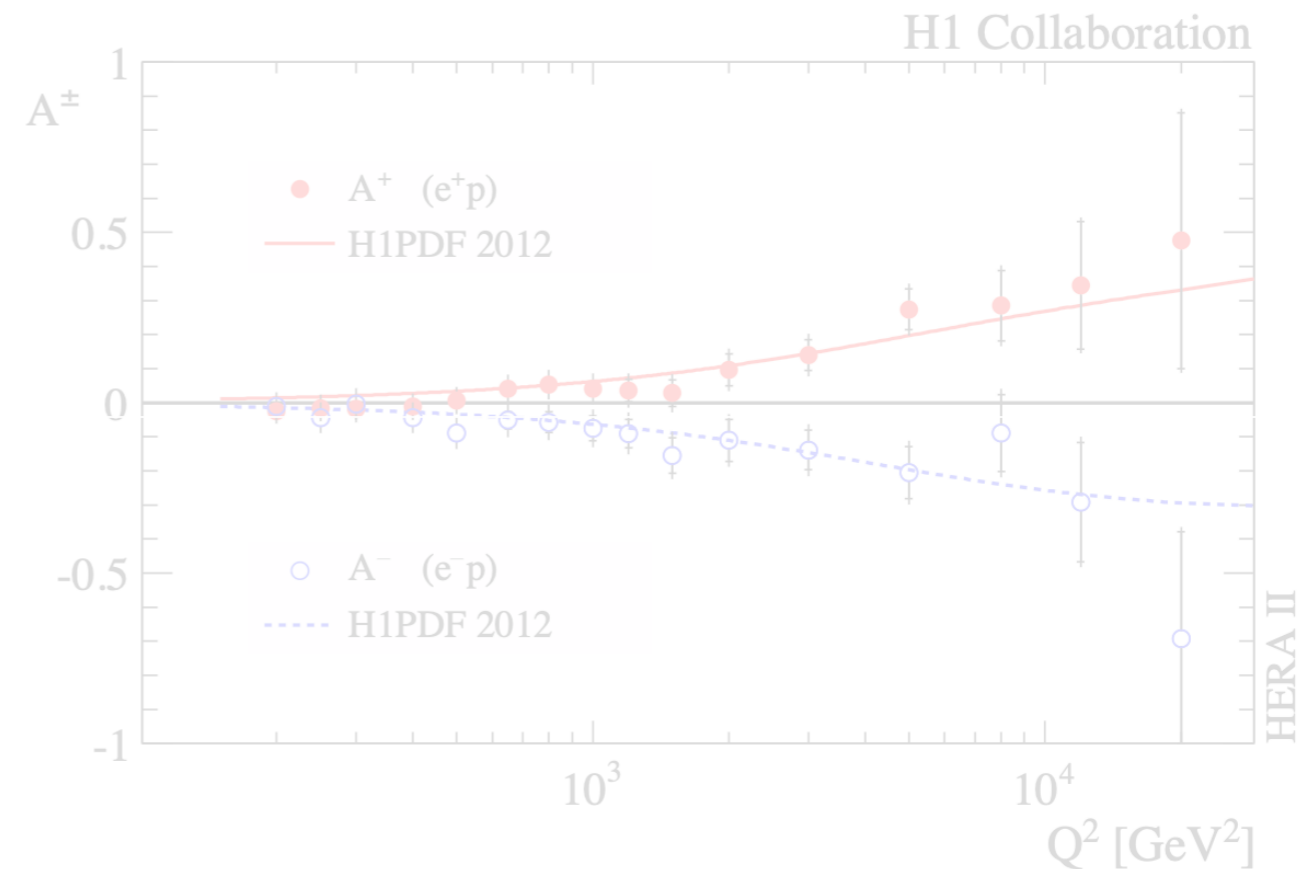
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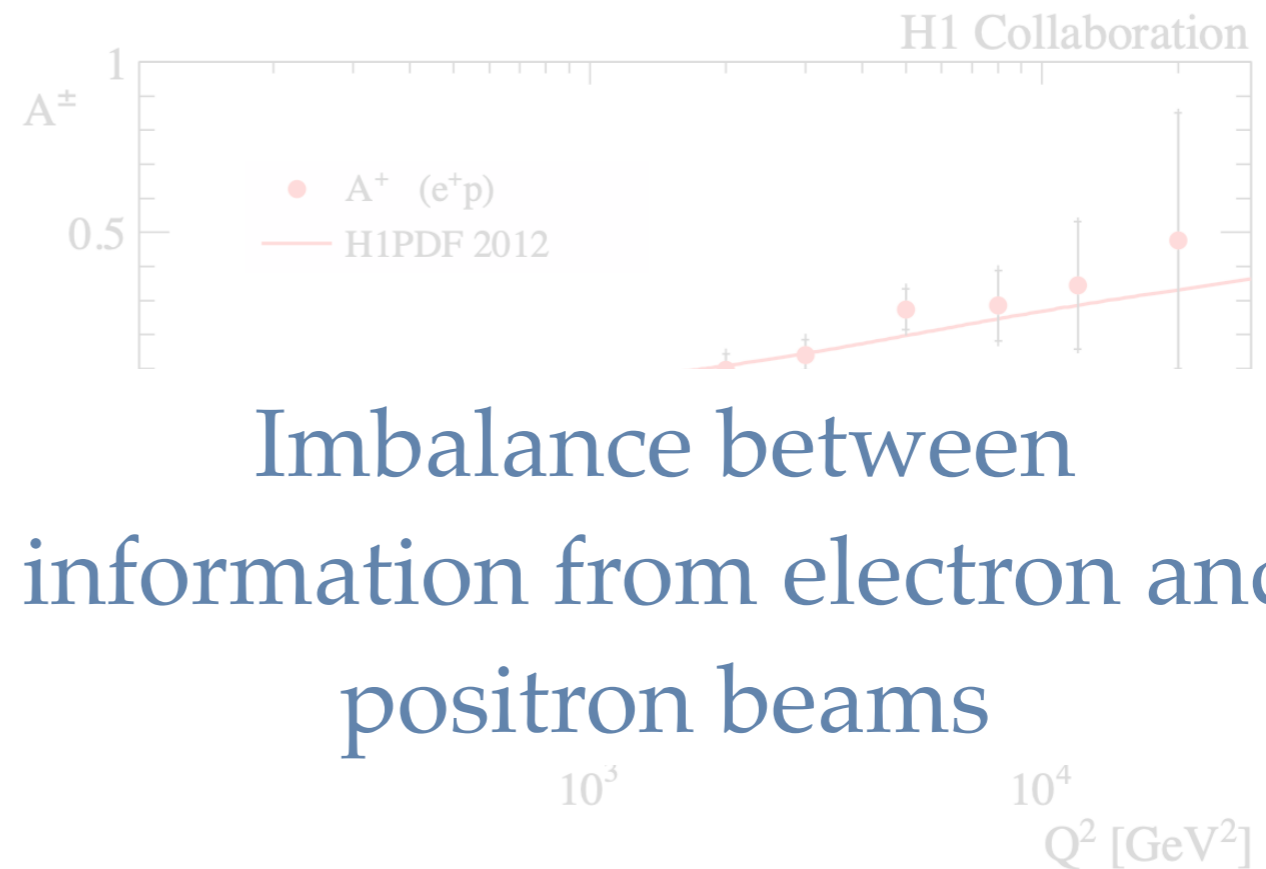
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Imbalance between
information from electron and
positron beams

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e^- asymmetry: 11 data

Parameterization of $g_1^{PV}(x, Q^2)$

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PV parton density comes from the structure

$$\gamma^5 \gamma^\mu$$

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 \longrightarrow **C-odd**

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1 parameter to be fitted

Error propagation in the analysis

PDF set for

Error propagation in the analysis

PDF set for

$$f_1(x, Q^2)$$

NNPDF4.0

Ball et al. (NNPDF), EPJ C 82 (2022)

Error propagation in the analysis

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100 MC replicas of unpolarized PDF

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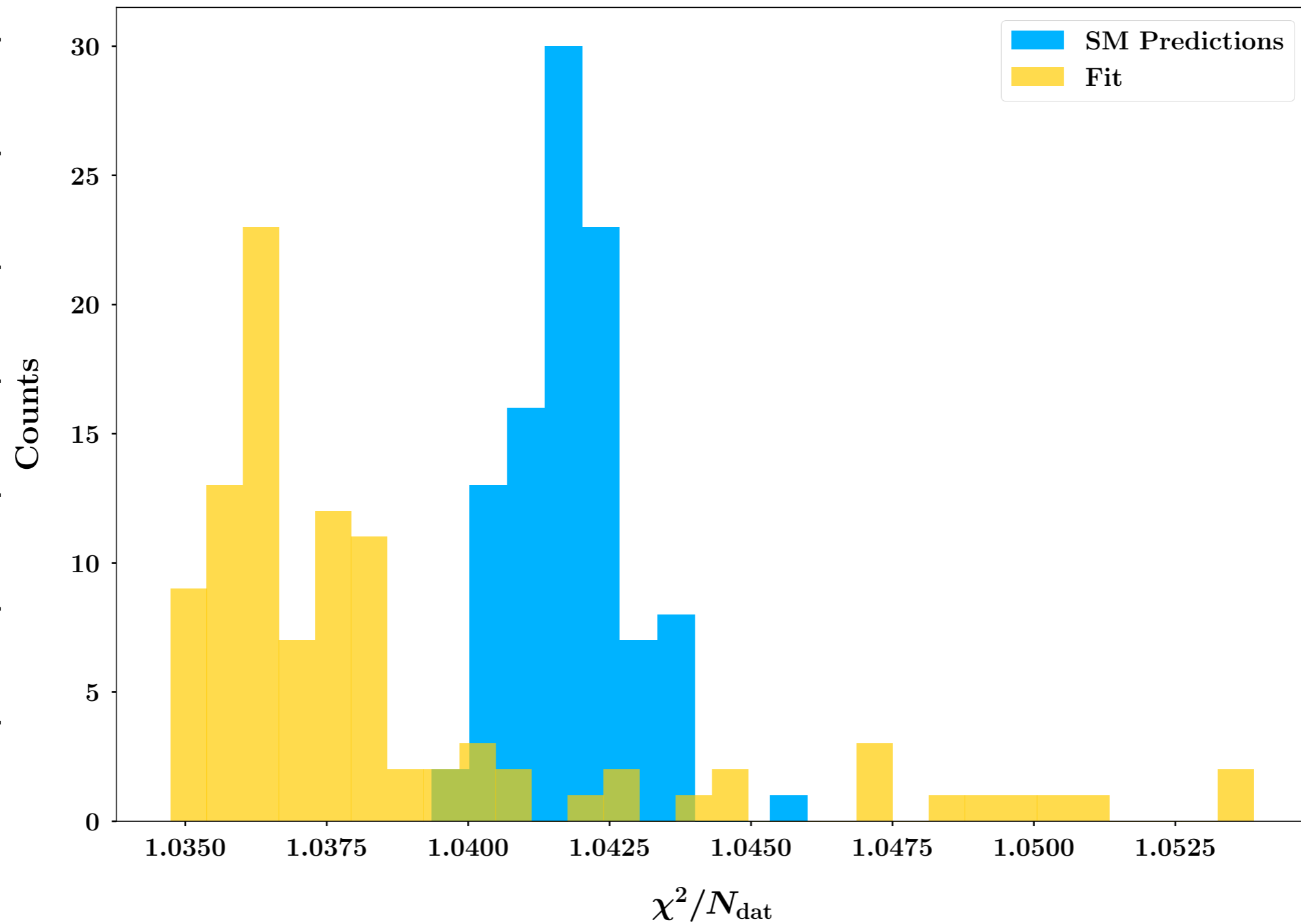
100 MC replicas experimental data

Statistical distribution of
100 values of parameter α

Results of the fit

	N of points	χ^2/N_{data} (SM)	χ^2/N_{data} (Fit)
HERA e^+	136	1.12	1.12
HERA e^-	138	0.98	0.98
JLab6	2	0.67	0.42
SLAC-E122	11	0.97	0.94
<i>TOTAL</i>	<i>287</i>	<i>1.042</i>	<i>1.037</i>

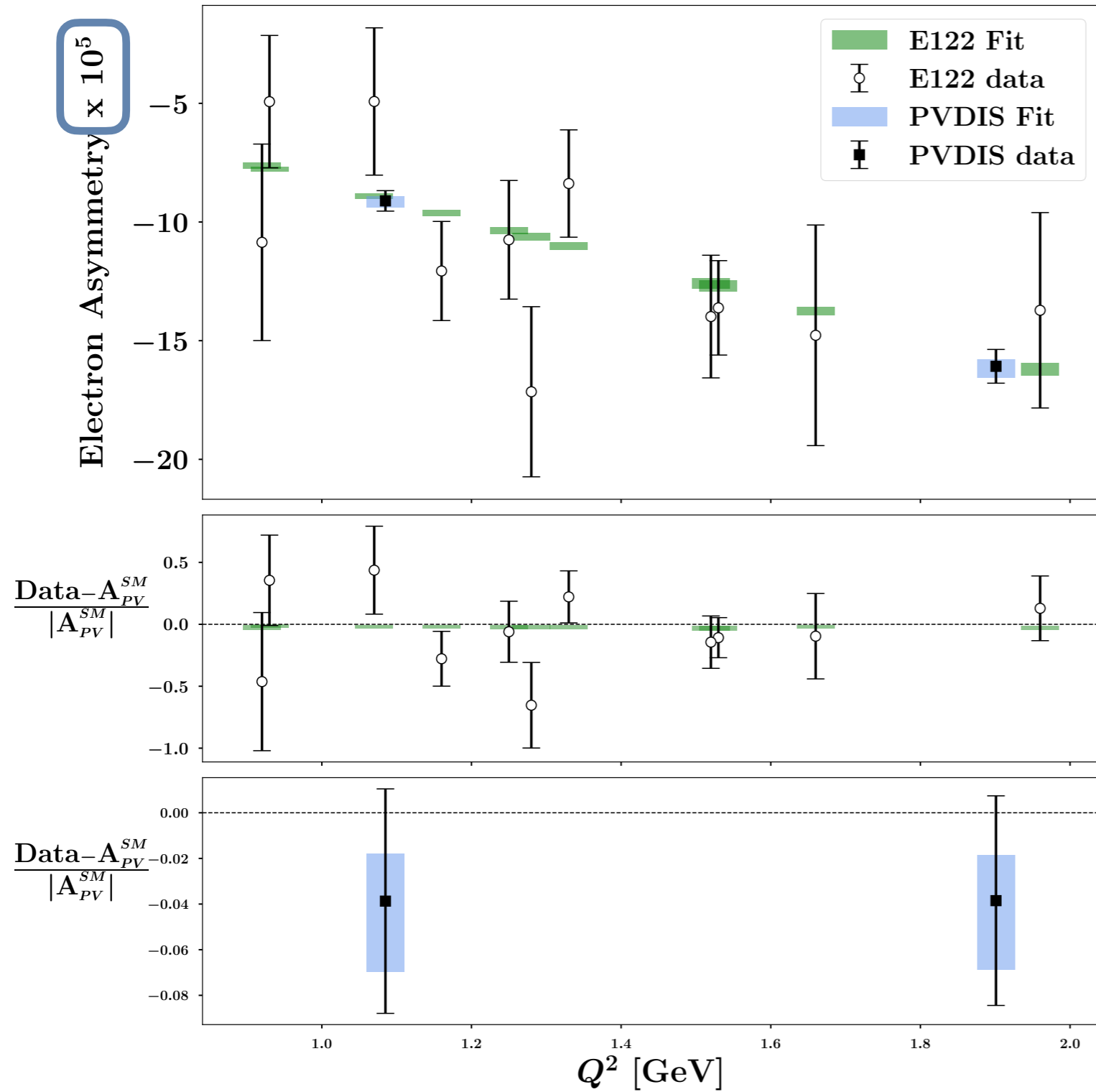
Results of the fit



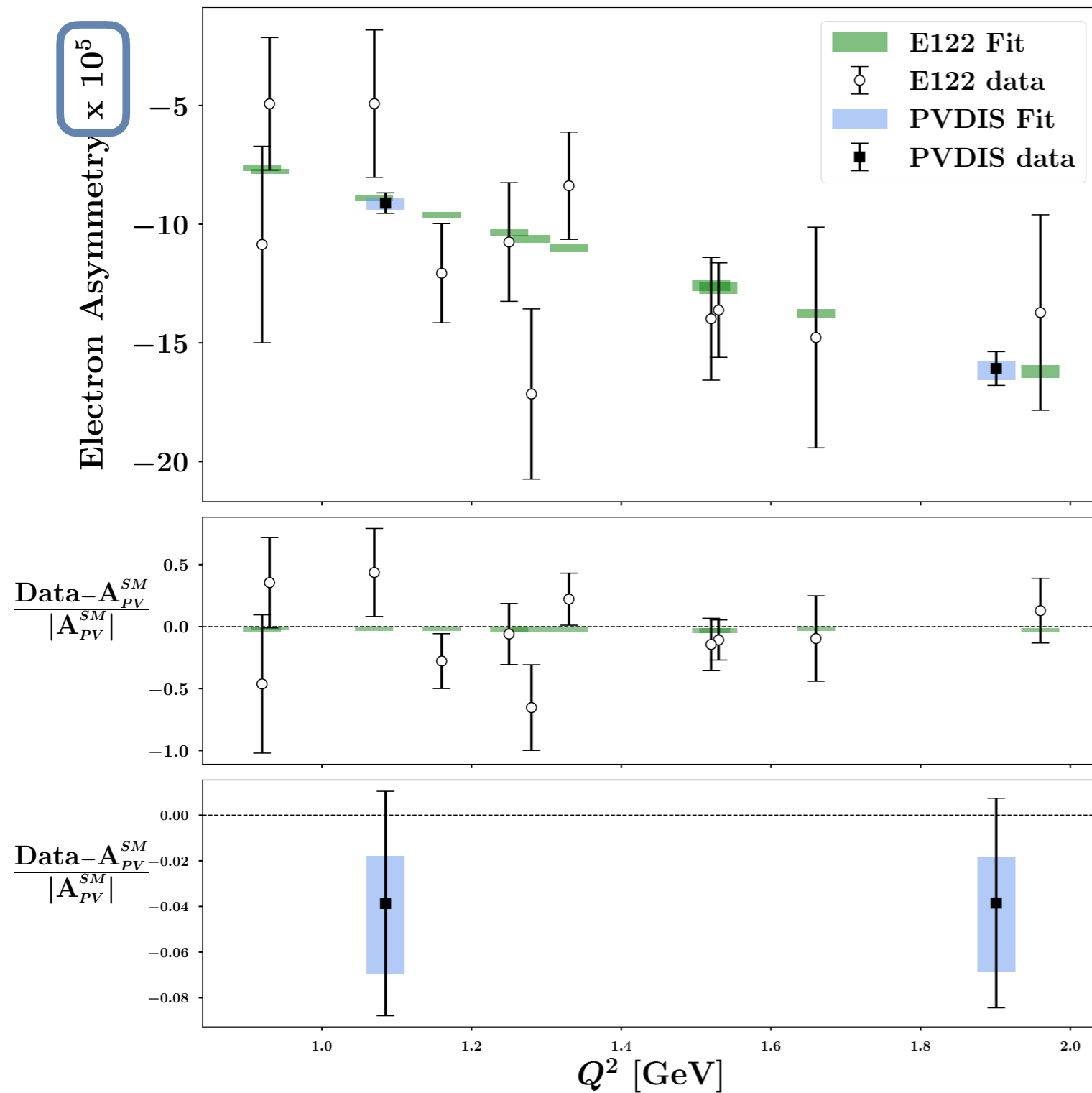
Fit)

7

Results of the fit: data vs theory

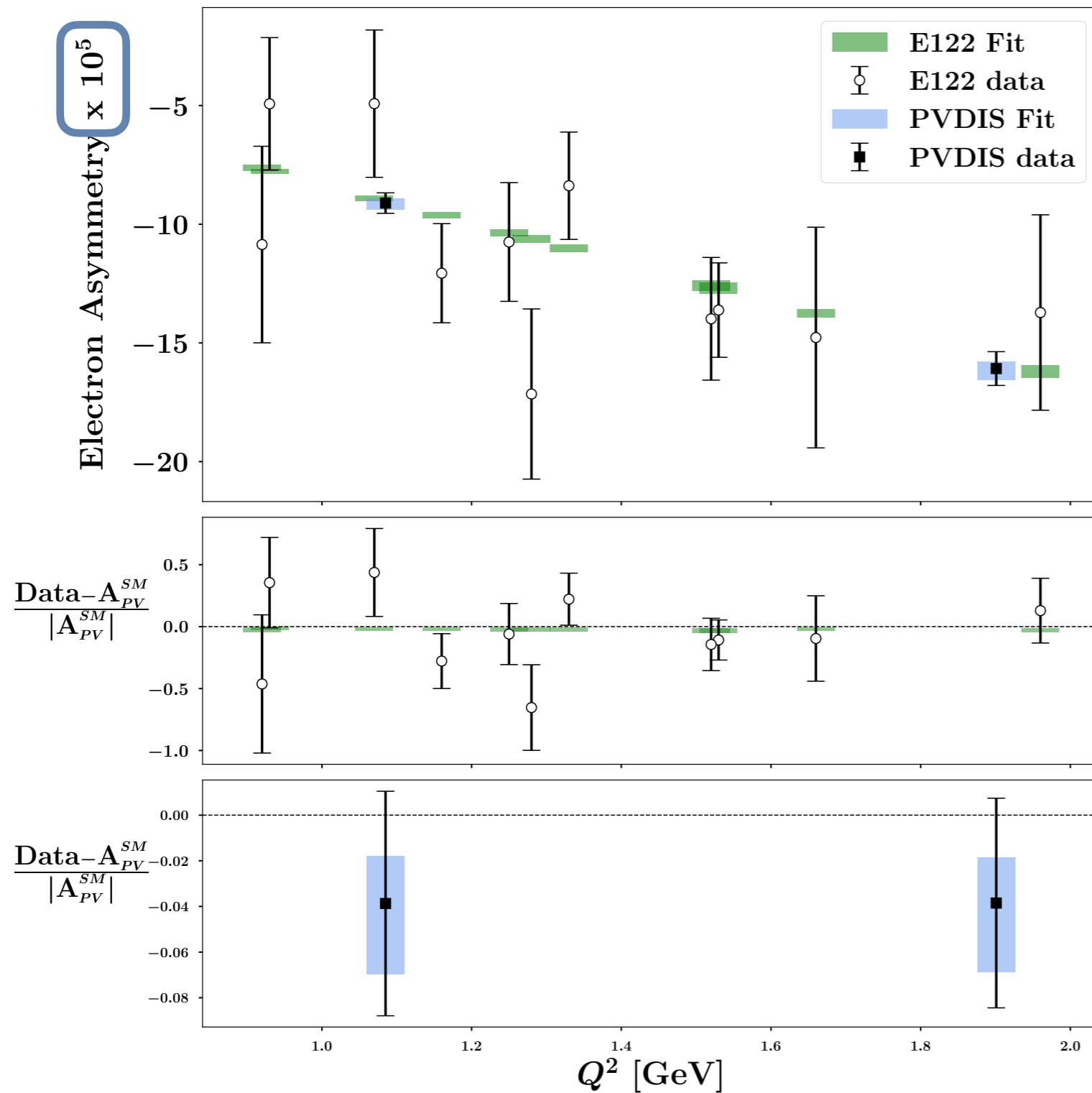


Results of the fit: data vs theory



Sizeable improvement of the fit
w.r.t. SM predictions

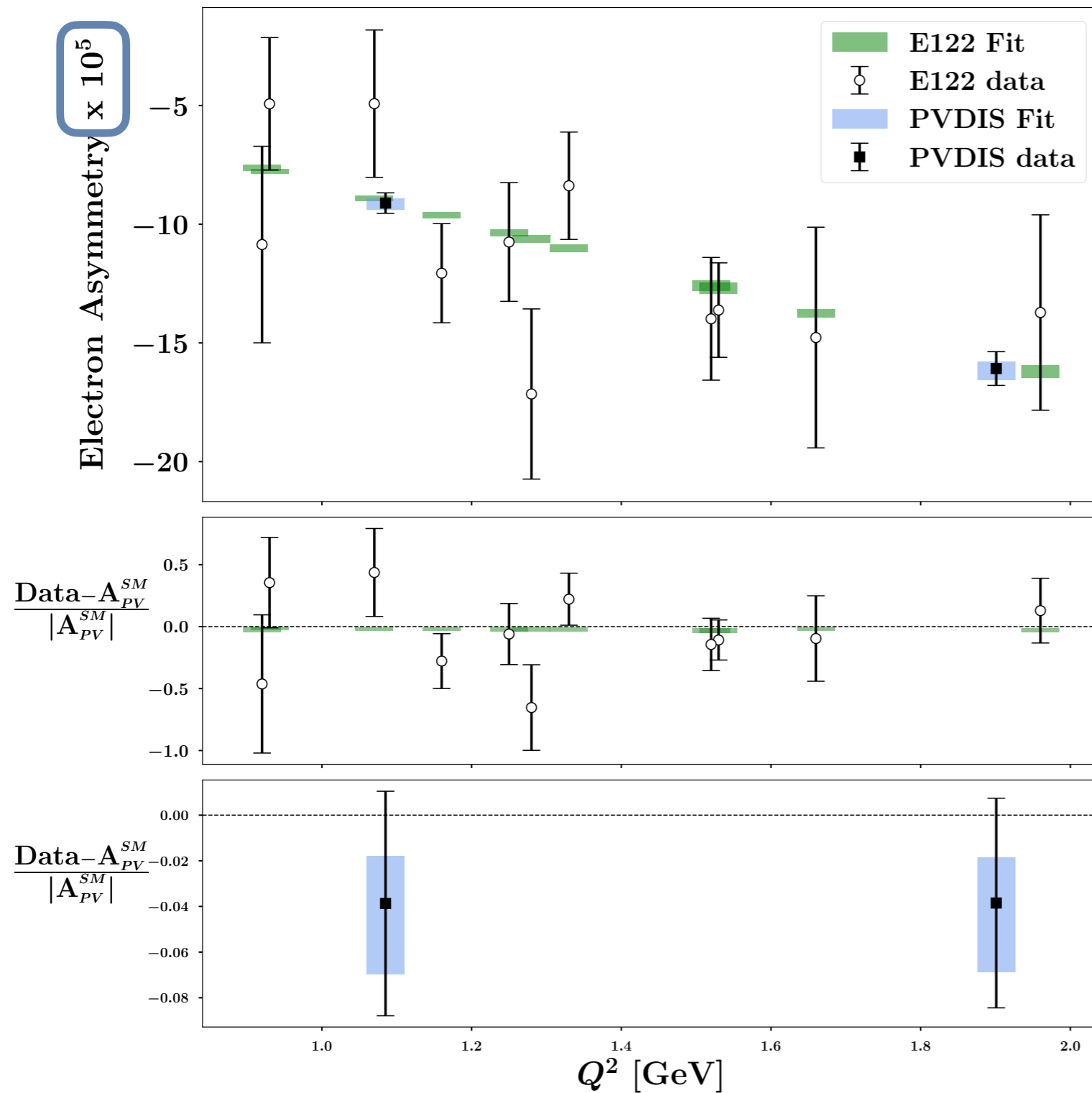
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Old dataset with still quite large
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Results of the fit: data vs theory



Sizeable improvement of the fit
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Old dataset with still quite large
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Data points which actually
drive the fit due to very small
experimental errors ($\sim \%$)

Results: size of the strong PV effect

$$g_1^{\text{PV}}(x) = \alpha g_1(x)$$

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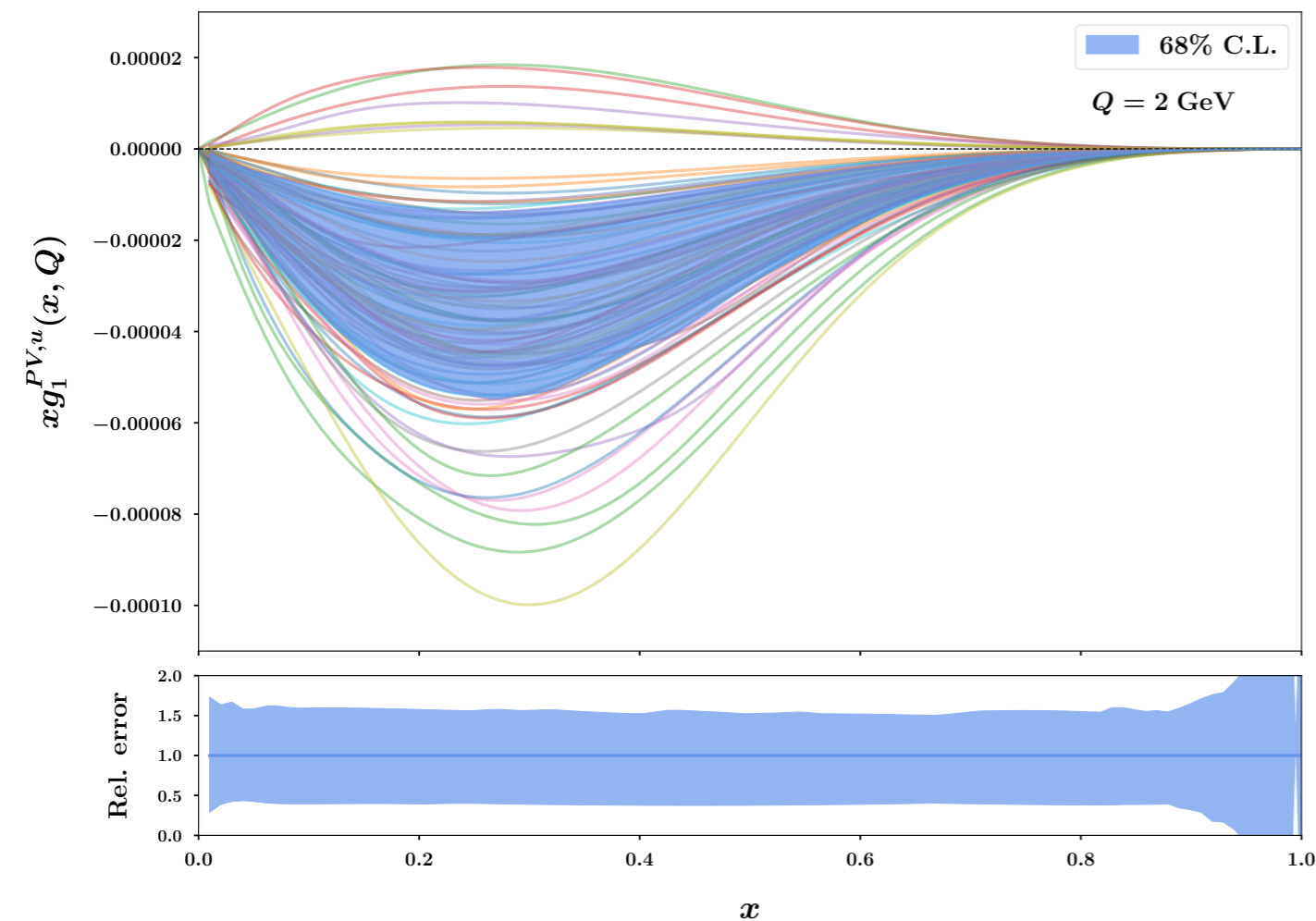
$$g_1^{\text{PV}}(x) = \alpha g_1(x)$$

$$\alpha = (-1.01 \pm 0.66) \cdot 10^{-4}$$

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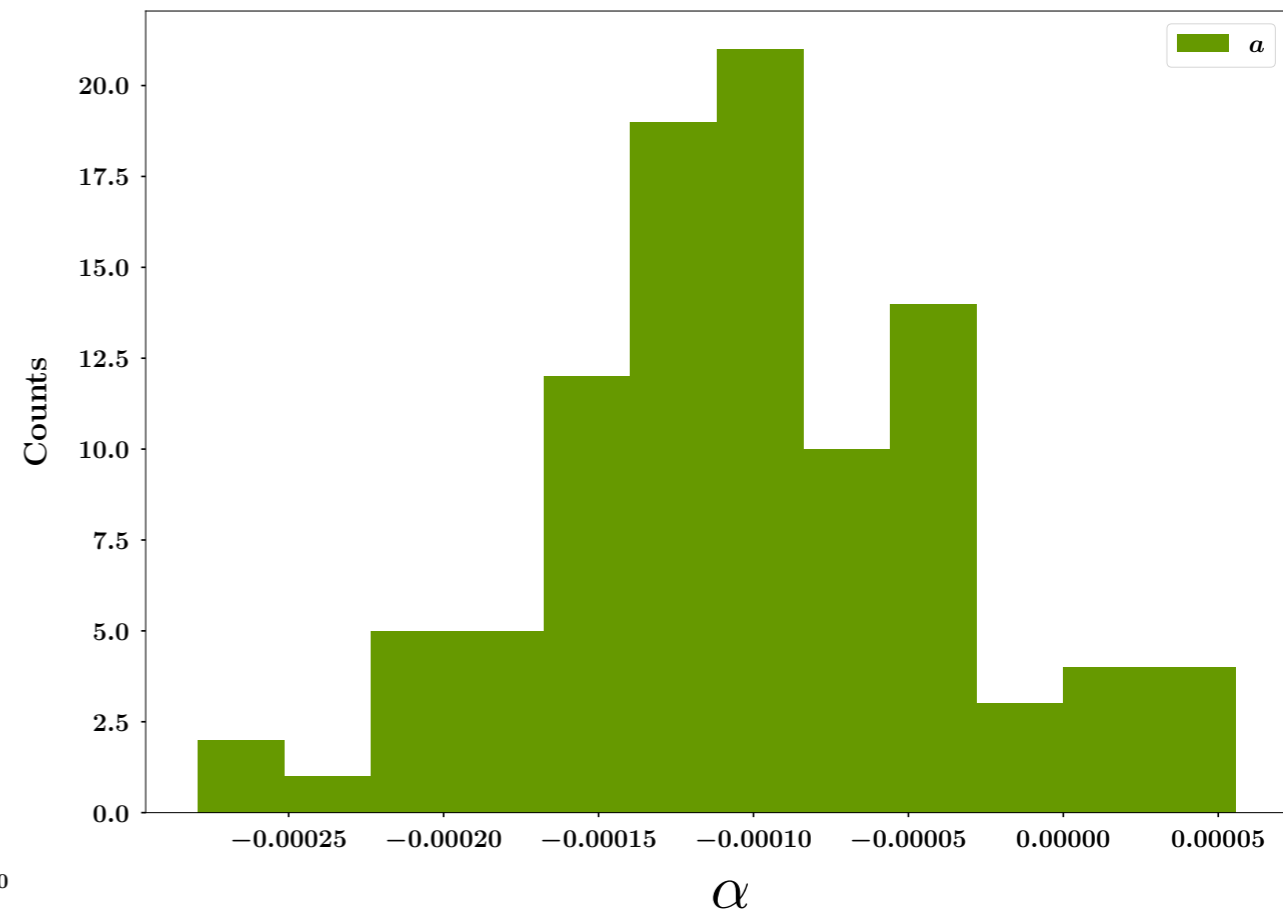
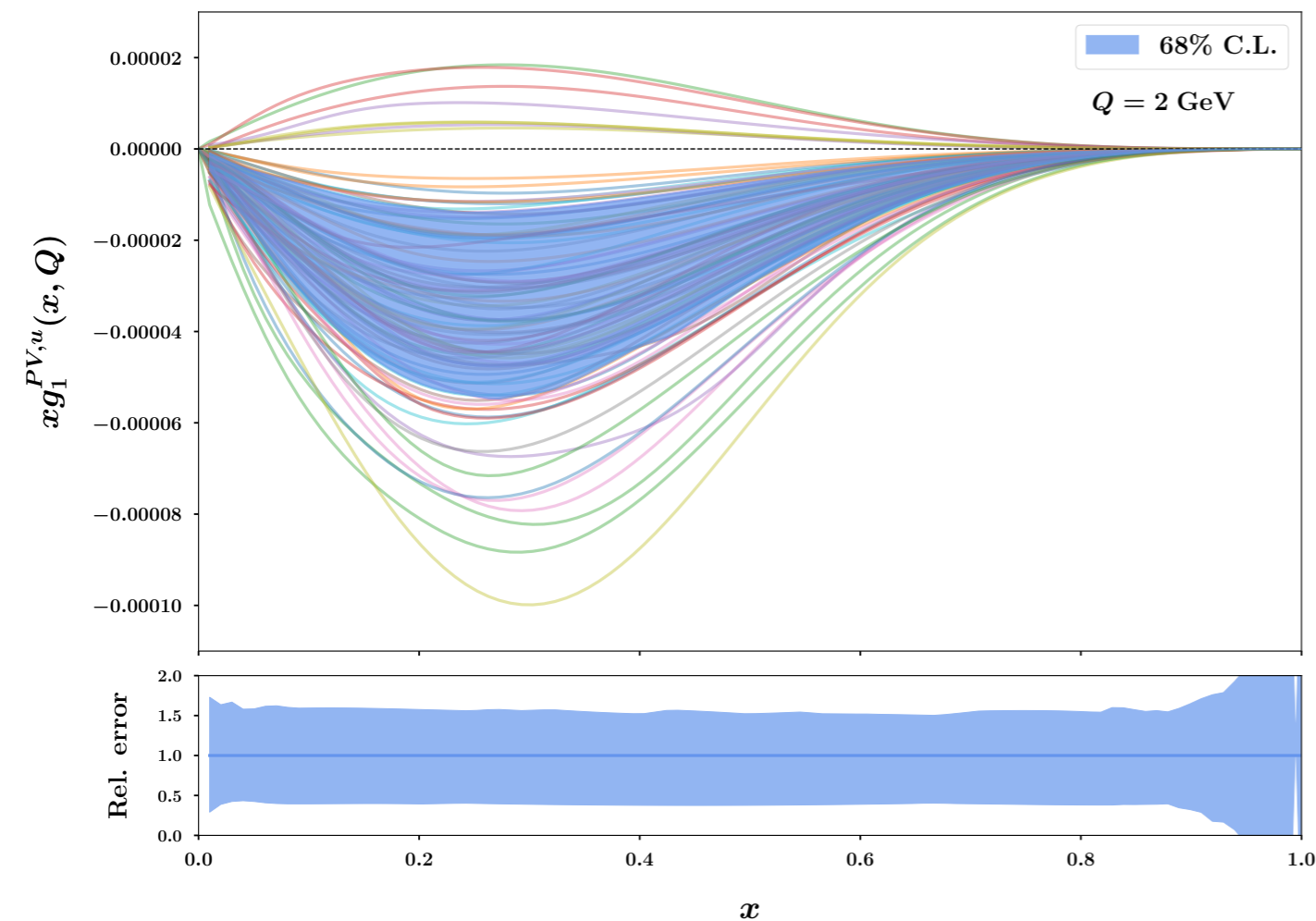
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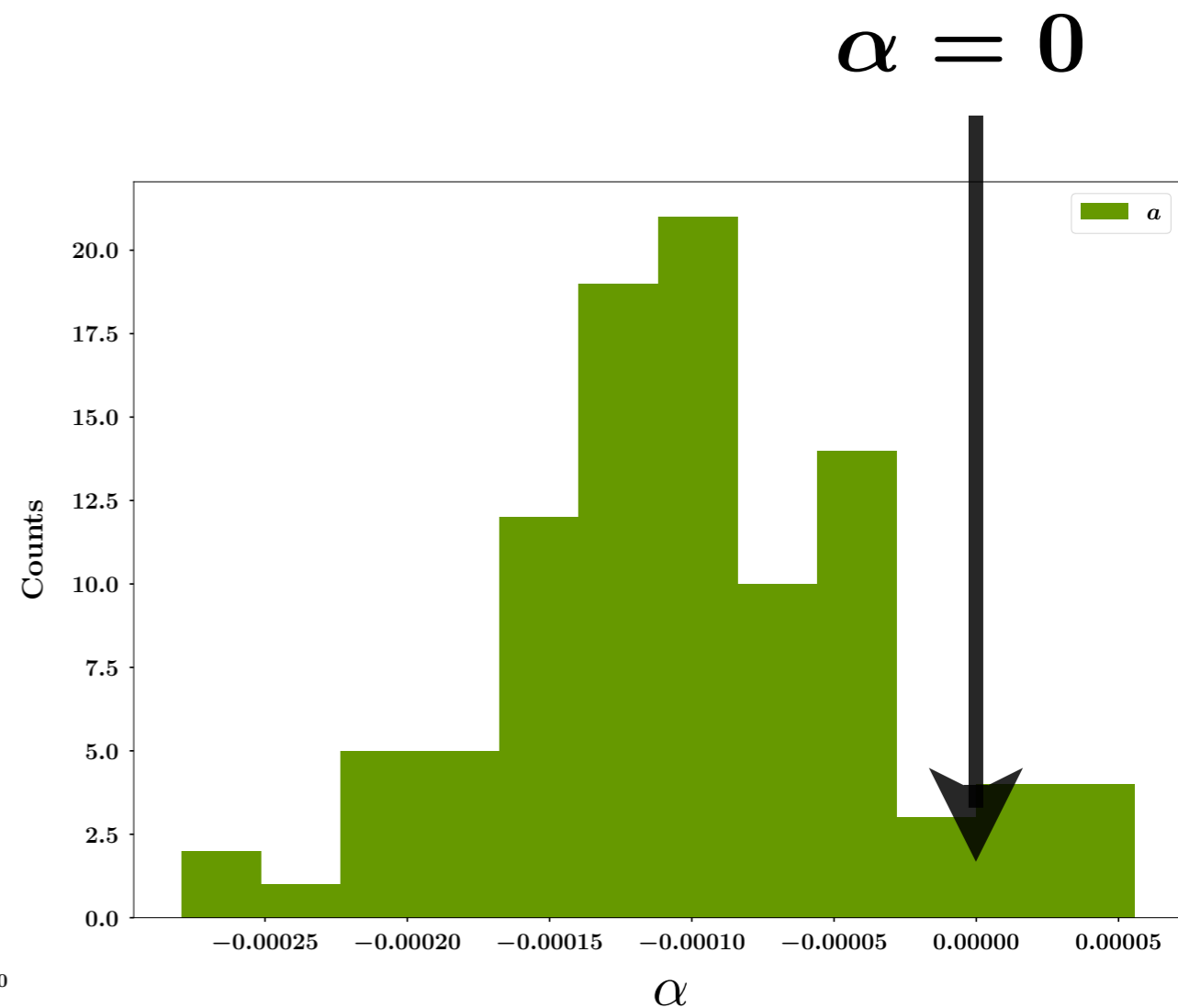
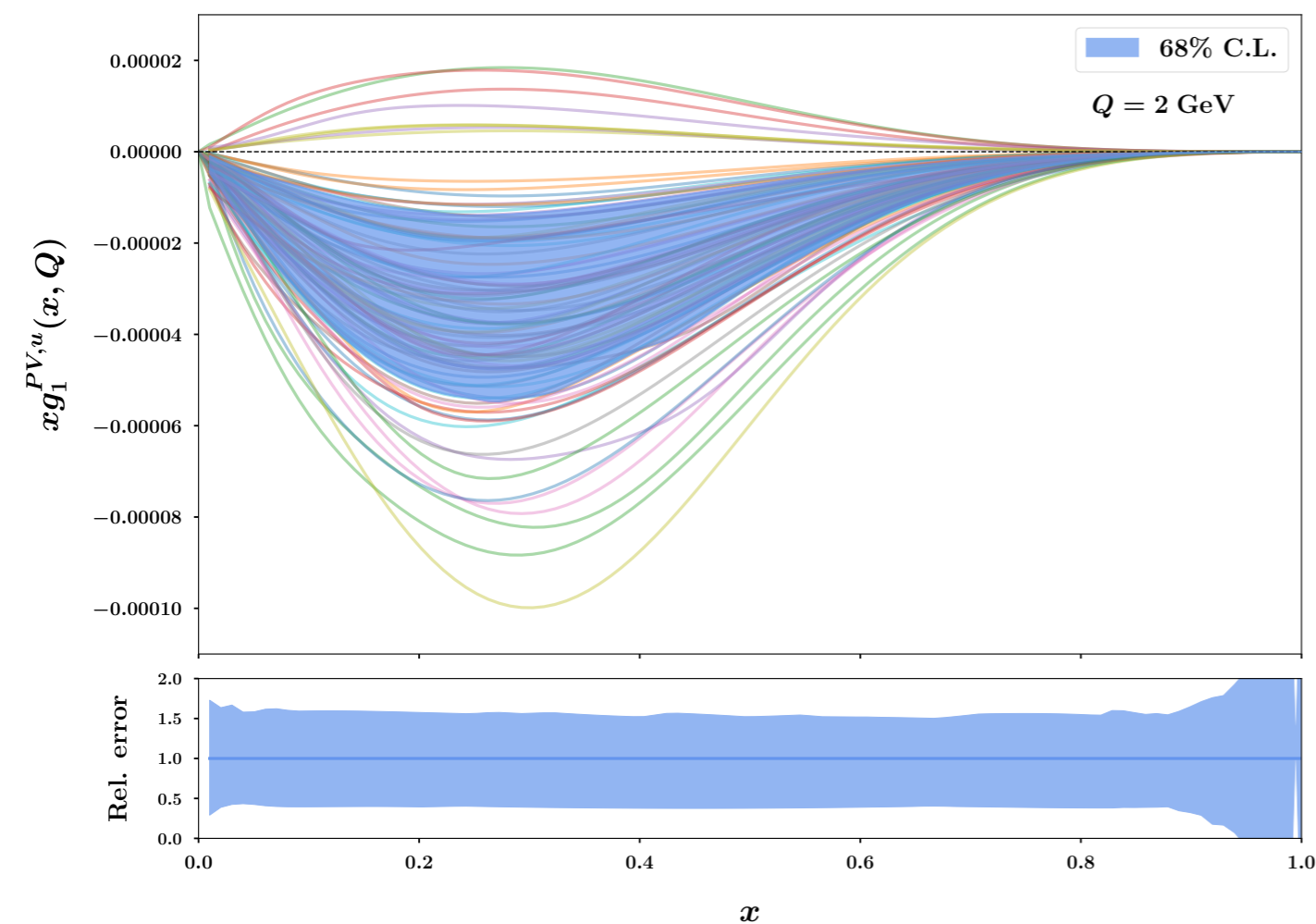
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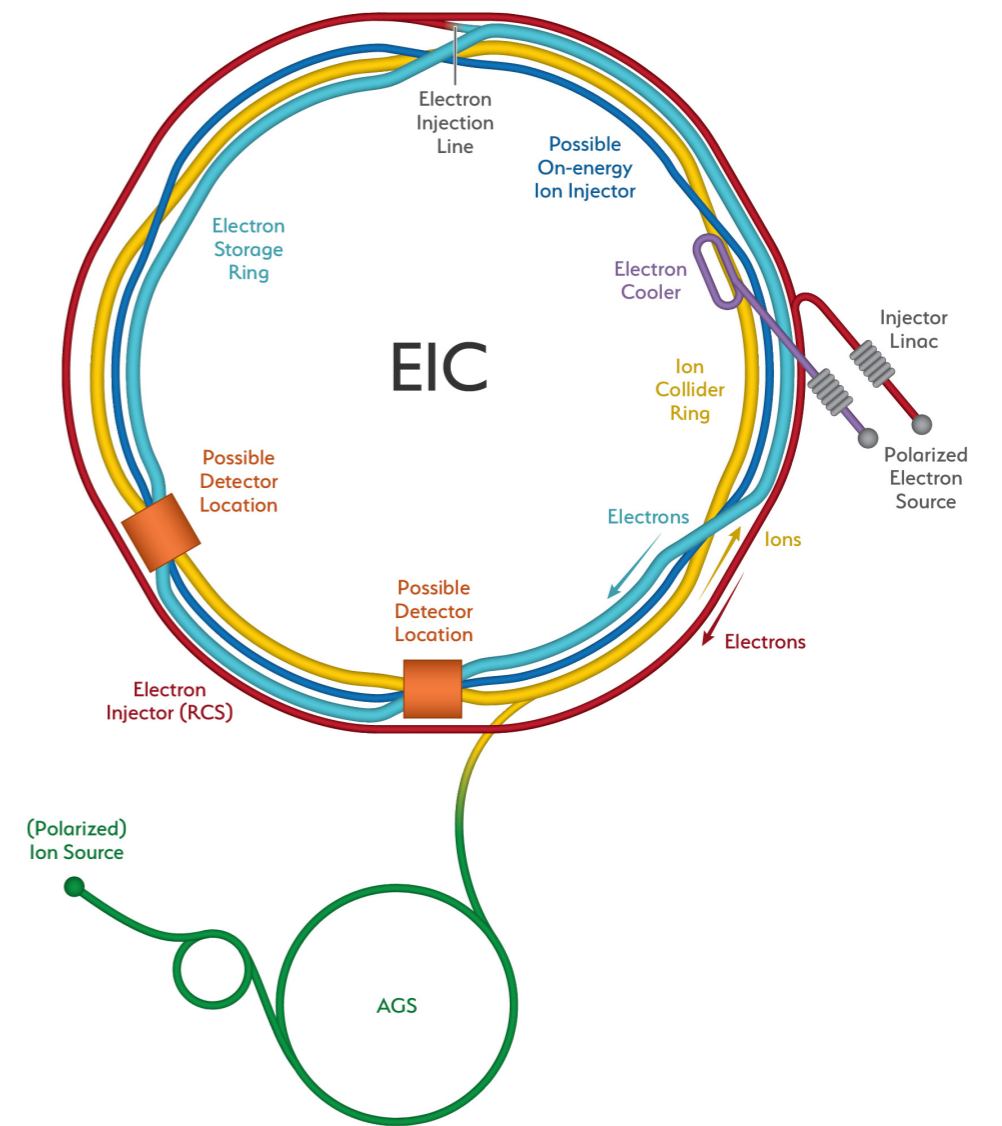
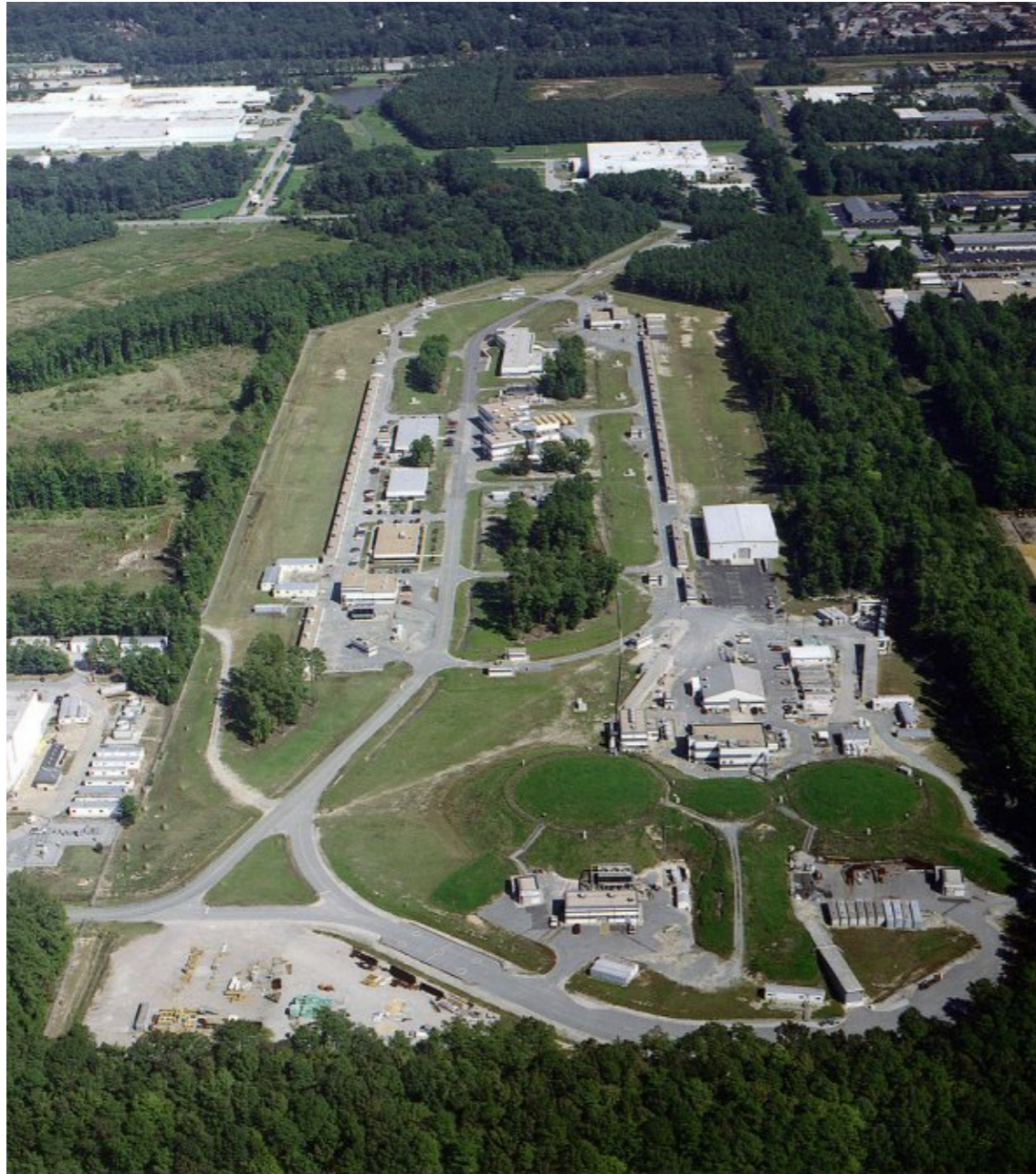
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Future facilities



Impact of future data

Impact of future data

JLab 12 GeV — SoLID detector

Wood, Bennet, Cho, et al., Science 275 (1997)

Souder, Reimer, Zheng, JLab Experiment E12-10-007 (2022 update)

Impact of future data

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Baseline

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$$\alpha = (-1.01 \pm 0.66) \cdot 10^{-4}$$

SoLID (d)

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SoLID (p)

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Impact of future data

JLab 12 GeV — SoLiD detector

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Souder, Reimer, Zheng, JLab Experiment E12-10-007 (2022 update)

Baseline

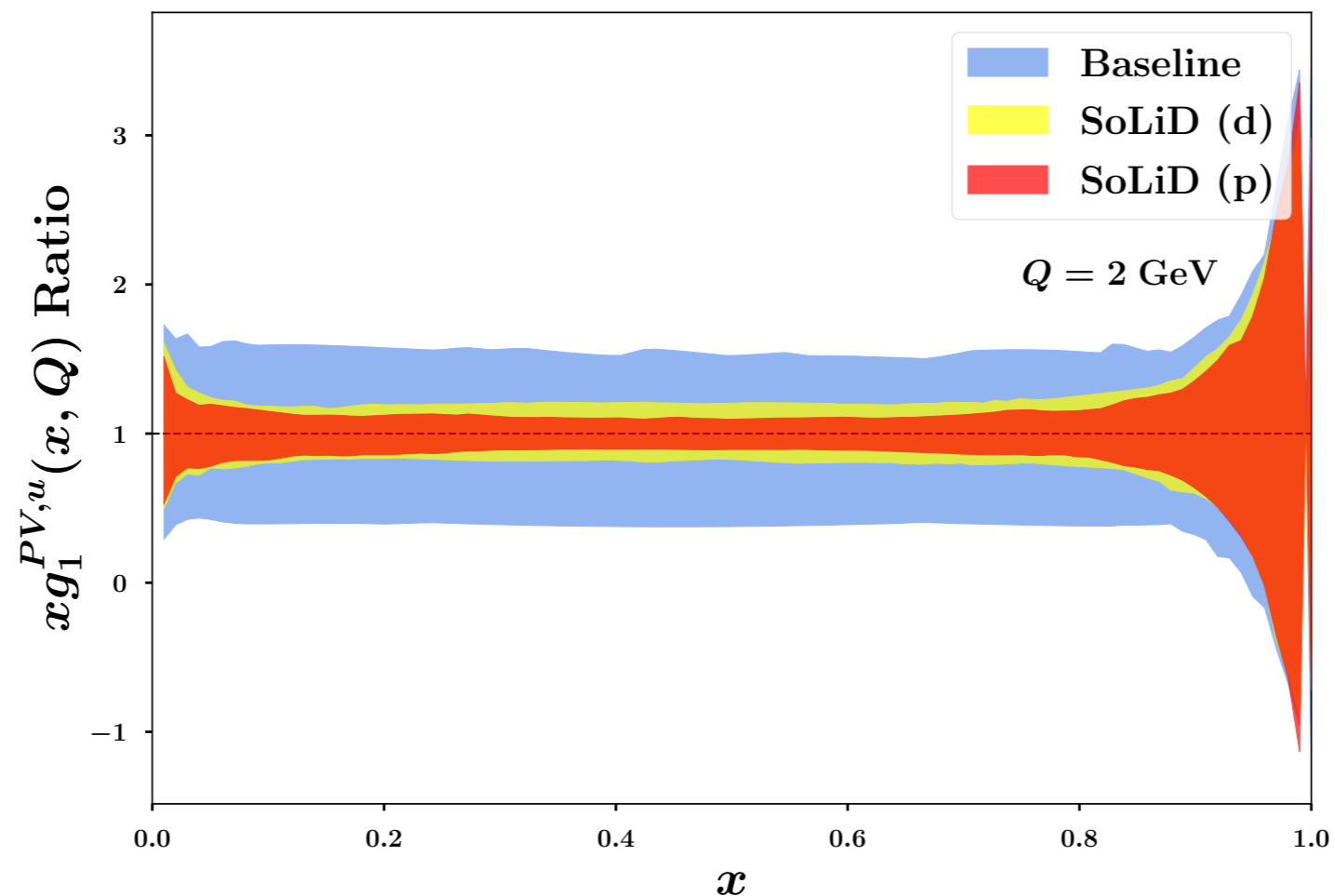
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Step forward: dependence on x

- BSM terms in QCD that may generate PV parton distributions

$$\begin{aligned}\mathcal{L}_{\text{CPV}}^{d \leq 6} &= -\frac{g_s^2}{32\pi^2} \bar{\theta} G \tilde{G}; && d = 4 \text{ QCD } \theta\text{-term} \\ &- \frac{i}{2} \sum_{q=u,d,s} d_q \bar{q} (\sigma \cdot F) \gamma_5 q; && d = 5 \text{ quark EDM} \\ &- \frac{i}{2} \sum_{q=u,d,s} \tilde{d}_q g_s \bar{q} (\sigma \cdot G) \gamma_5 q; && d = 5 \text{ quark chromo EDM} \\ &+ d_w \frac{g_s}{6} G \tilde{G} G; && d = 6 \text{ Weinberg's } 3g \text{ operator} \\ &+ \sum_i C_i^{(4q)} O_i^{(4q)}; && d = 6 \text{ Four-quark operators}\end{aligned}$$

See talk by Y-S Yoo @SPIN23

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+ bunch of SMEFT operators

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Question to F. Petriello

Step forward: dependence on x

Preliminary

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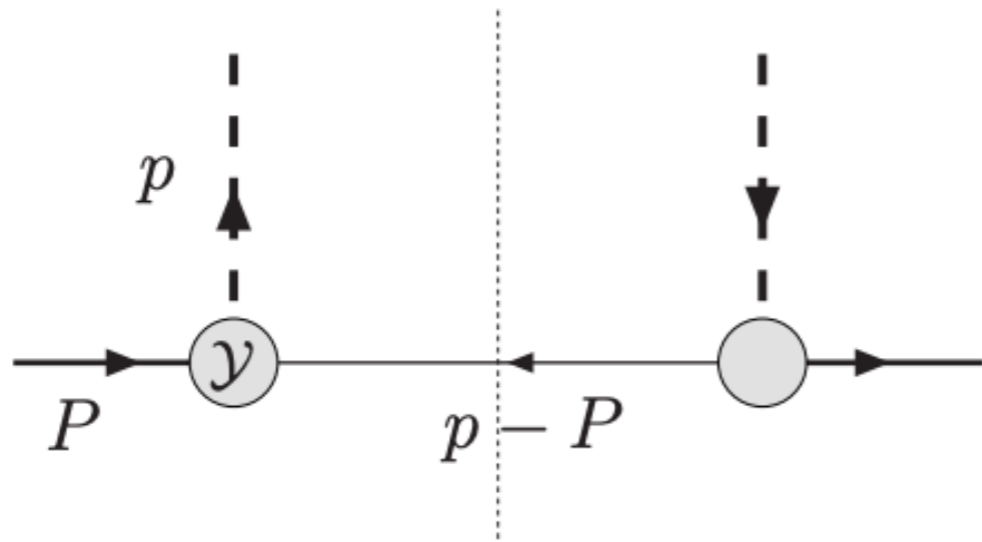
Bacchetta, Conti, Radici, PRD 78 (2008)

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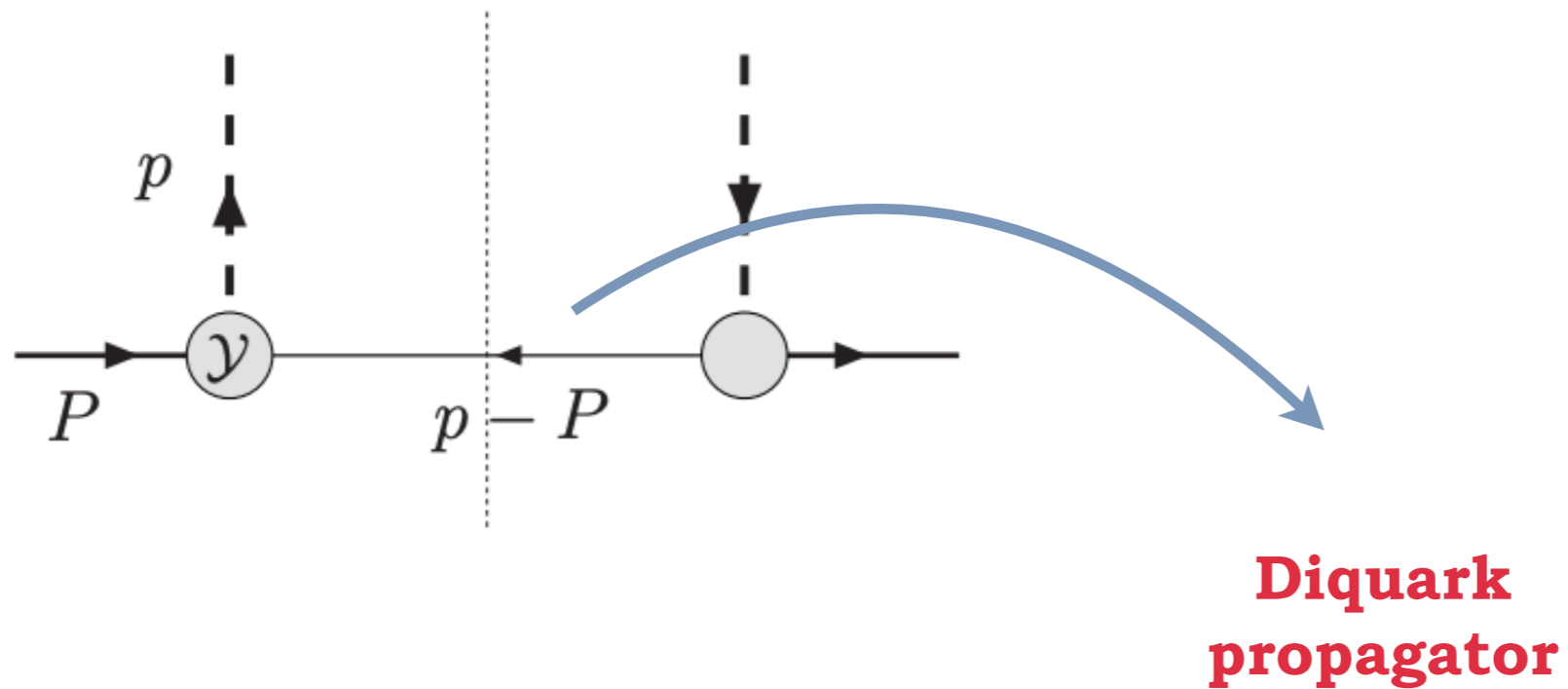


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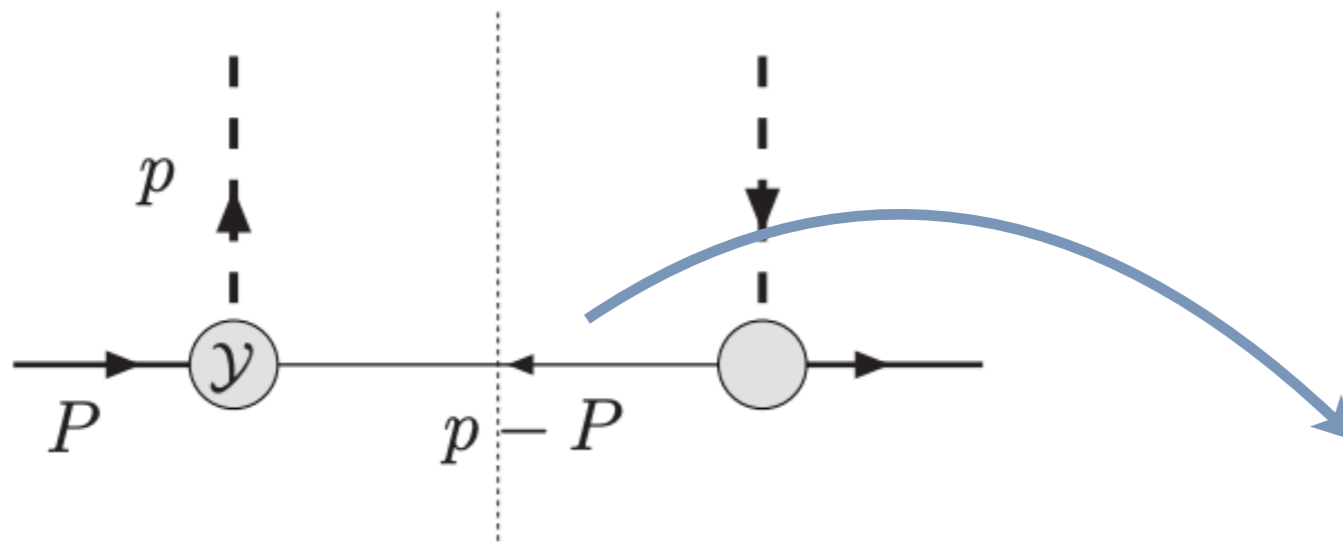


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**Diquark
propagator**

Scalar

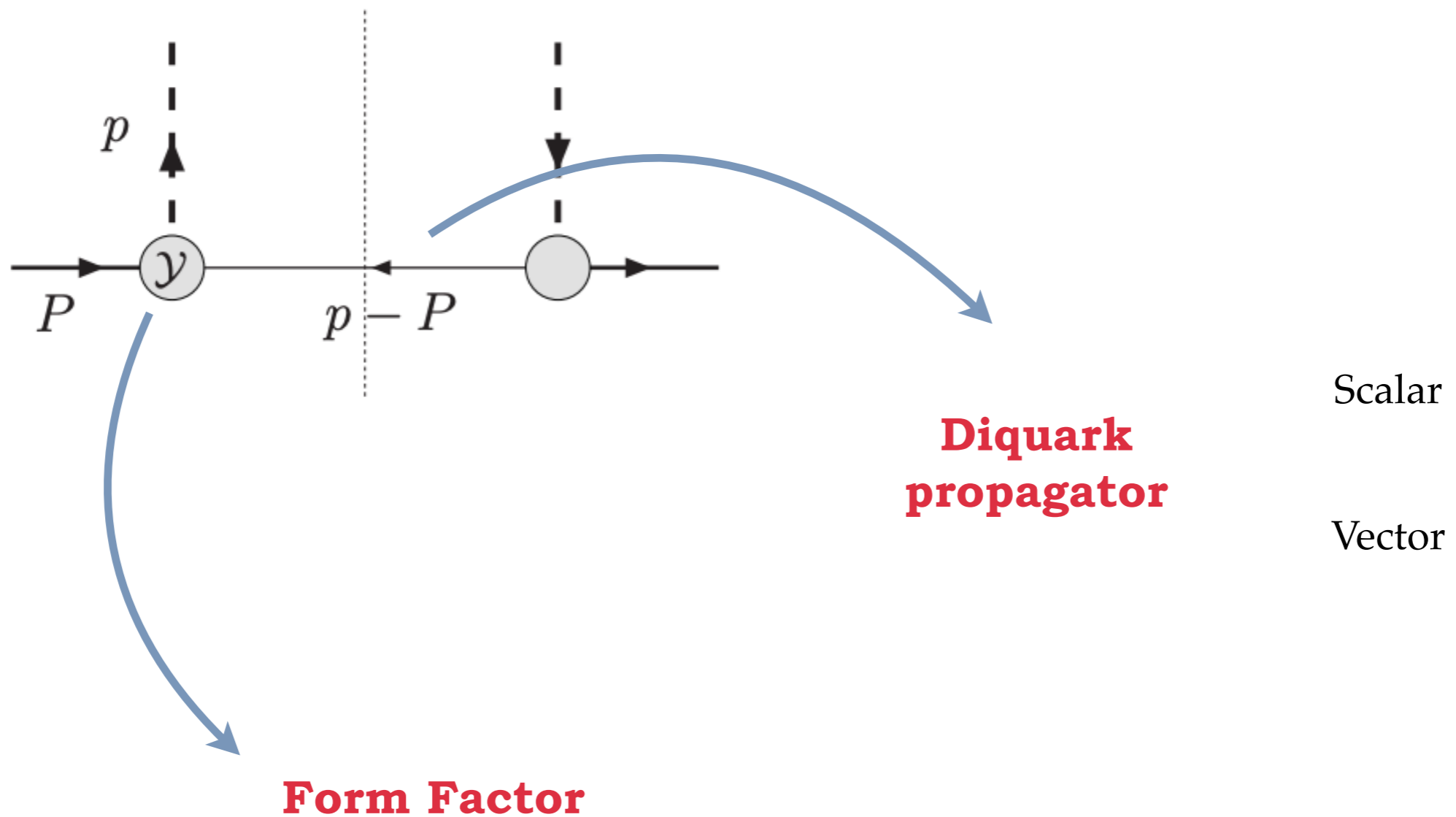
Vector

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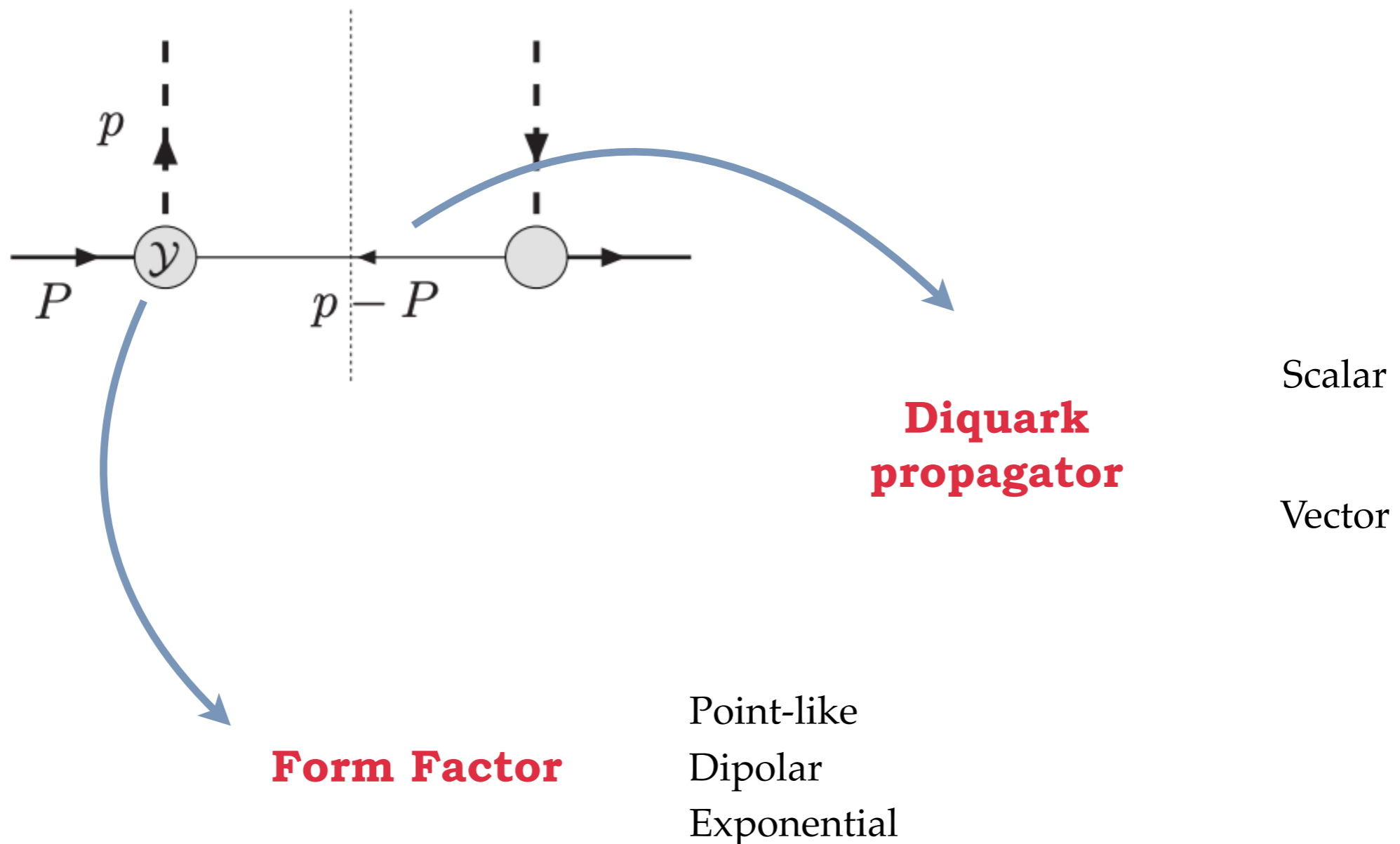


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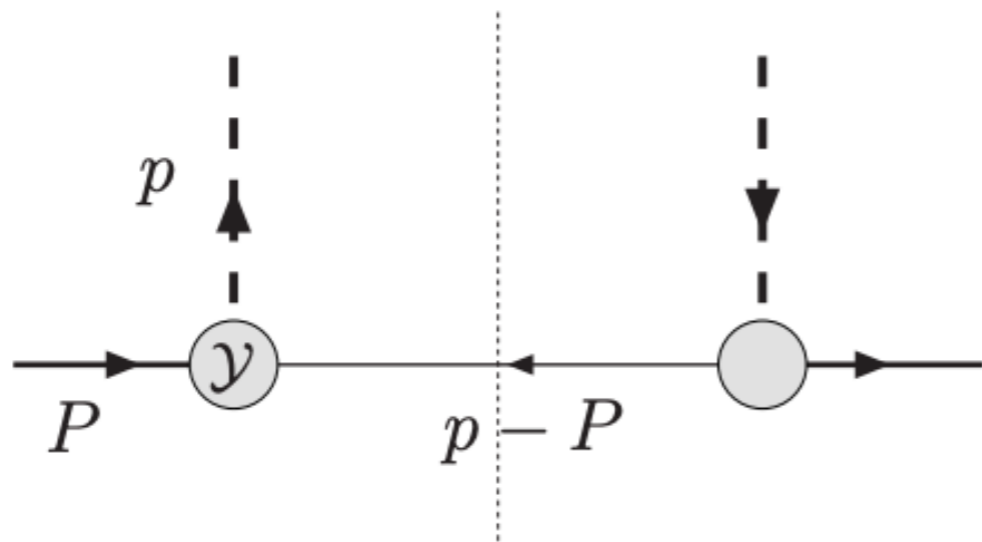


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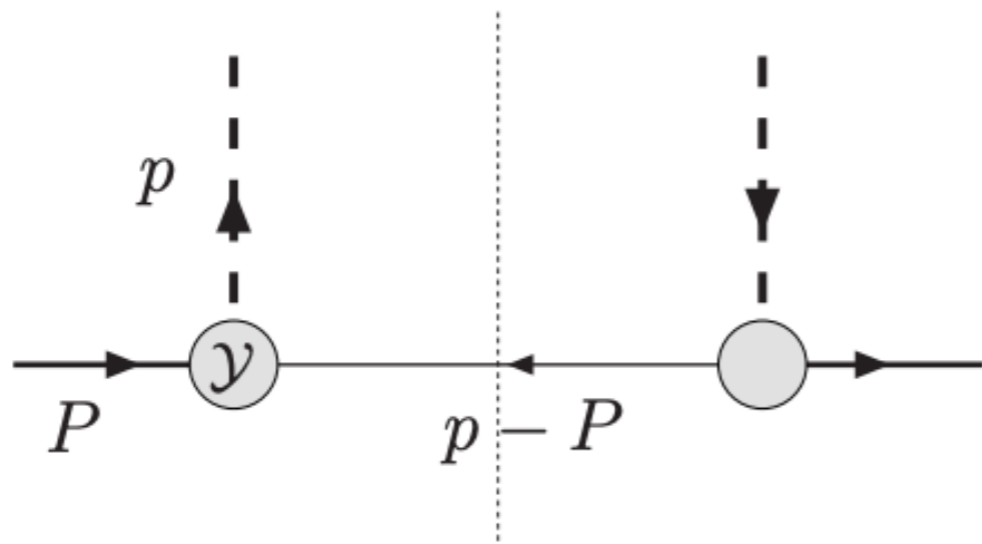


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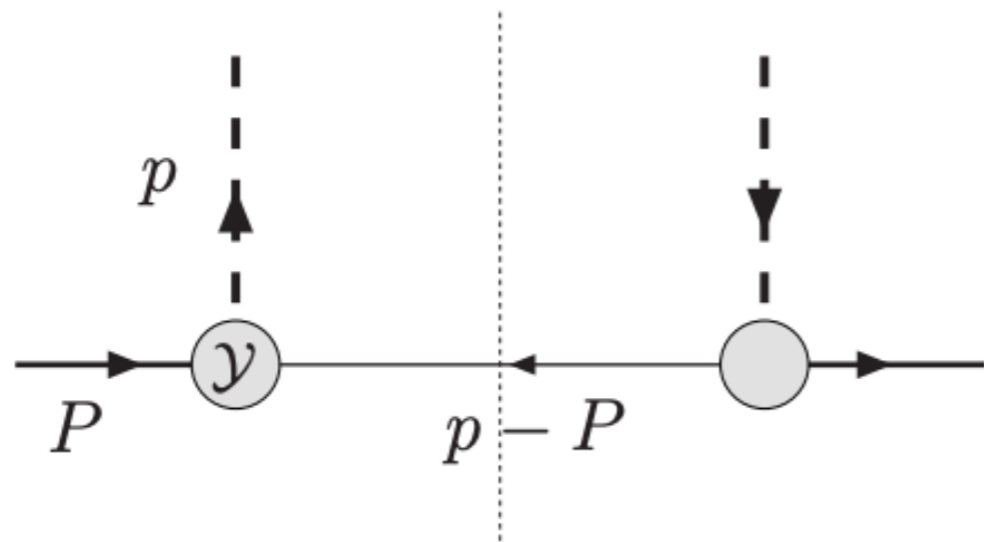
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Diquark propagator

Scalar
Vector

$$\langle P - k | \psi(0) | P, S \rangle = \frac{i}{\not{k} - m} \varepsilon_{\mu}^*(P - k, \lambda_v) \mathcal{Y}_v^{\mu} U(P, S)$$

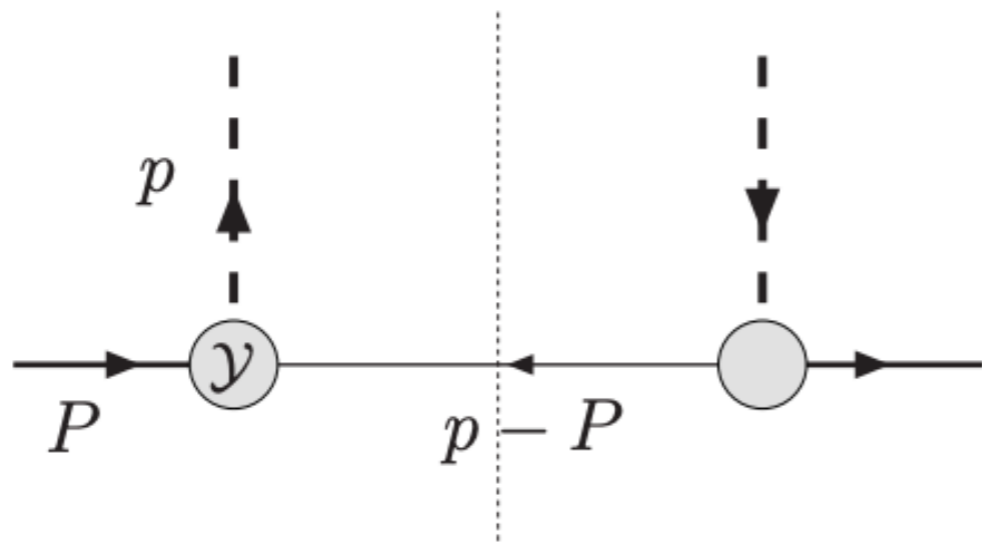
$$\mathcal{Y}_v^{\mu} = i \frac{g_v(k^2)}{\sqrt{2}} \gamma^{\mu} \gamma_5$$

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Diquark propagator

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Form Factor

Dipolar

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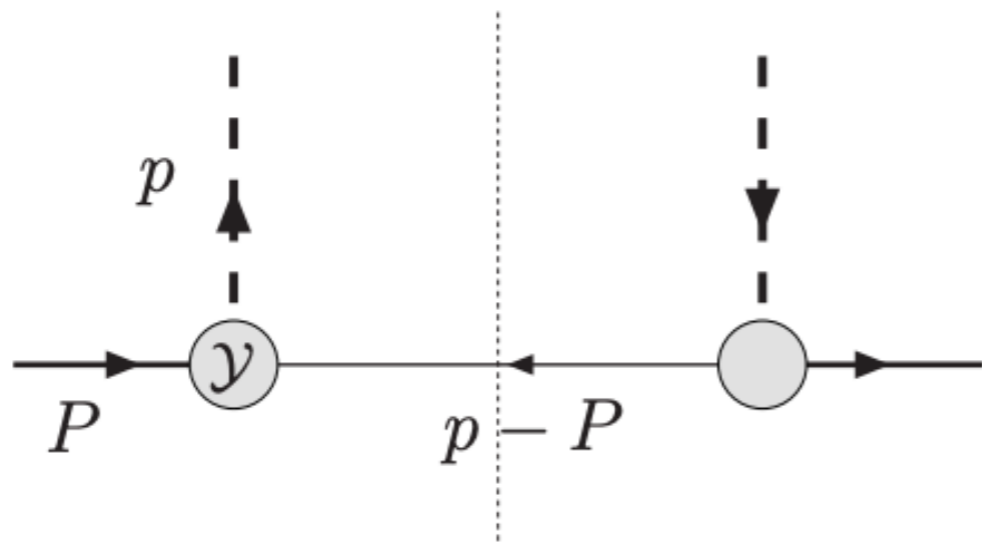
$$g_X(k^2) = g_X^{\text{dip}} \frac{p^2 - m^2}{|p^2 - \Lambda_X^2|^2}$$

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Preliminary

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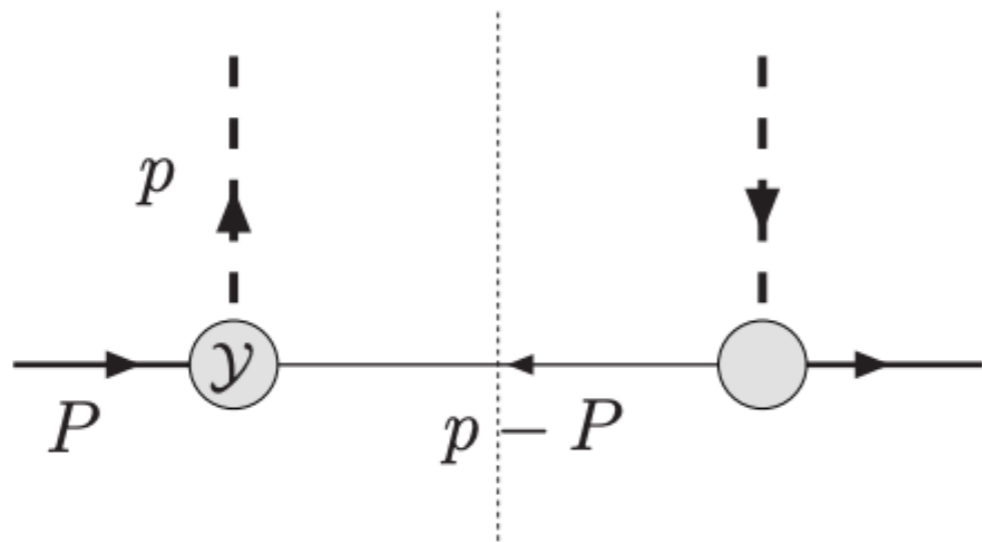
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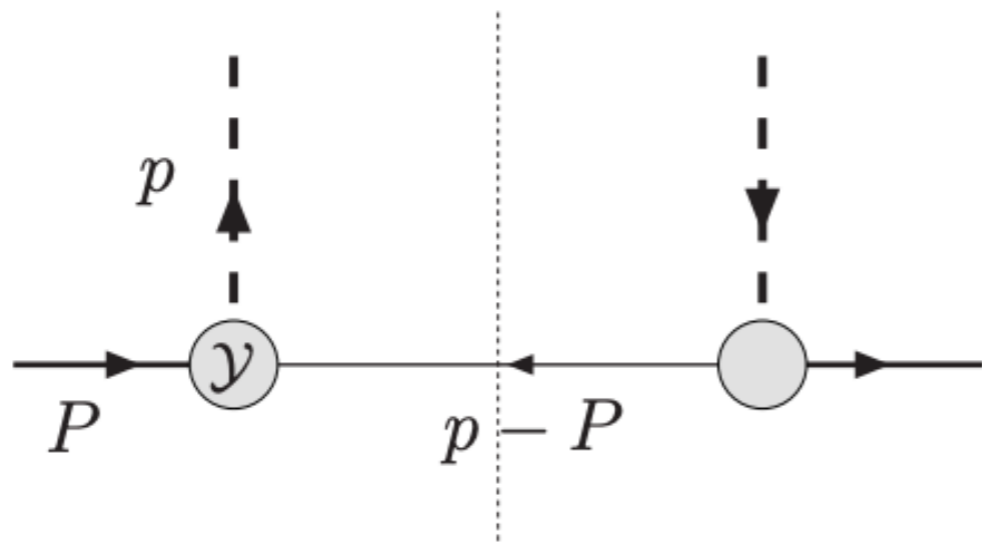
$$\mathcal{Y}_v^{\mu} = i \frac{g_v(k^2)}{\sqrt{2}} \gamma^{\mu} \gamma_5 \quad \xrightarrow{\text{P-violating}} \quad \mathcal{Y}_v^{\mu} = i \frac{g_v(k^2)}{\sqrt{2}} \gamma^{\mu} \gamma_5 (a - b \gamma_5)$$

Step forward: dependence on x

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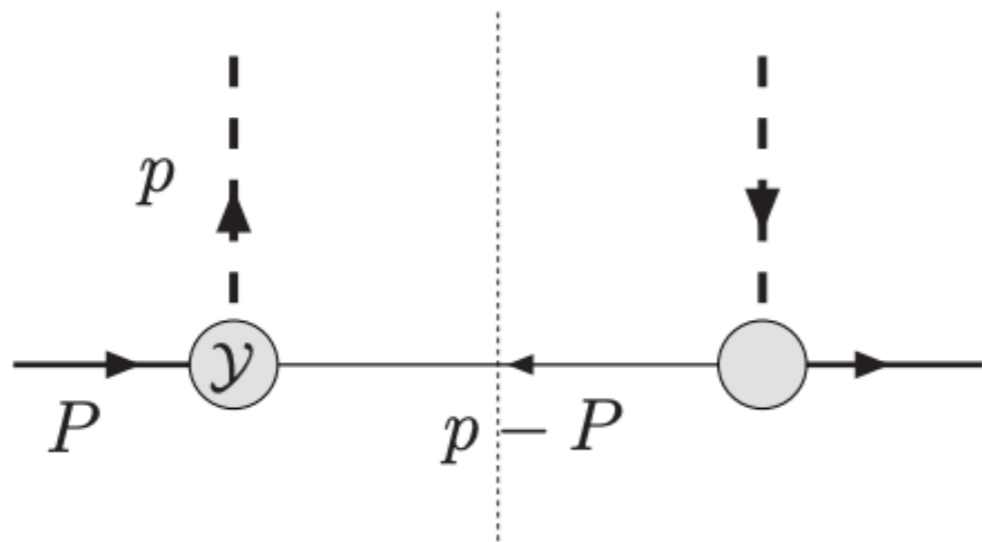


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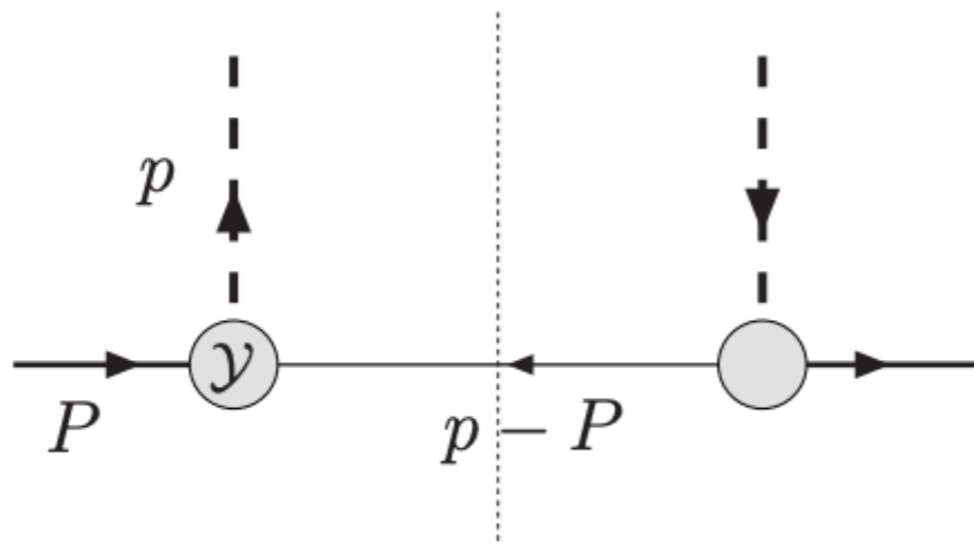
$$\mathcal{Y}_s = ig_s(k^2)(a - b\gamma_5)$$

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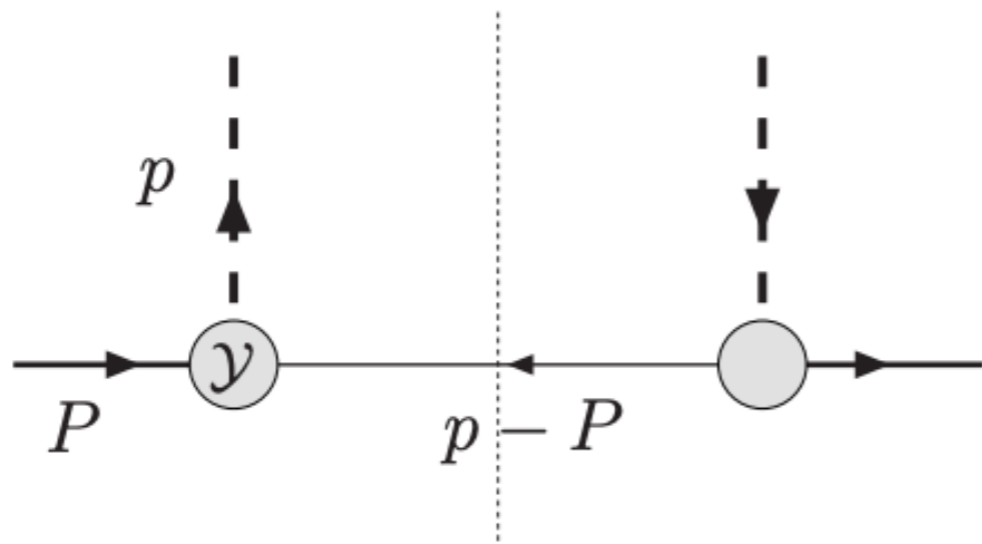
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Step forward: dependence on x

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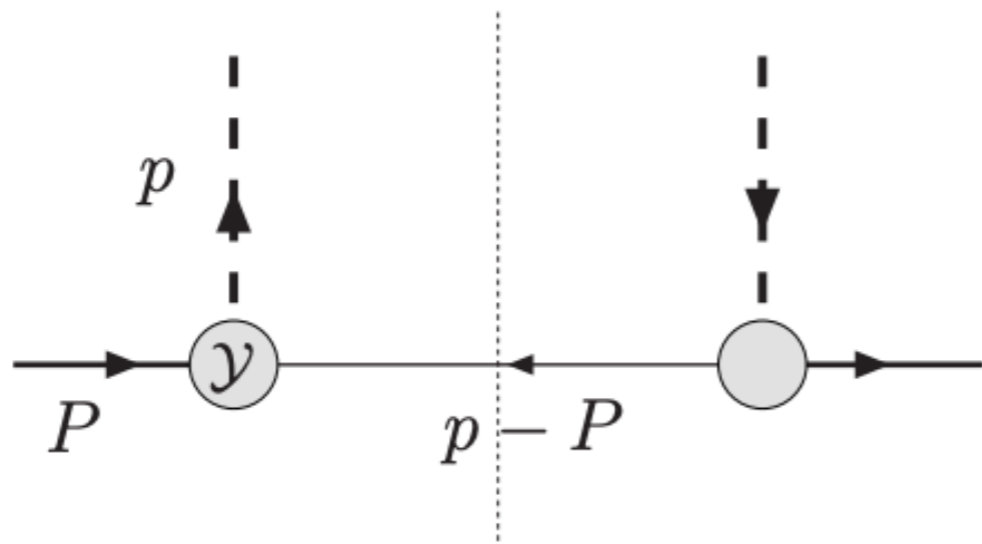
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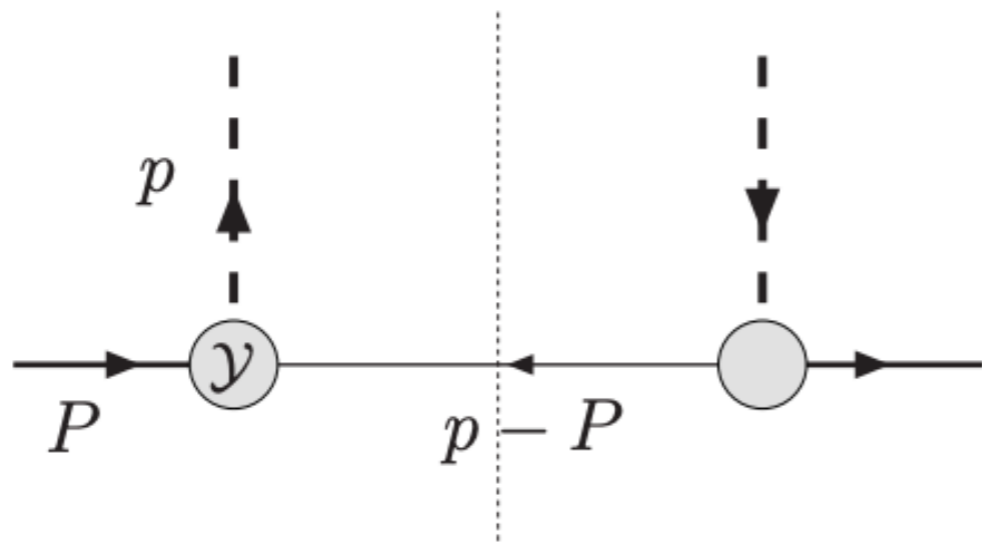
$$g_{1v}^{PV} = -a b_v \frac{(1-x)^2 2((xM)^2 - m^2) + L_v^2(1+x^2)}{48\pi^2 L_v^6}$$

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$$\mathcal{Y}_v^\mu = i \frac{g_v(k^2)}{\sqrt{2}} \gamma^\mu \gamma_5 (a - b\gamma_5)$$

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$$g_{1v}^{PV} = -a b_v \frac{(1-x)^2 2((xM)^2 - m^2) + L_v^2(1+x^2)}{48\pi^2 L_v^6}$$

$$g_{1u}^{PV} = g_s^2 N_s^2 g_{1s}^{PV} + g_v^2 N_v^2 g_{1v}^{PV}$$

Step forward: dependence on x

- Spectator model for PV parton distributions

Next steps:

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- ▶ Fit model parameters to phenomenological extraction

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Step forward: a new CP-odd PDF

- Further investigations on a new P-odd, CP-odd distribution function arising when considering the polarisation of the target

$$\begin{aligned} \Phi^q(x, Q^2) = & \left\{ f_1^q(x, Q^2) + g_1^{\text{PV}q}(x, Q^2)\gamma_5 \right. \\ & + S_L \left(g_1^q(x, Q^2)\gamma_5 + f_{1L}^{\text{PV}q}(x, Q^2) \right) \\ & \left. - \not{S}_T \left(h_1^q(x, Q^2)\gamma_5 - e_{1T}^{\text{PV}q}(x, Q^2) \right) \right\} \frac{\not{n}_+}{2} \end{aligned}$$

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$$\Delta x_B g_5(x_B, Q^2) \approx \Delta x_B g_5^{(\gamma)}(x_B, Q^2) = \frac{1}{2} \sum_q e_q^2 x_B f_{1L}^{\text{PV}(q-\bar{q})}$$

PDFs in DIS processes

Quark Polarization

Nucleon Pol.

	U	L	T
U	$f_1(x)$		
L		$g_1(x)$	
T			$h_1(x)$

PDFs in DIS processes

with P violation

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PDFs in DIS processes

with P violation

Electric charge

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Nucleon Pol.

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L	$f_{1L}^{PV}(x)$	$g_1(x)$	
T			$h_1(x)$

Axial charge

PDFs in DIS processes

with P violation

Electric charge

Quark Polarization

Nucleon Pol.

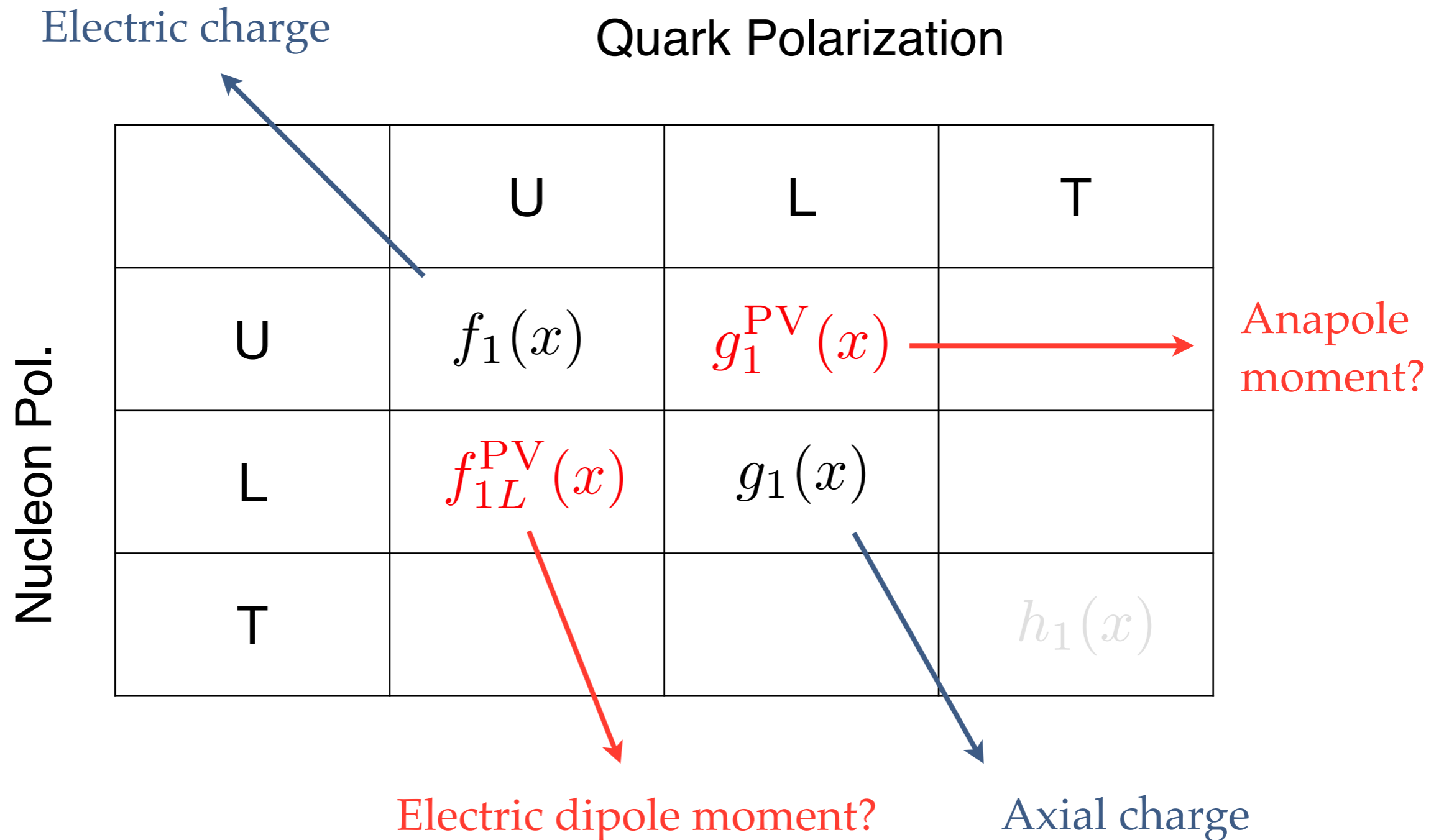
	U	L	T
U	$f_1(x)$	$g_1^{PV}(x)$	
L	$f_{1L}^{PV}(x)$	$g_1(x)$	
T			$h_1(x)$

Anapole moment?

Axial charge

PDFs in DIS processes

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Summary

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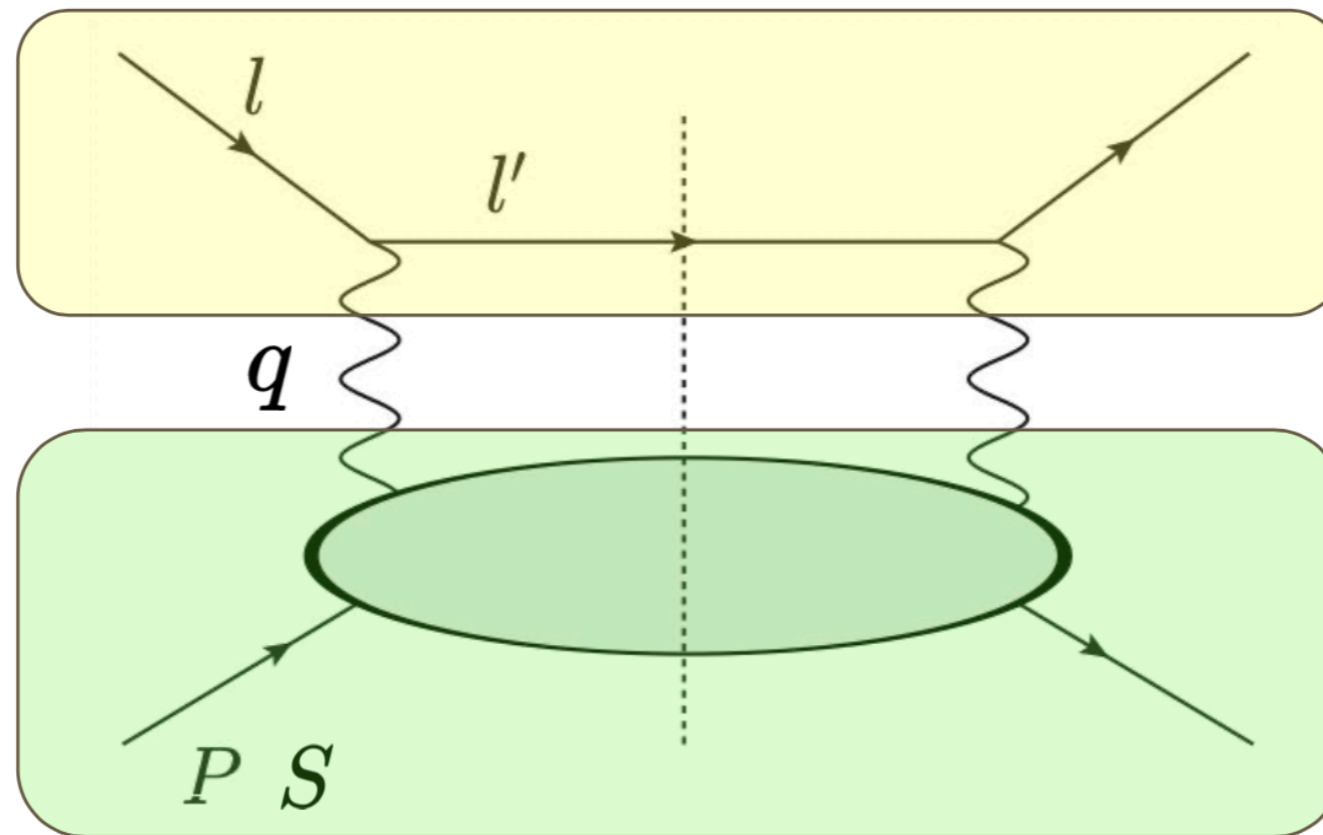
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- In this assumption, a new structure function in DIS cross section for one-photon exchange is generated
- A fit of present experimental data is compatible with a non-zero contribution from a new strong PV parton density
- Improvements in the theoretical framework of our analysis are surely needed to obtain more and more accurate results

Backup

DIS Cross Section

$$\frac{d^3\sigma}{dx_B dy d\phi_S} = \frac{\alpha^2 y}{2Q^4} L_{\mu\nu}(l, l', \lambda_e) 2MW^{\mu\nu}(q, P, S)$$

Leptonic tensor - QED
(completely calculable)



Hadronic tensor - QCD
(NOT completely calculable)

J. Collins, "Foundation of Perturbative QCD"

Hadronic Tensor (unpolarized)

$$2MW_{\mu\nu}(q, P) = \sum_X \int \frac{d^3 P_X}{2E_X} \delta^4(P + q - P_X) \langle P | J_\mu^\dagger(0) | P_X \rangle \langle P_X | J_\nu(0) | P \rangle$$

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Dominant contribution on the Light-Cone

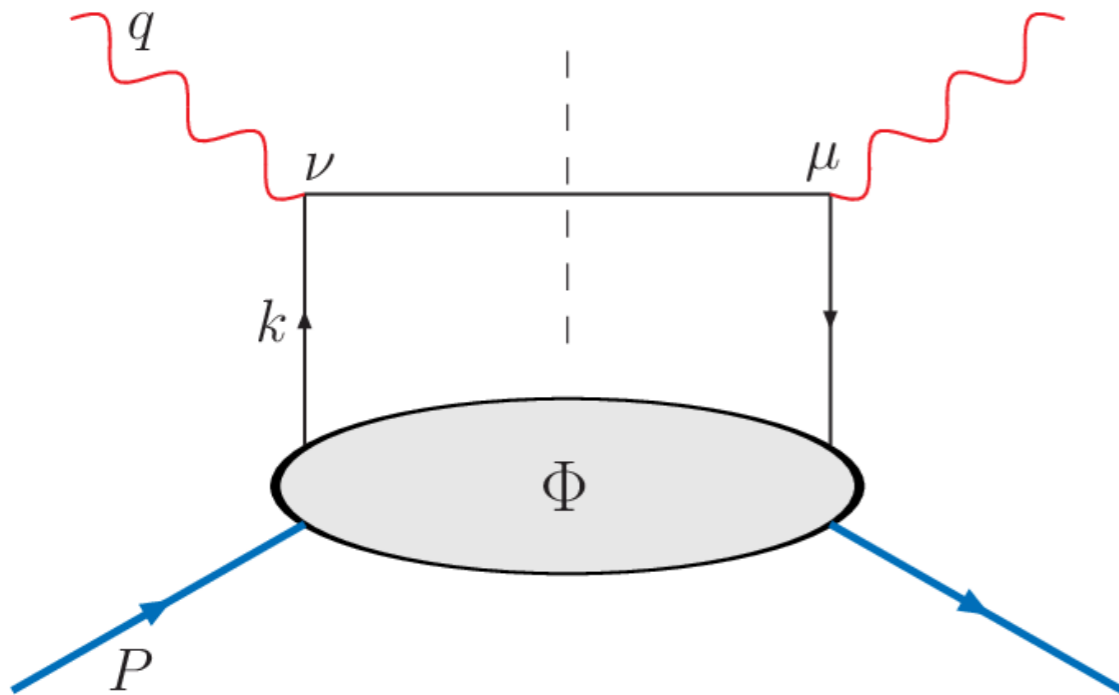
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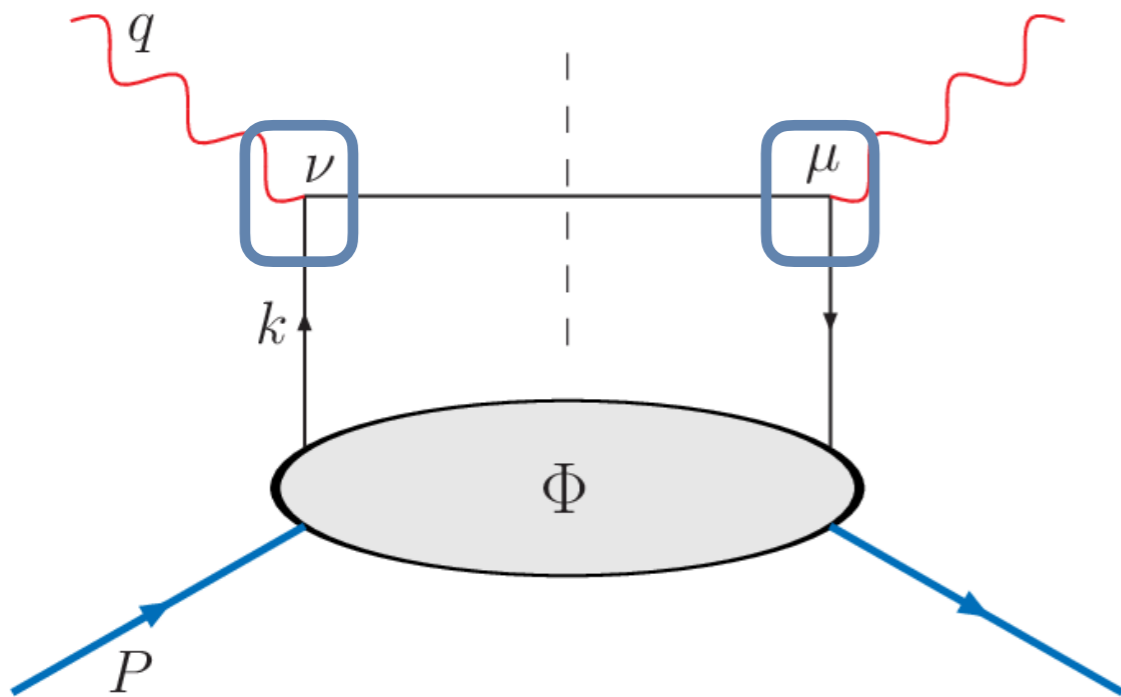
$$2MW^{\mu\nu}(q, P, S) = \sum_q e_q^2 \frac{1}{2} \text{Tr} [\Phi(q, P, S) \Gamma^\mu \gamma^+ \Gamma^\nu]$$

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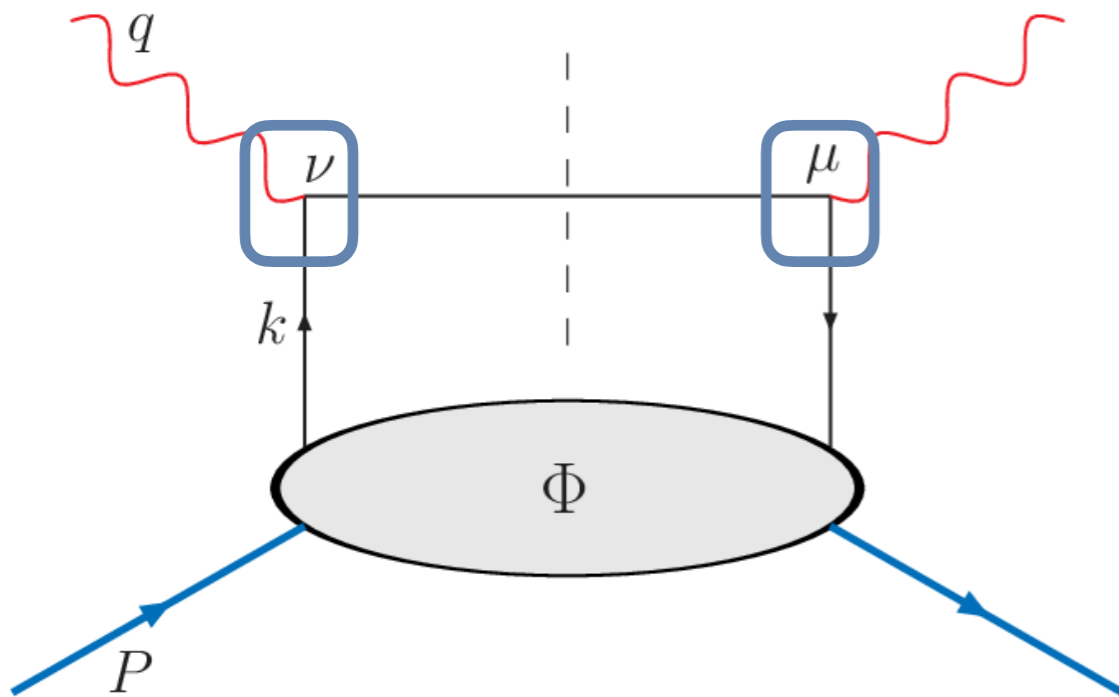
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Vertices of the interactions

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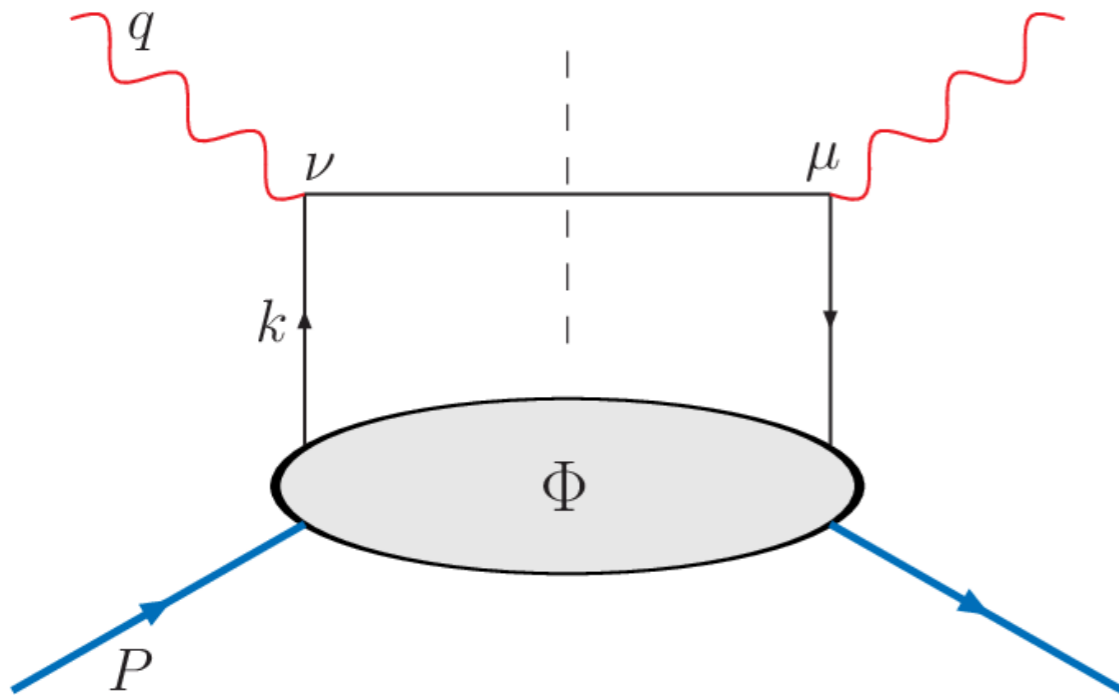


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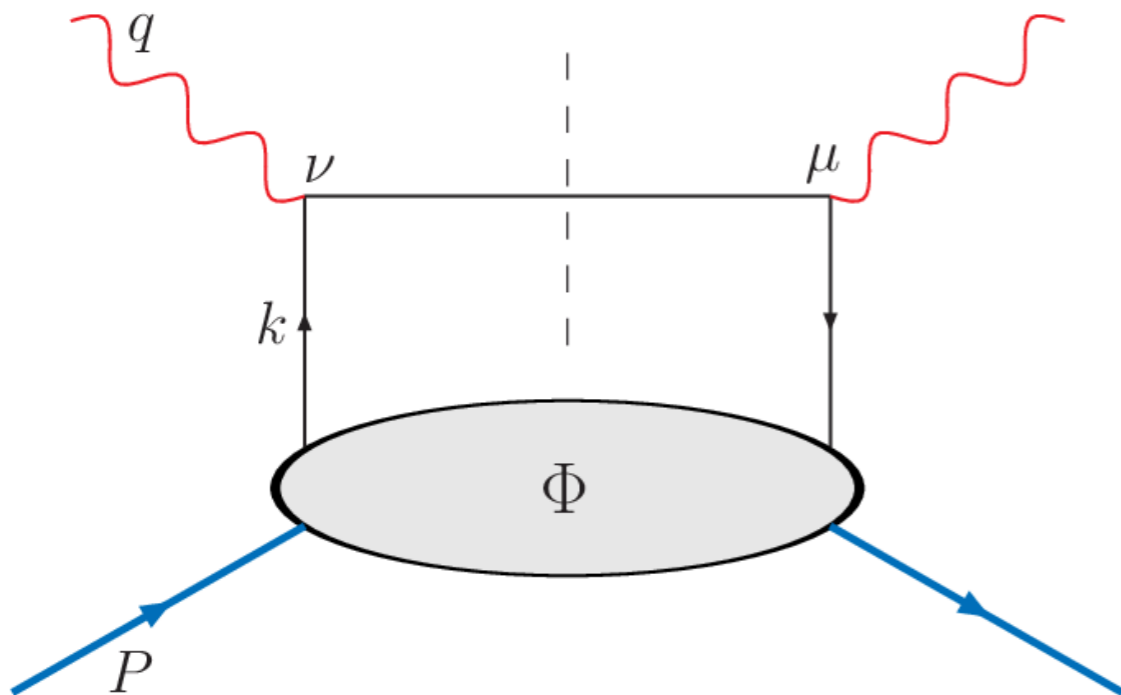


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Correlation distribution function

Hadronic Tensor (unpolarized)



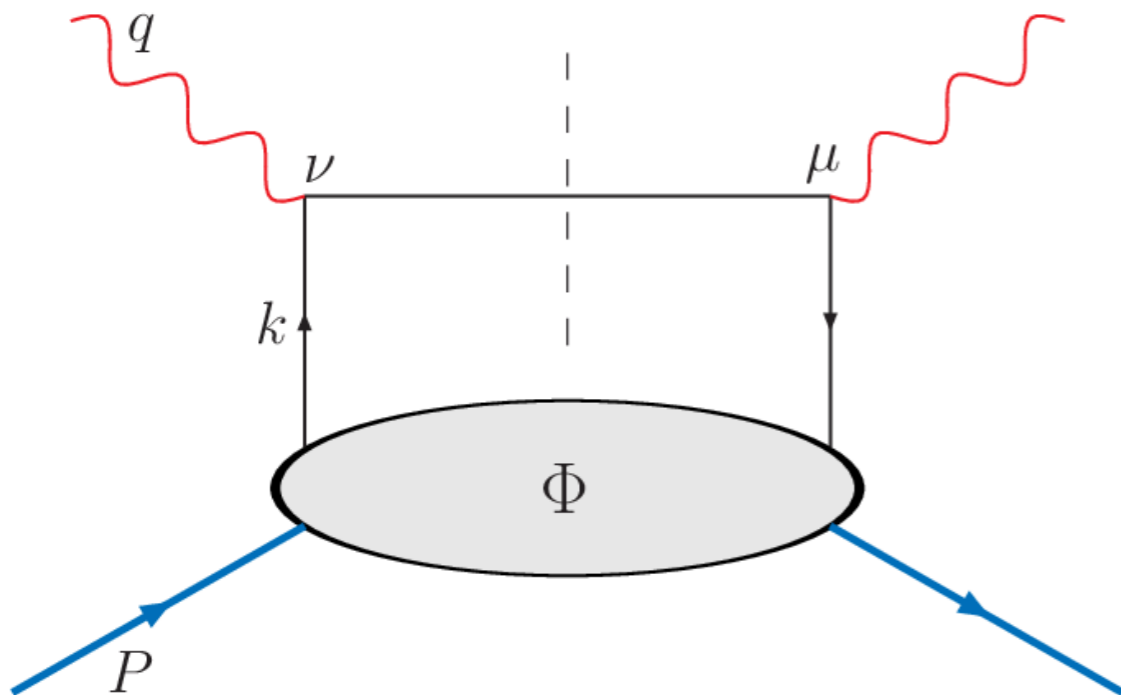
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Decomposition in partonic densities

J. Collins, "Foundation of Perturbative QCD"

M. Anselmino et al., Z. Phys. C 64, 267 (1997)

Neutral-Current DIS

$$\frac{d\sigma^\pm}{dx dy} = \frac{2\pi\alpha^2}{xyQ^2} \left[\begin{aligned} & \left(Y_+ + \gamma^2 y^2 / 2 \right) (F_{2UU} + \lambda F_{2LU}^\pm) \\ & - y^2 (F_{L,UU} + \lambda F_{L,LU}^\pm) \\ & - \frac{Y_-}{\sqrt{1 + \gamma^2}} (x F_{3UU}^\pm + \lambda x F_{3LU}^\pm) \end{aligned} \right]$$

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$$F_{2LU}^\pm(x, Q^2) = \mp g_A^e \eta_{\gamma Z} F_2^{(\gamma Z)} \pm 2g_V^e g_A^e \eta_Z F_2^{(Z)},$$

$$x F_{3UU}^\pm(x, Q^2) = \mp g_A^e \eta_{\gamma Z} x F_3^{(\gamma Z)} \pm 2g_V^e g_A^e \eta_Z x F_3^{(Z)},$$

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$$\begin{aligned} C_{1u}^{\text{SM}} &= -0.1887 - 0.0011 \times \frac{2}{3} \ln(\langle Q^2 \rangle / 0.14 \text{ GeV}^2) \\ C_{1d}^{\text{SM}} &= 0.3419 - 0.0011 \times \frac{-1}{3} \ln(\langle Q^2 \rangle / 0.14 \text{ GeV}^2) \\ C_{2u}^{\text{SM}} &= -0.0351 - 0.0009 \ln(\langle Q^2 \rangle / 0.078 \text{ GeV}^2) \\ C_{2d}^{\text{SM}} &= 0.0248 + 0.0007 \ln(\langle Q^2 \rangle / 0.021 \text{ GeV}^2) \end{aligned}$$

Impact of future data

Electron-Ion Collider (EIC)

Abdul Khalek, et al., Nucl. Phys. A 1026 (2022)

Boughezal, Emmert, Kutz, et al., PRD 106 (2022)

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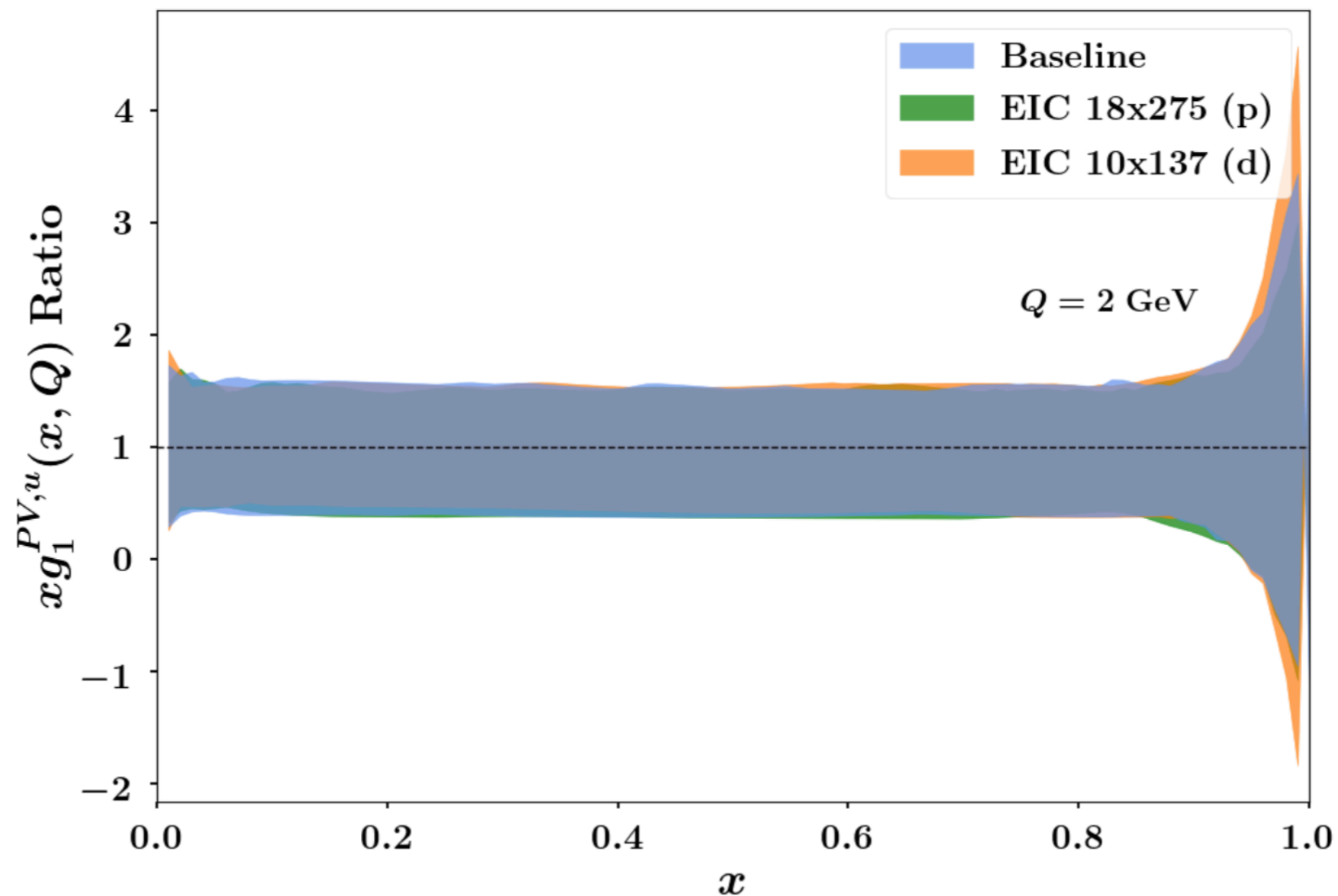
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