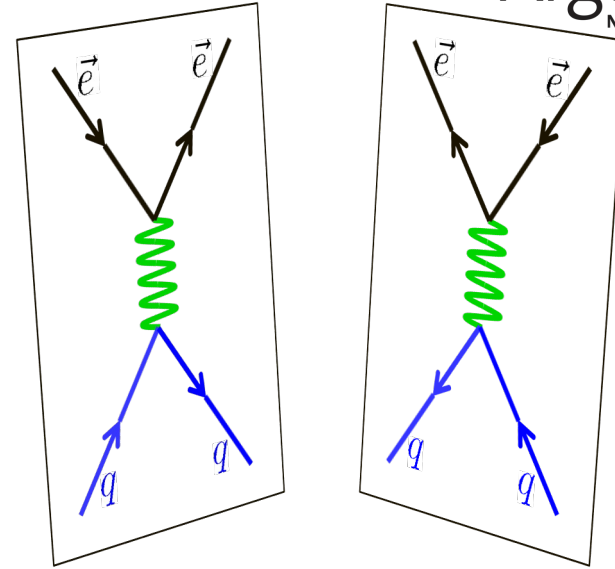


# PARTON DISTRIBUTIONS AND PVDIS IN SOLID



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19 June 2024

Argonne National Laboratory  
Lemont, IL

The question is not about parton distribution uncertainties in 2024, but rather what these uncertainties will be in 203x.

# PVDIS MEASUREMENT

$$\sigma^l \propto |\mathcal{M}_\gamma + \mathcal{M}_{PV}^l|^2 \quad \sigma^r \propto |\mathcal{M}_\gamma + \mathcal{M}_{PV}^r|^2$$

$$A_{LR}^{PV} = \frac{\sigma^l - \sigma^r}{\sigma^l + \sigma^r} \approx \frac{\mathcal{M}_{PV}^l - \mathcal{M}_{PV}^r}{\mathcal{M}_\gamma}$$

$$\approx - \left( \frac{3G_F Q^2}{2\sqrt{2}\pi\alpha} \right) \frac{2C_{1u} - C_{1d} (1 + R_s) + Y (2C_{2u} - C_{2d}) R_v}{5 + R_s}$$

$$R_s(x) = 2 \frac{s(x) + \bar{s}(x)}{u(x) + d(x)} \xrightarrow{x \rightarrow 11} 0$$

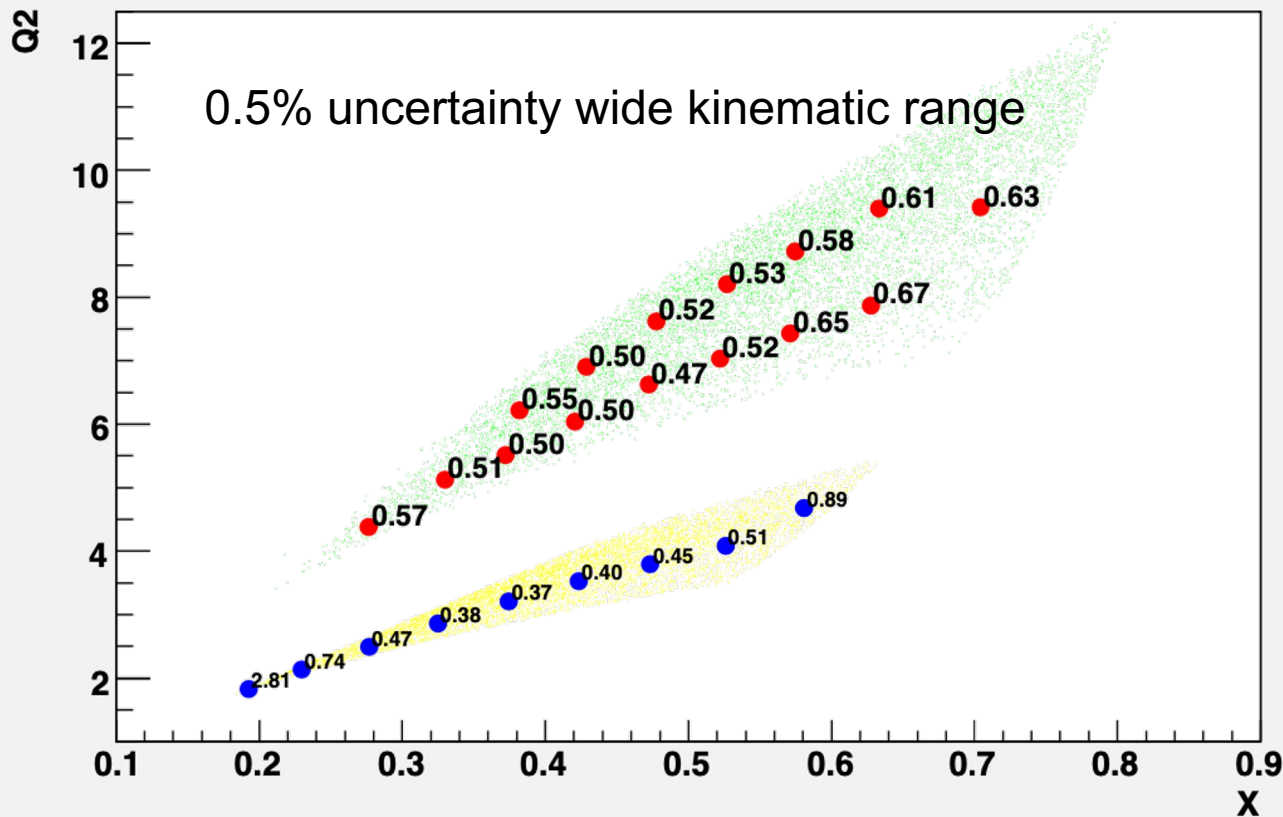
$$R_v(x) = \frac{u_v(x) + d_v(x)}{u(x) + d(x)} \xrightarrow{x \rightarrow 1} 1$$

Half full or  
half empty

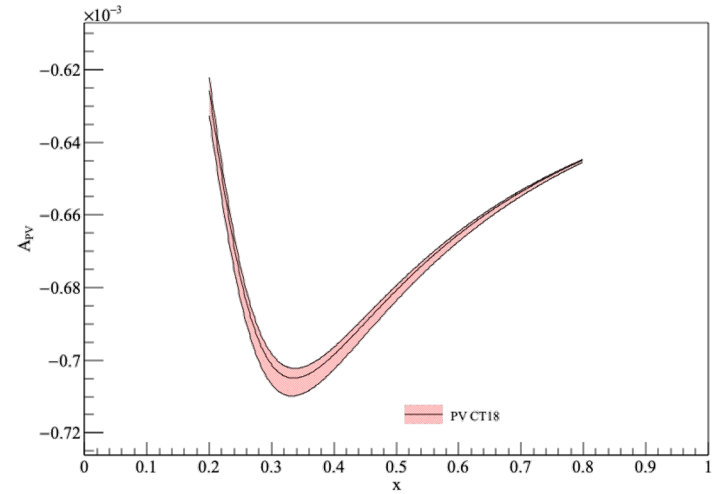
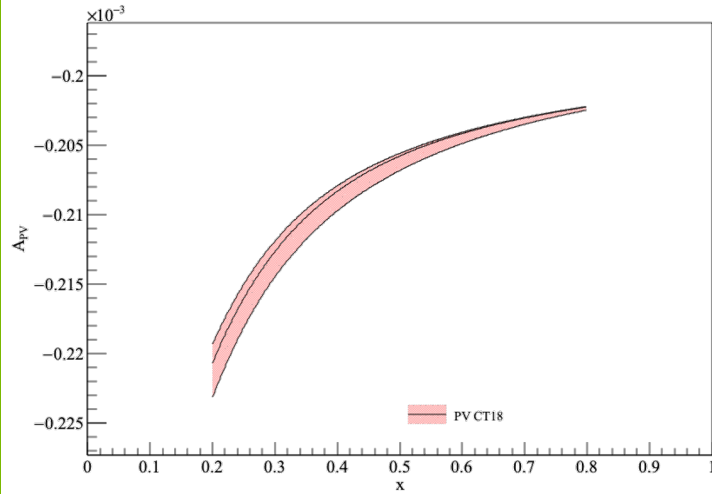


# SOLID PVDIS ASYMMETRY UNCERTAINTY

Asymmetry Uncertainty (%) vs. x (60 days at each energy, P=85%)

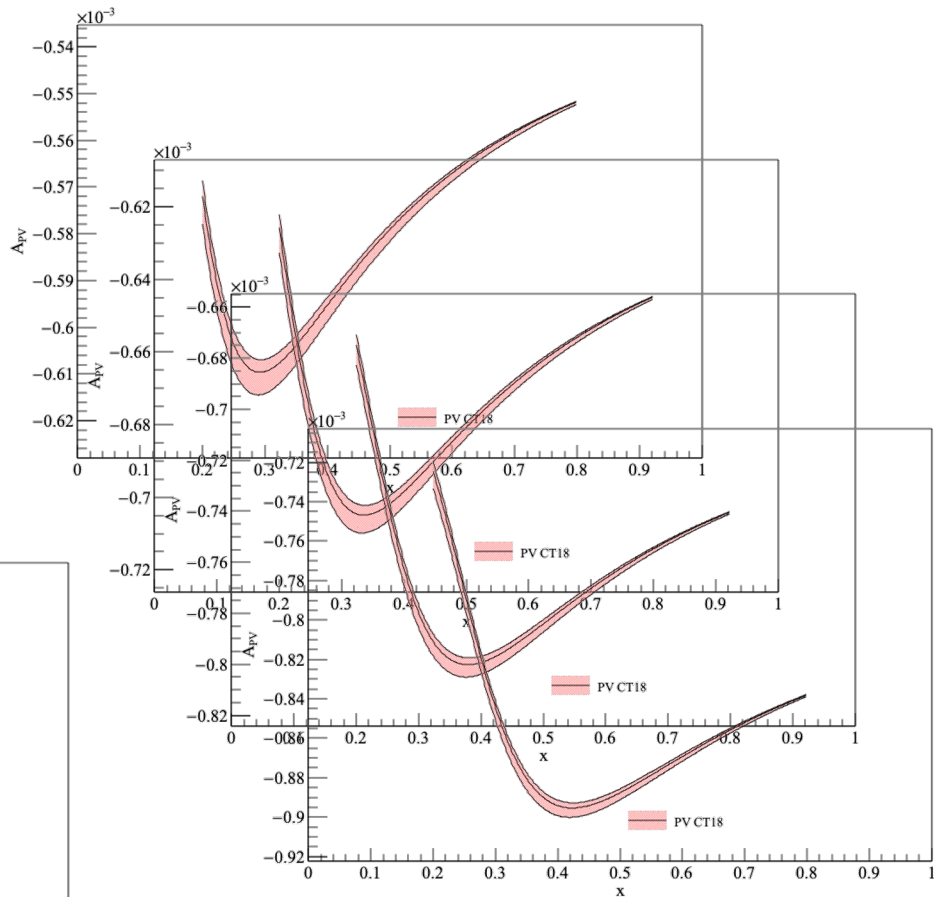
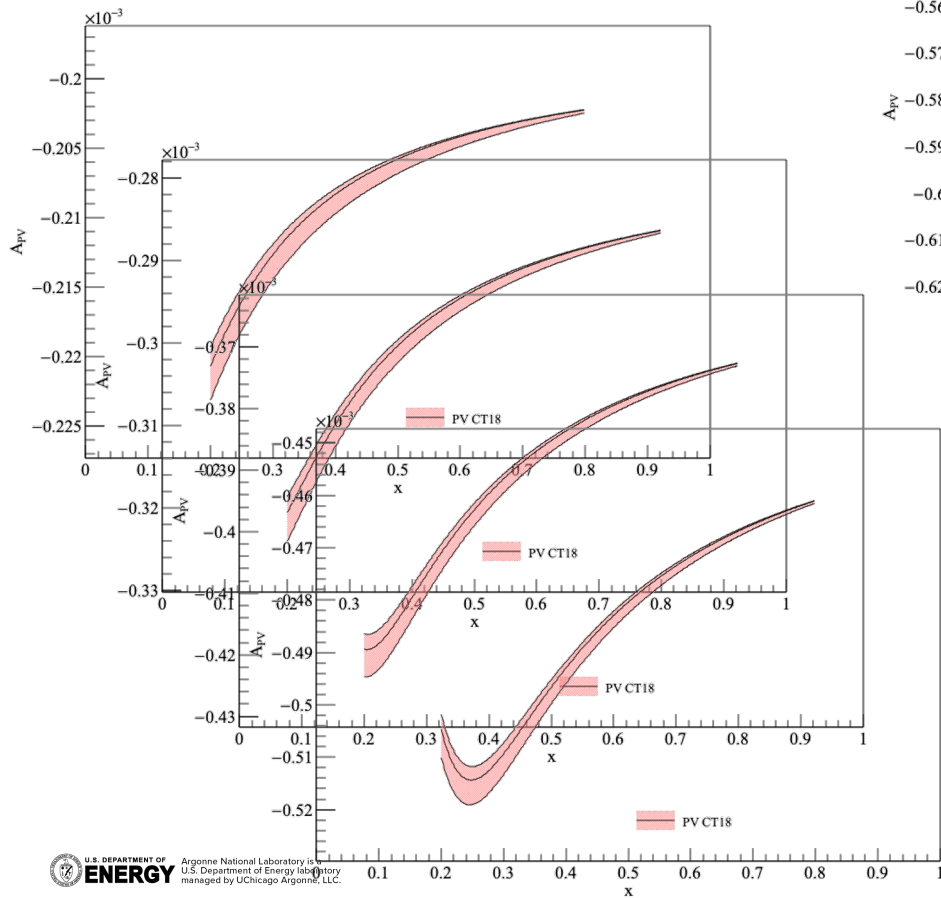


# $A_{LR}$ VS X

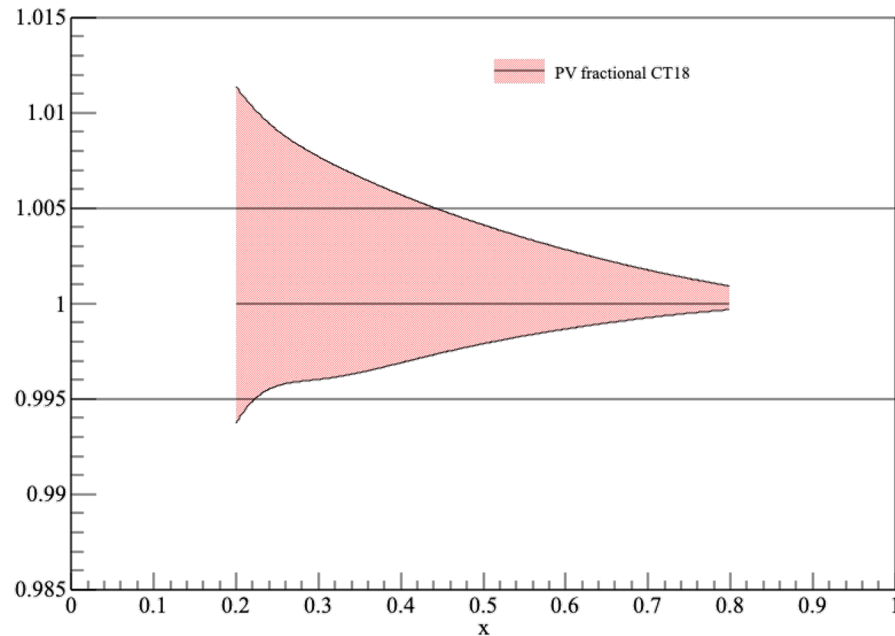
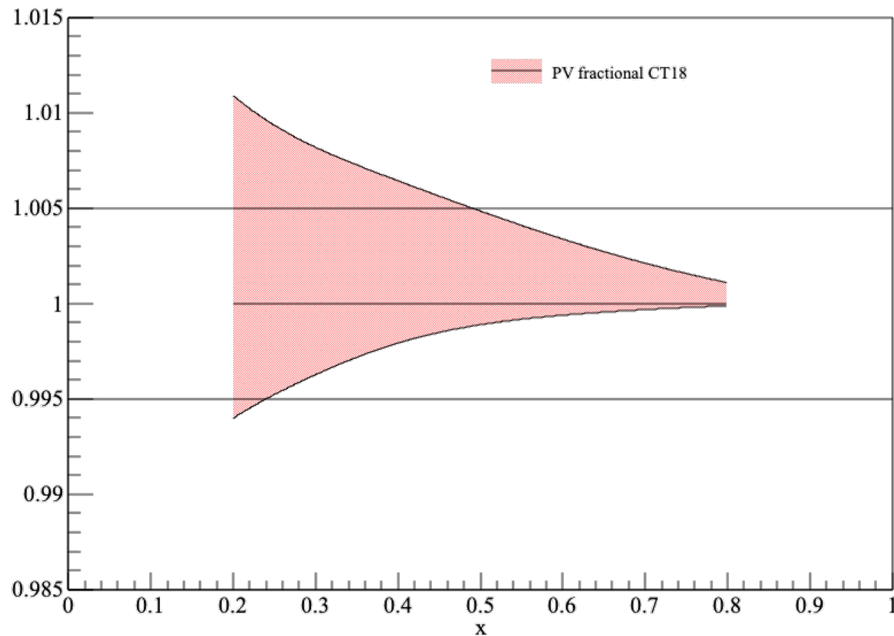


Calculate  $A_{LR}$  and associated PDF uncertainties for 2  $Q^2$  bins, 11 GeV beam

# $A_{LR}$ VS X



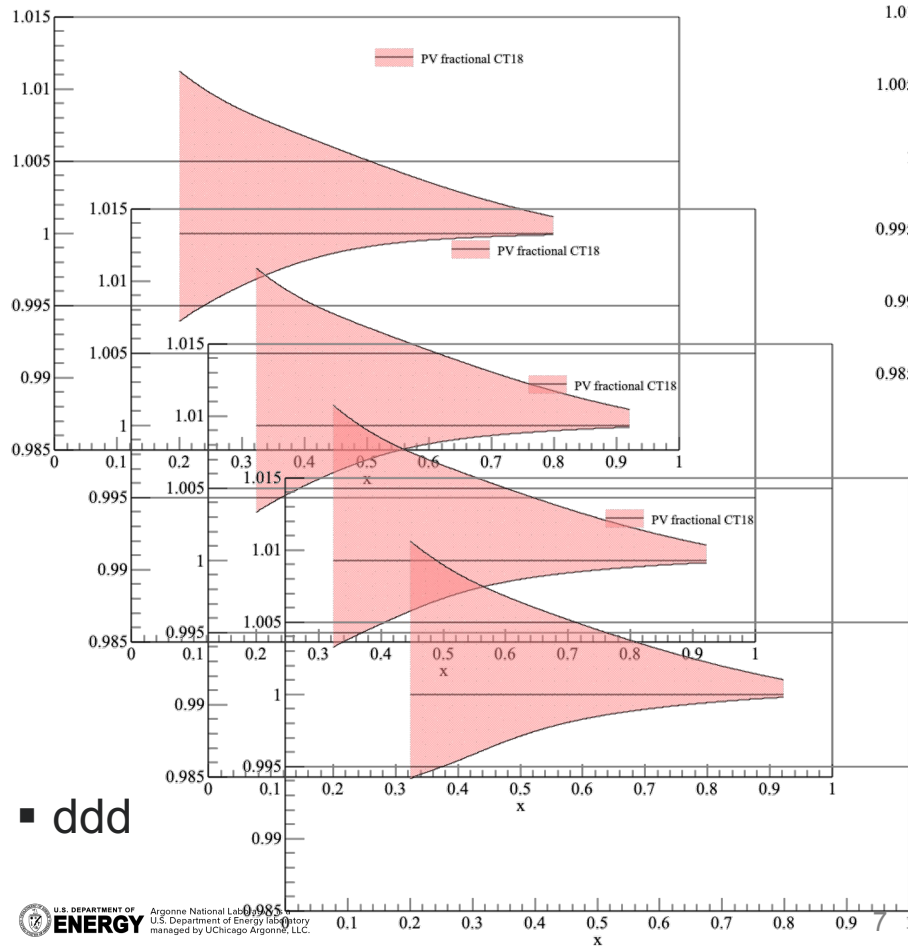
# $A_{LR}$ VS X (PERCENTAGE UNCERTAINTY)



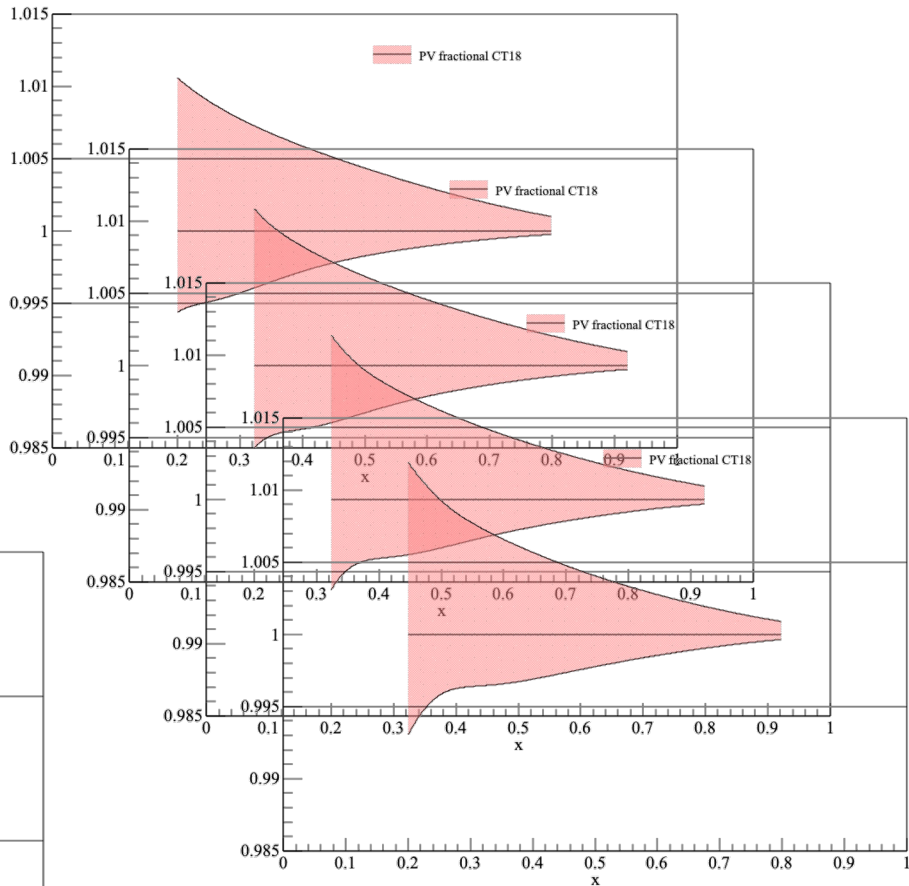
Uncertainties at high- $x < 0.5\%$

In general uncertainties  $< 1\%$

# $A_{LR}$ VS X



■ ddd



# $R_s$ AND $R_v$ VS $X$

$$A_{PV}^{DIS} = - \left( \frac{3G_F Q^2}{2\sqrt{2}\pi\alpha} \right) \frac{2C_{1u} - C_{1d} (1 + R_s) + Y (2C_{2u} - C_{2d}) R_v}{5 + R_s}$$

$$0.85 \lesssim R_v (x, Q^2) = \frac{u_v (x, Q^2) + d_v (x, Q^2)}{u (x, Q^2) + d (x, Q^2)} \leq 1$$

$$0.34 \lesssim Y \lesssim 1.0 \quad \text{and} \quad (2C_{2u} - C_{2d}) \approx 0.038$$

That is, in terms of

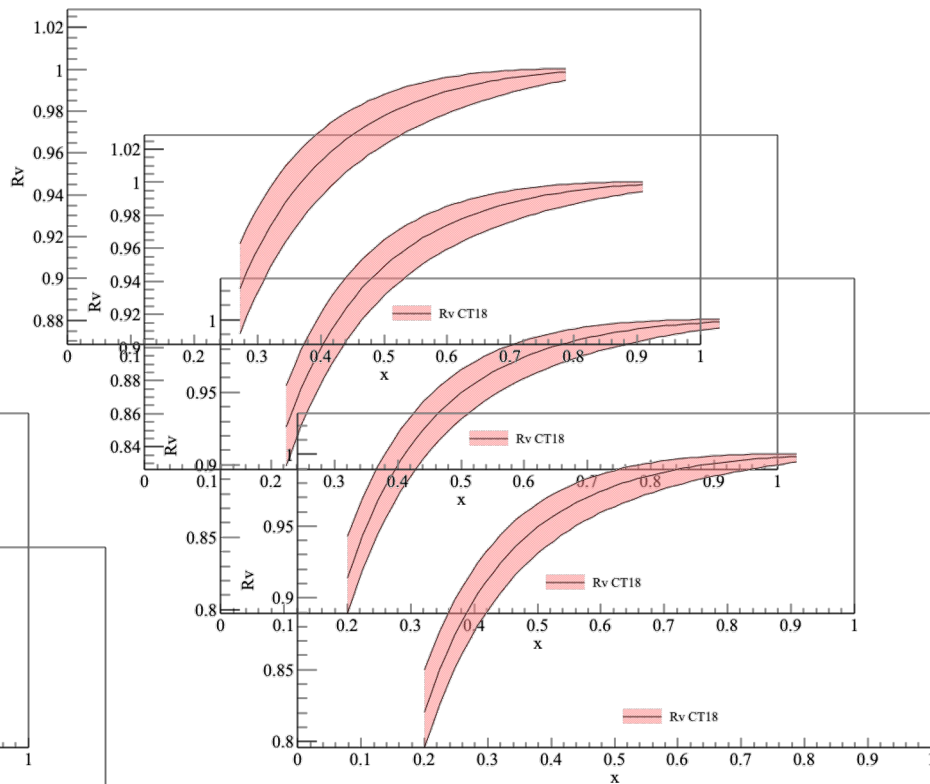
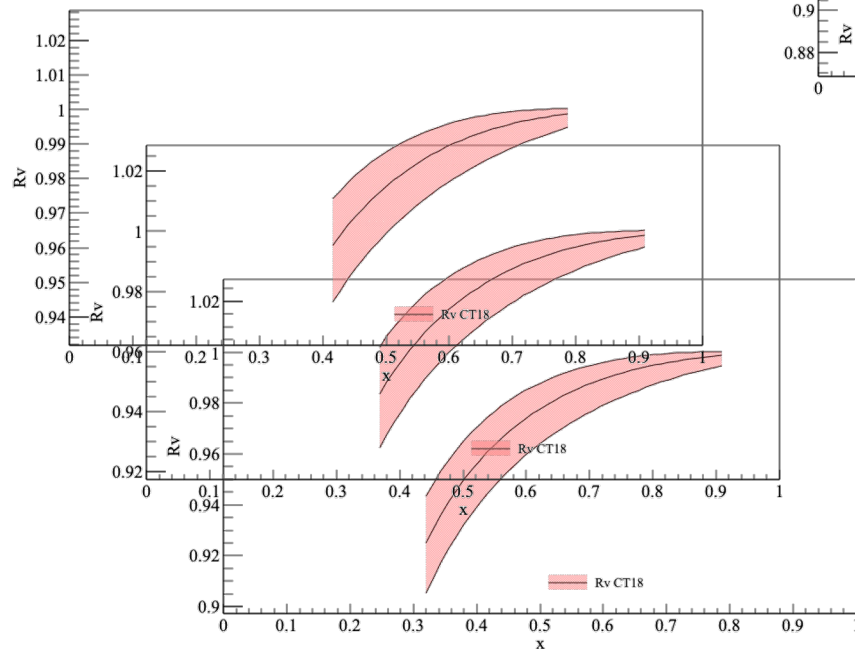
- $\delta A_{PV}$ ,  $\delta R_v$  will have little impact
- $\delta(2C_{2u} - C_{2d})$ ,  $\delta R_v$  is still important



# $R_V$ VS $x$

$\delta R_V \leq 2.5\%$  at low- $x$

$\delta R_V \leq 0.5\%$  at high- $x$



# $R_s$ AND $R_v$ VS $x$

$$A_{PV}^{DIS} = - \left( \frac{3G_F Q^2}{2\sqrt{2}\pi\alpha} \right) \frac{2C_{1u} - C_{1d} (1 + R_s) + Y (2C_{2u} - C_{2d}) R_v}{5 + R_s}$$

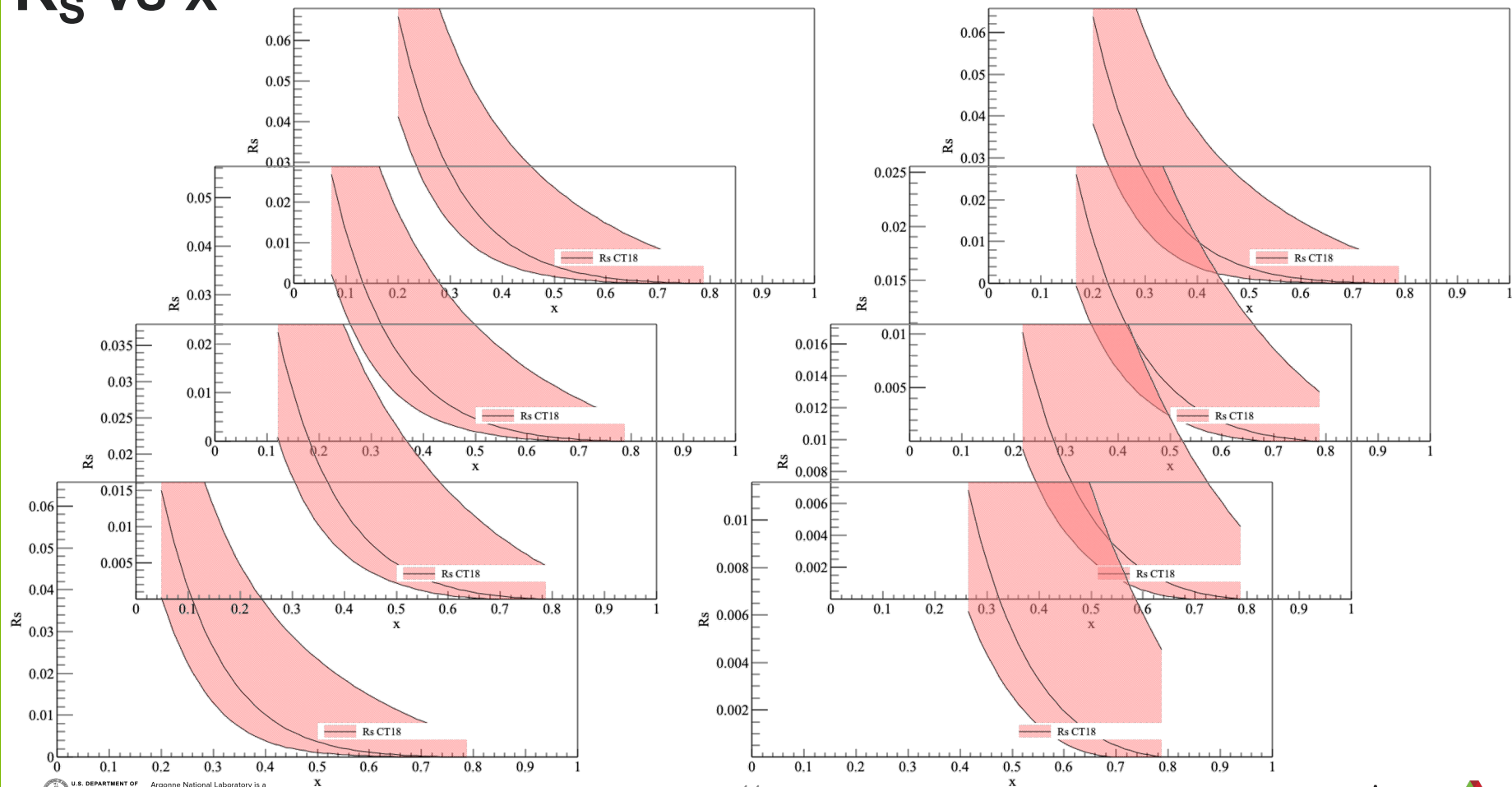
$$0 \leq R_s(x, Q^2) = 2 \frac{s(x, Q^2) + \bar{s}(x, Q^2)}{u(x, Q^2) + d(x, Q^2)} \lesssim 0.05$$

$$C_{1d} \approx 0.35$$

That is, in terms of

- $\delta A_{PV}$ ,  $\delta R_s$  will have little impact
- $\delta(2C_{2u} - C_{2d})$ ,  $\delta R_s$  is still important

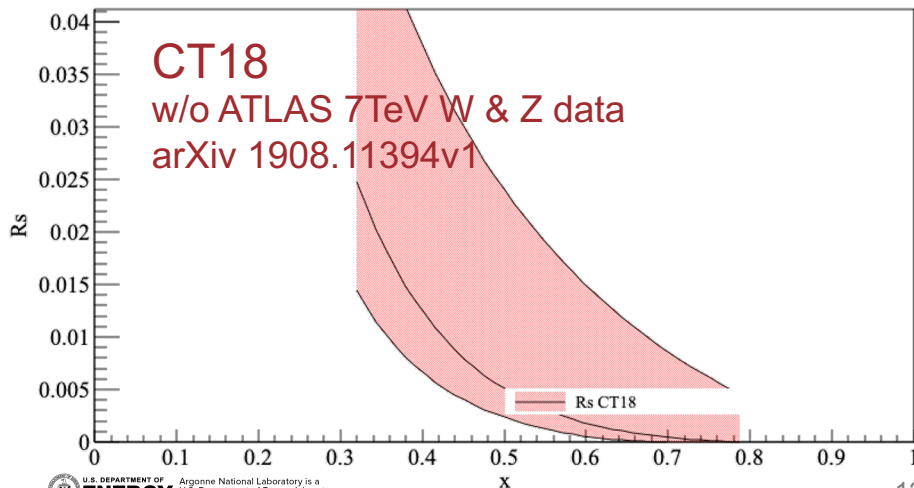
# $R_s$ VS X



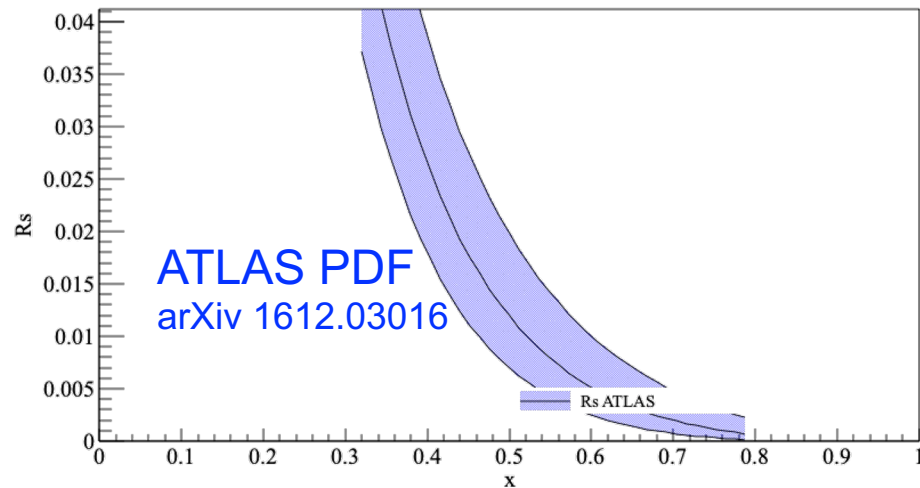
# $R_s$ VS X

Primary difference is the treatment of ATLAS 7 TeV W & Z measurements

$R_s$  6.500000 CT18



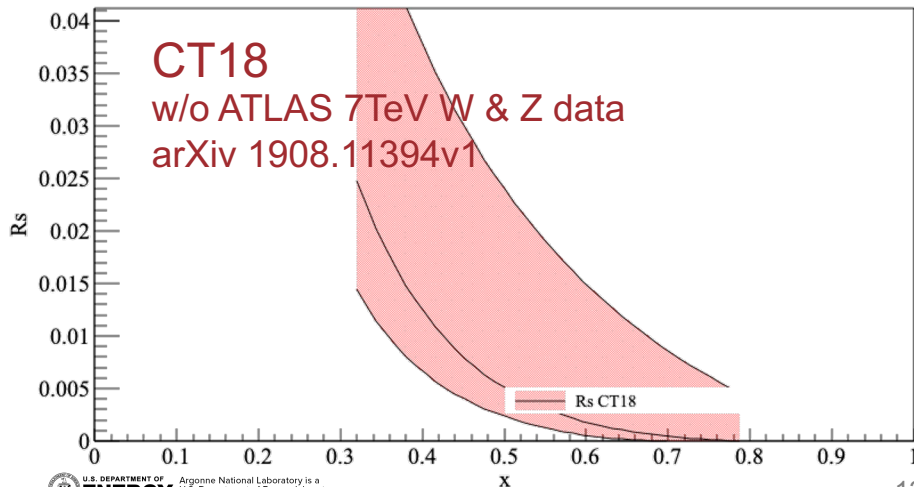
$R_s$  6.500000 ATLAS



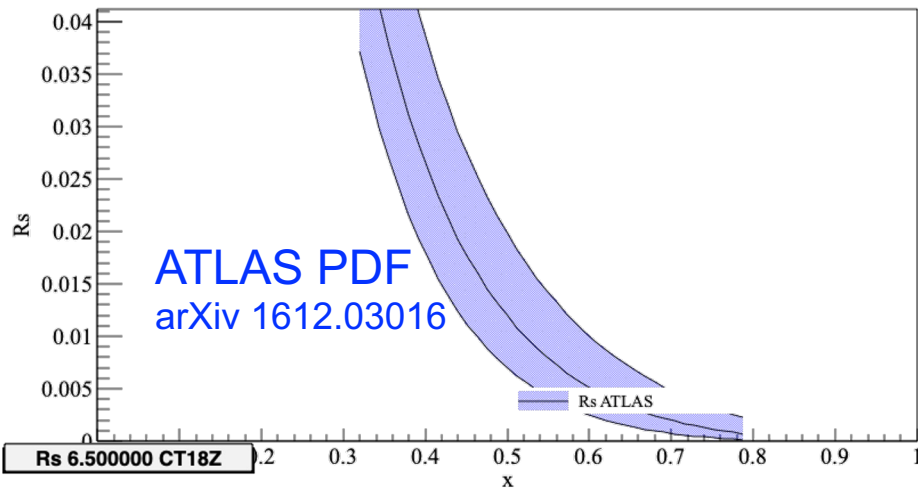
# $R_s$ VS X

Primary difference is the treatment of ATLAS 7 TeV W & Z measurements

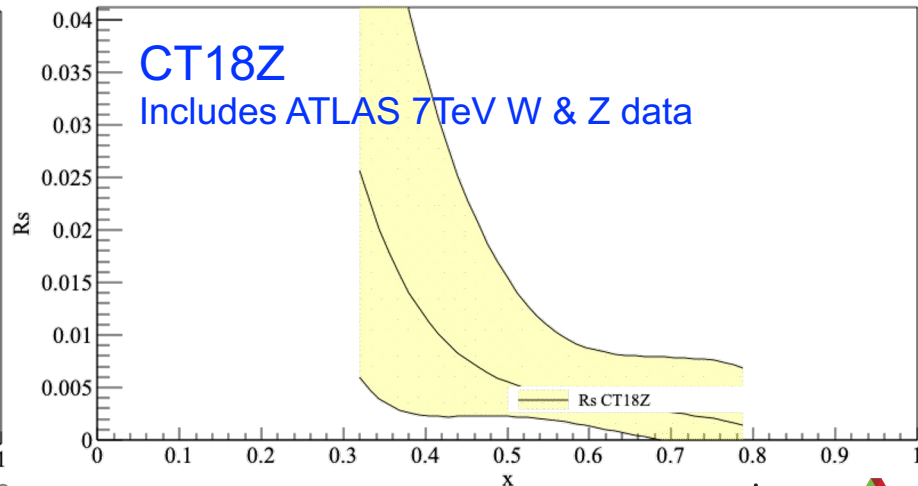
Rs 6.500000 CT18



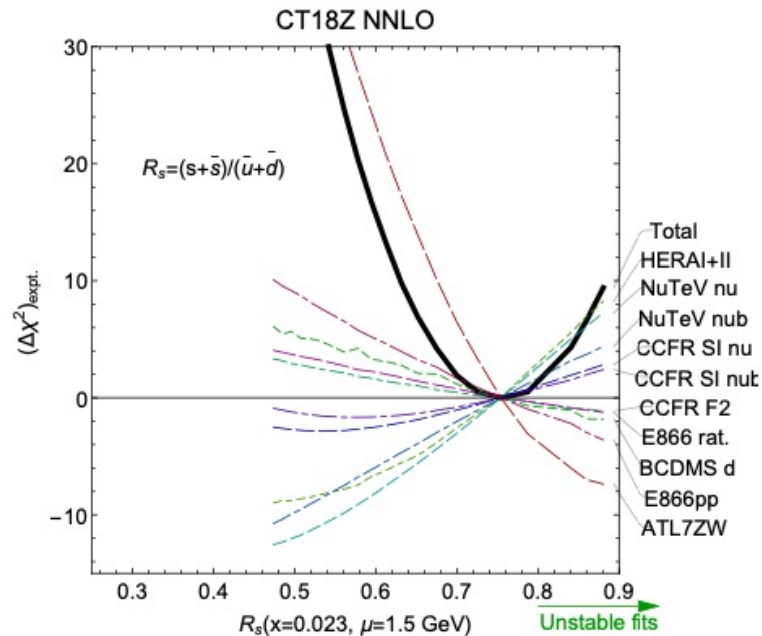
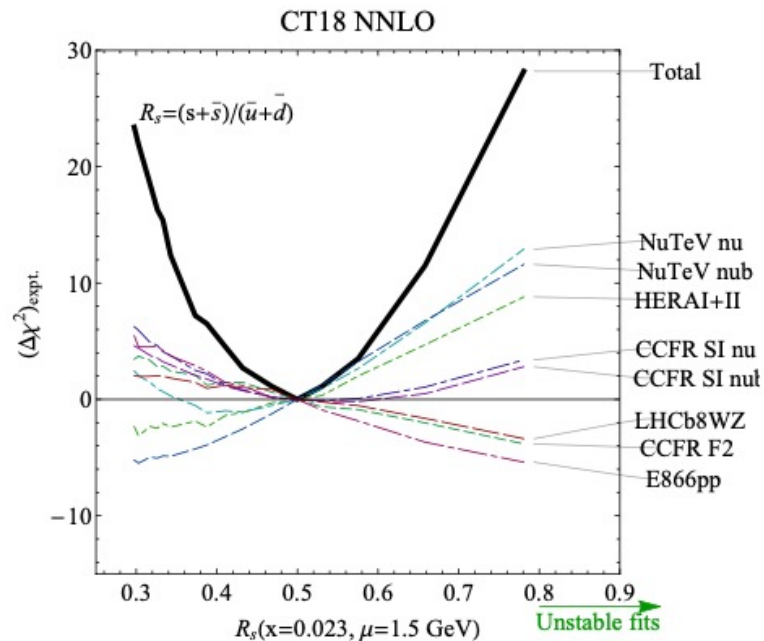
Rs 6.500000 ATLAS



Rs 6.500000 CT18Z



# CT18NLO CT18ZNLO LEGRANGE MULTIPLIER SCAN



# NEW ATLAS W & Z DATA

ATLAS, arXiv [2404.06204](https://arxiv.org/abs/2404.06204), submitted to EPJC.

PDF set	$W^- \rightarrow \ell^- \nu$	$W^+ \rightarrow \ell^+ \nu$	$Z \rightarrow \ell \ell$
$\sigma_{\text{fid}}(\sqrt{s} = 5.02 \text{ TeV}) [\text{pb}]$			
Data	$1384 \pm 16$	$2228 \pm 25$	$333.0 \pm 4.1$
CT18	$1360 \pm 10$ (scale) $^{+30}_{-40}$ (PDF)	$2200 \pm 10$ (scale) $^{+40}_{-70}$ (PDF)	$320 \pm 1$ (scale) $^{+5}_{-9}$ (PDF)
MSHT20	$1351^{+5}_{-6}$ (scale) $^{+22}_{-23}$ (PDF)	$2180 \pm 10$ (scale) $^{+30}_{-40}$ (PDF)	$324 \pm 1$ (scale) $^{+4}_{-5}$ (PDF)
NNPDF31	$1381 \pm 6$ (scale) $\pm 16$ (PDF)	$2232^{+8}_{-9}$ (scale) $\pm 25$ (PDF)	$329 \pm 1$ (scale) $\pm 4$ (PDF)
$\sigma_{\text{fid}}(\sqrt{s} = 13 \text{ TeV}) [\text{pb}]$			
Data	$3486 \pm 38$	$4571 \pm 49$	$780.3 \pm 10.4$
CT18	$3410^{+40}_{-20}$ (scale) $^{+60}_{-100}$ (PDF)	$4460^{+40}_{-30}$ (scale) $^{+80}_{-130}$ (PDF)	$748^{+5}_{-4}$ (scale) $^{+18}_{-25}$ (PDF)
MSHT20	$3400^{+40}_{-20}$ (scale) $^{+40}_{-60}$ (PDF)	$4460^{+40}_{-30}$ (scale) $^{+60}_{-70}$ (PDF)	$763^{+6}_{-4}$ (scale) $^{+9}_{-12}$ (PDF)
NNPDF31	$3450^{+40}_{-20}$ (scale) $\pm 30$ (PDF)	$4510^{+40}_{-30}$ (scale) $\pm 40$ (PDF)	$769^{+6}_{-4}$ (scale) $\pm 7$ (PDF)

# NEW CMS W & Z DATA

CMS, <http://cds.cern.ch/record/2868090> (2023)

$$\sqrt{s} = 5.02 \text{ TeV}$$

	Data	NNPDF3.1	NNPDF4.0	CT18	MSHT20
$W^+ \rightarrow \ell^+ \nu$	$2476 \pm 2_{\text{stat}} \pm 8_{\text{syst}} \pm 47_{\text{lum}}$	$2476^{+24}_{-24}$	$2513^{+18}_{-18}$	$2431^{+41}_{-41}$	$2421^{+28}_{-28}$
$W^- \rightarrow \ell^- \bar{\nu}$	$1525 \pm 2_{\text{stat}} \pm 5_{\text{syst}} \pm 29_{\text{lum}}$	$1519^{+18}_{-18}$	$1543^{+9}_{-9}$	$1505^{+25}_{-25}$	$1490^{+18}_{-18}$
$W^\pm \rightarrow \ell^\pm \nu$	$4001 \pm 3_{\text{stat}} \pm 10_{\text{syst}} \pm 76_{\text{lum}}$	$3995^{+38}_{-38}$	$4056^{+22}_{-22}$	$3936^{+64}_{-64}$	$3911^{+46}_{-46}$
$Z \rightarrow \ell^+ \ell^-$	$319.9 \pm 0.9_{\text{stat}} \pm 1.2_{\text{syst}} \pm 6.2_{\text{lum}}$	$319.5^{+3.7}_{-3.7}$	$325.2^{+1.8}_{-1.8}$	$310.2^{+4.9}_{-4.9}$	$314.0^{+3.5}_{-3.5}$
$W^+ / W^-$	$1.623 \pm 0.003_{\text{stat}} \pm 0.007_{\text{syst}}$	$1.631^{+0.016}_{-0.016}$	$1.628^{+0.013}_{-0.013}$	$1.615^{+0.014}_{-0.014}$	$1.625^{+0.008}_{-0.008}$
$W^\pm / Z$	$12.51 \pm 0.04_{\text{stat}} \pm 0.03_{\text{syst}}$	$12.51^{+0.12}_{-0.12}$	$12.47^{+0.08}_{-0.08}$	$12.69^{+0.13}_{-0.13}$	$12.46^{+0.05}_{-0.05}$

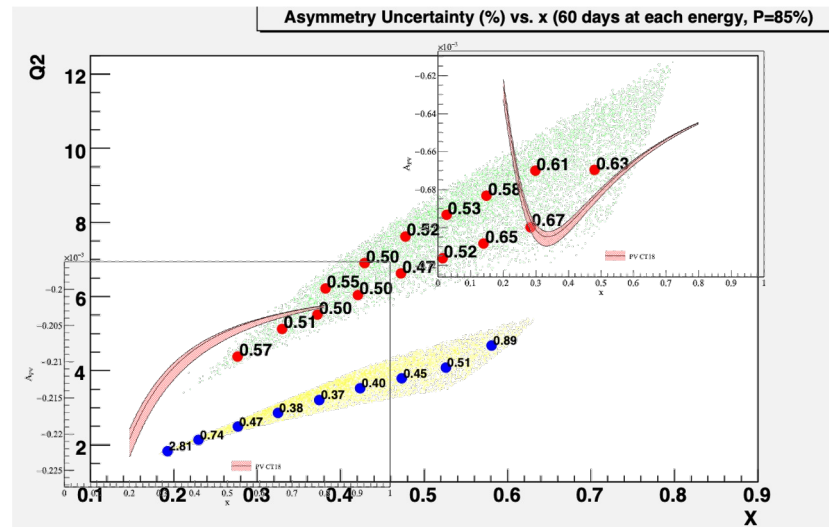
$$\sqrt{s} = 13 \text{ TeV}$$

	Data	NNPDF3.1	NNPDF4.0	CT18	MSHT20
$W^+ \rightarrow \ell^+ \nu$	$5318 \pm 4_{\text{stat}} \pm 18_{\text{syst}} \pm 86_{\text{lum}}$	$5061^{+62}_{-62}$	$5118^{+45}_{-45}$	$5003^{+89}_{-89}$	$4991^{+57}_{-57}$
$W^- \rightarrow \ell^- \bar{\nu}$	$4039 \pm 4_{\text{stat}} \pm 14_{\text{syst}} \pm 66_{\text{lum}}$	$3871^{+45}_{-45}$	$3930^{+28}_{-28}$	$3783^{+65}_{-65}$	$3816^{+43}_{-43}$
$W^\pm \rightarrow \ell^\pm \nu$	$9360 \pm 10_{\text{stat}} \pm 30_{\text{syst}} \pm 160_{\text{lum}}$	$8930^{+90}_{-90}$	$9050^{+60}_{-60}$	$8790^{+150}_{-150}$	$8810^{+100}_{-100}$
$Z \rightarrow \ell^+ \ell^-$	$775 \pm 2_{\text{stat}} \pm 3_{\text{syst}} \pm 13_{\text{lum}}$	$743^{+18}_{-18}$	$754^{+6}_{-6}$	$719^{+16}_{-16}$	$734^{+8}_{-8}$
$W^+ / W^-$	$1.317 \pm 0.002_{\text{stat}} \pm 0.005_{\text{syst}}$	$1.307^{+0.017}_{-0.017}$	$1.302^{+0.012}_{-0.012}$	$1.322^{+0.013}_{-0.013}$	$1.308^{+0.009}_{-0.009}$
$W^\pm / Z$	$12.08 \pm 0.03_{\text{stat}} \pm 0.03_{\text{syst}}$	$12.02^{+0.28}_{-0.28}$	$12.00^{+0.11}_{-0.11}$	$12.21^{+0.16}_{-0.16}$	$12.00^{+0.07}_{-0.07}$



# SUMMARY: PDF UNCERTAINTIES

- Under control at high-x
- $\delta R_v(x) = \frac{u_v(x)+d_v(x)}{u(x)+d(x)}$  small
- $\delta R_s(x) = \frac{s(x)+\bar{s}(x)}{u(x)+d(x)}$  new data
- Lattice contributions



The question is not about parton distribution uncertainties in 2024, but rather what these uncertainties will be in 203x.

PDF uncertainties appear to be under control  
We can sing like Cicadas!